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Assignment: 2(b)

① total number of colours $k = 5$

Number of marbles ~~placed~~ placed on each Pigeonhole

$$n = 4$$

the least number of marbles to be chosen which will guarantee there will be at least 4 marbles of same colour is

$$= k(n) + 1$$

$$= 5(4) + 1$$

$$= 21$$

② total number of Pigeonhole grades possible from 0 to 100 $= k = 101$ and $n = 1$

to have at least two students receive same score on the final exam is

$$= kn + 1$$

$$= 101(1) + 1$$

$$= 102$$

③ No of Pigeonhole $= 5 = k$

No of Pigeon ~~hole~~ in each Pigeonhole $= n = 5$

maximum number of students required in discrete maths class to be sure that at least six will receive the grade is

$$= k(n) + 1$$

$$= (5)5 + 1$$

$$= 26$$

④

total elements in sample space 'S' are 11

$$A = \{3, 5, 9\} \text{ and } B = \{3, 5, 7, 11\}$$

(i) $P(A) = \frac{|A|}{|S|}$

$$= 3/11$$

(ii) $P(\text{odd or prime number})$

$$= \text{total unique numbers of } A \text{ and } B / S$$

$$= 5/11$$

(iii)

$$\begin{aligned} P(B') &= 1 - P(B) \\ &= 1 - (4/11) \\ &= 7/11 \end{aligned}$$

5

given,

In Apple county, 51% adults were male

Percentage of female = $100 - 51\%$ ~~0.51~~

$$= 100 - 51\%$$

$$= 49\%$$

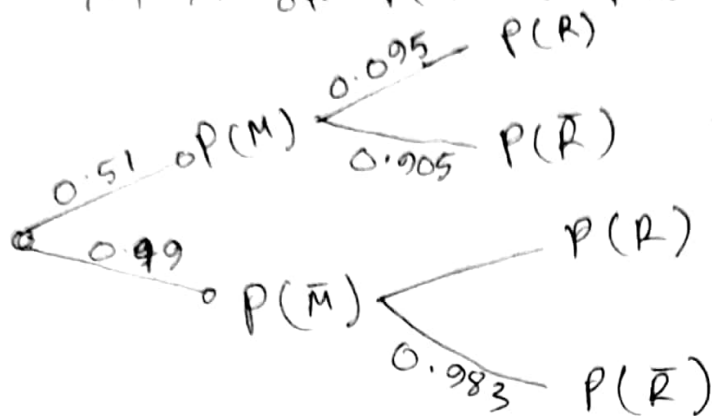
a) Probability of selected person is female =
Percentage of female

$$P(\bar{M}) = 49\%$$

$$P(\bar{M}) = 0.49$$

(b) 9.5% of male from rural area

1.7% of female from rural area



① Probability of getting some one who is from rural area given that person is male
 $= P(R|M)$

Using conditional Probability

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

$$P(R|M) = \frac{P(R \cap M)}{P(M)}$$

$$P(M) = 0.51, \quad P(R) = 0.095$$

$$\begin{aligned} P(R \cap M) &= P(M) \times P(R) \\ &= 0.51 \times 0.095 \\ &= 0.0484 \end{aligned}$$

$$\begin{aligned} P(R|M) &= \frac{0.0484}{0.51} \\ &= 0.0949 \end{aligned}$$

(11) Probability that selected subject is a male given that ~~he~~ he come from rural area is $P(M|R)$

$$P(M|R) = \frac{P(M \cap R)}{P(R)}$$

$$\begin{aligned} P(M \cap R) &= P(M) \times P(R) \\ &= 0.51 \times 0.095 \\ &= 0.0484 \end{aligned}$$

$$\begin{aligned} P(R) &= P(M \cap R) + P(\bar{M} \cap R) \\ &= P(M) \times P(R) + P(\bar{M}) \times P(R) \\ &= 0.51 \times 0.095 + 0.49 \times 0.017 \\ &= 0.0567 \end{aligned}$$

$$\begin{aligned} P(M|R) &= \frac{0.0484}{0.0567} \\ &= 0.8536 \end{aligned}$$

(iii) if Apple country has 100000 adult population

Number of female from urban area is =

total female - Number of female from rural area

total female = 49% of total population

$$= \frac{49}{100} \times 100,000$$

$$= 49000$$

Numbers of female from rural area = 1.7% of 49000

$$= \frac{1.7}{100} \times 49000$$

$$= 833$$

Number of female from urban area

$$= 49000 - 833$$

$$= 48167$$

⑥ Let, A = Event of person Purchases Latex Paint
 B = Event of person Purchase Semigloss

$$P(A) = 0.75, \quad P(B) = 0.25$$

R = Customer Purchased Roller

P = Customer Purchased Paint tray

$P(R/A)$ = Probability that person Purchased Roller when he already buy the Latex Paint.

$$P(R/A) = 0.60$$

$P(P/A)$ = Probability that person Purchased Paint tray when he already Purchased the Latex Paint.

$$P(P/A) = 0.25$$

Similarly,

$$P(R/B) = 0.3, \quad P(P/B) = 0.05$$

① Probability that person does not purchased roller after he purchased a Semigloss Paint means he had purchased Paint tray

$$P(P|B) = 0.5$$

② $P(P|A)$ = Probability that a person does not purchased roller after he purchased a latex paint.

means he bought Paint tray of the Latex Paint

$$= 0.25$$

③ By Bayes theorem

$$P(A|R) = \frac{P(R|A) P(A)}{P(R|A) P(A) + P(R|B) P(B)}$$

$$= \frac{(0.60)(0.75)}{(0.60)(0.75) + (0.3)(0.25)}$$

$$= \frac{0.45}{0.45 + 0.075}$$

$$= \frac{0.45}{0.525}$$

$$= 0.857$$