



## **Assignment-4**

**Group: 15**

**Subject: Discrete Structure.**

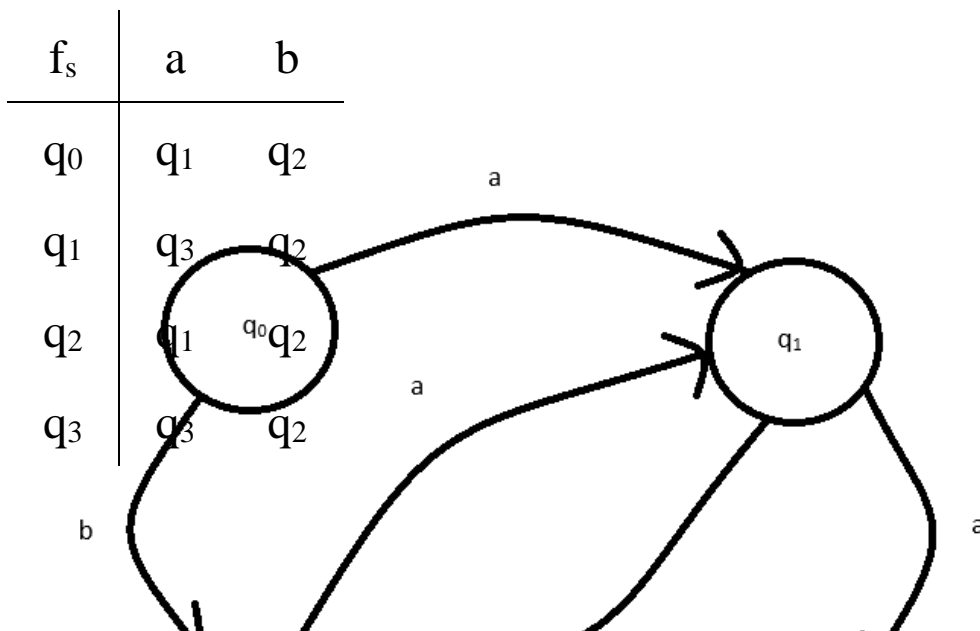
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## QUESTION 1

Let  $M = \{S, I, q_0, fs, F\}$  be the DFA such that  $S = \{q_0, q_1, q_2, q_3\}$ ,  $I = \{a, b\}$ ,  $F = \{q_1\}$ ,  $q_0$ =initial state and  $fs$  is given by:

$fs(q_0, a) = q_1$ ,	$fs(q_0, b) = q_2$
$fs(q_1, a) = q_3$ ,	$fs(q_1, b) = q_2$
$fs(q_2, a) = q_1$ ,	$fs(q_2, b) = q_2$
$fs(q_3, a) = q_3$ ,	$fs(q_3, b) = q_2$

i. Construct a state transition diagram of the DFA given the state transition function,  $fs$ .



ii) DFA can be applied to verify the password of an email.

DFA can be used to first match the email and after that the password can be matched using the dfa with the password stored for an email address.

Beside this DFA can help to determine whether a password is invalid or not like there should be one integer at least and one alphabet, there cannot be any special character as it would lead to a

dead state. Minimum length password DFA could be built in order to accept a password with minimum length and all specification.

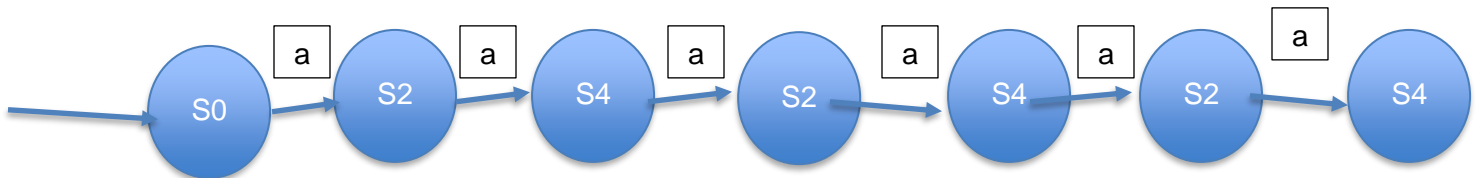
## Question 2:

i)

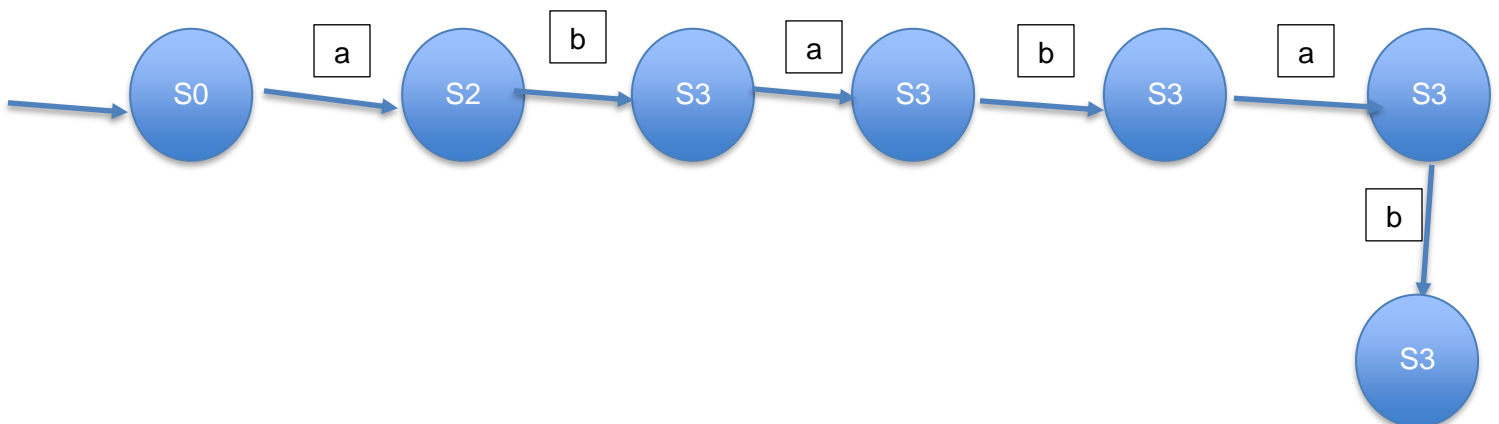
S	a	b
S1	S2	S1
S2	S3	S1
S3	S4	S3
S4	S3	S3
S5	S2	S4

ii)

a)  $W = \text{aaaaaa}$



b)  $W = \text{ababab}$



## Question 3:

i.

a)

States  $S=\{S_0, S_1, S_2, S_3, S_4, S_5\}$

Input symbols  $I=\{1, 0\}$

Start state  $q_0=S_0$

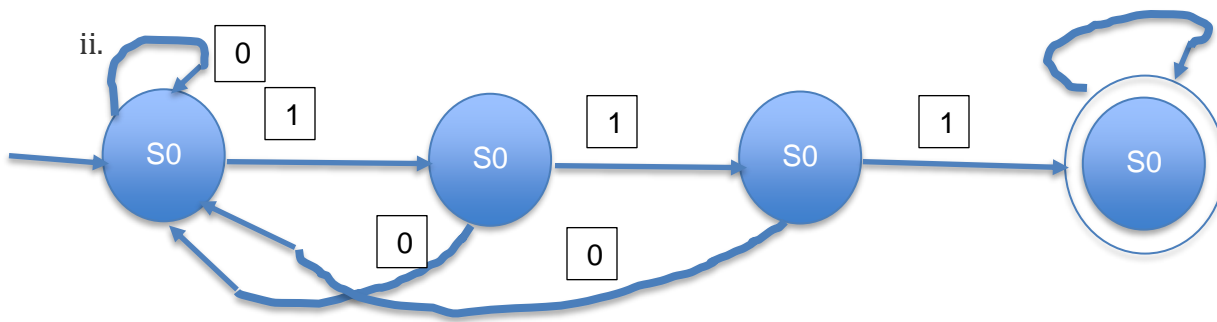
Final states  $F=\{S_0, S_5\}$

b)

Given string: 0011101100

Current state	Input	Next State
$S_0$	0	$S_0$
$S_0$	0	$S_0$
$S_0$	1	$S_1$
$S_1$	1	$S_2$
$S_2$	1	$S_3$
$S_3$	0	$S_5$
$S_5$	1	$S_5$
$S_5$	1	$S_5$
$S_5$	0	$S_4$
$S_4$	0	$S_4$

Since at the end of the string we are at state  $S_4$  and since  $S_4$  is not a final state, therefore, the string is not accepted by the DFA.



## QUESTION 4

### States:

$q_0$ : Wander

$q_1$ : Evade

$q_2$ : Attack

### Input:

A: not enemies

B: enemies & not vulnerable

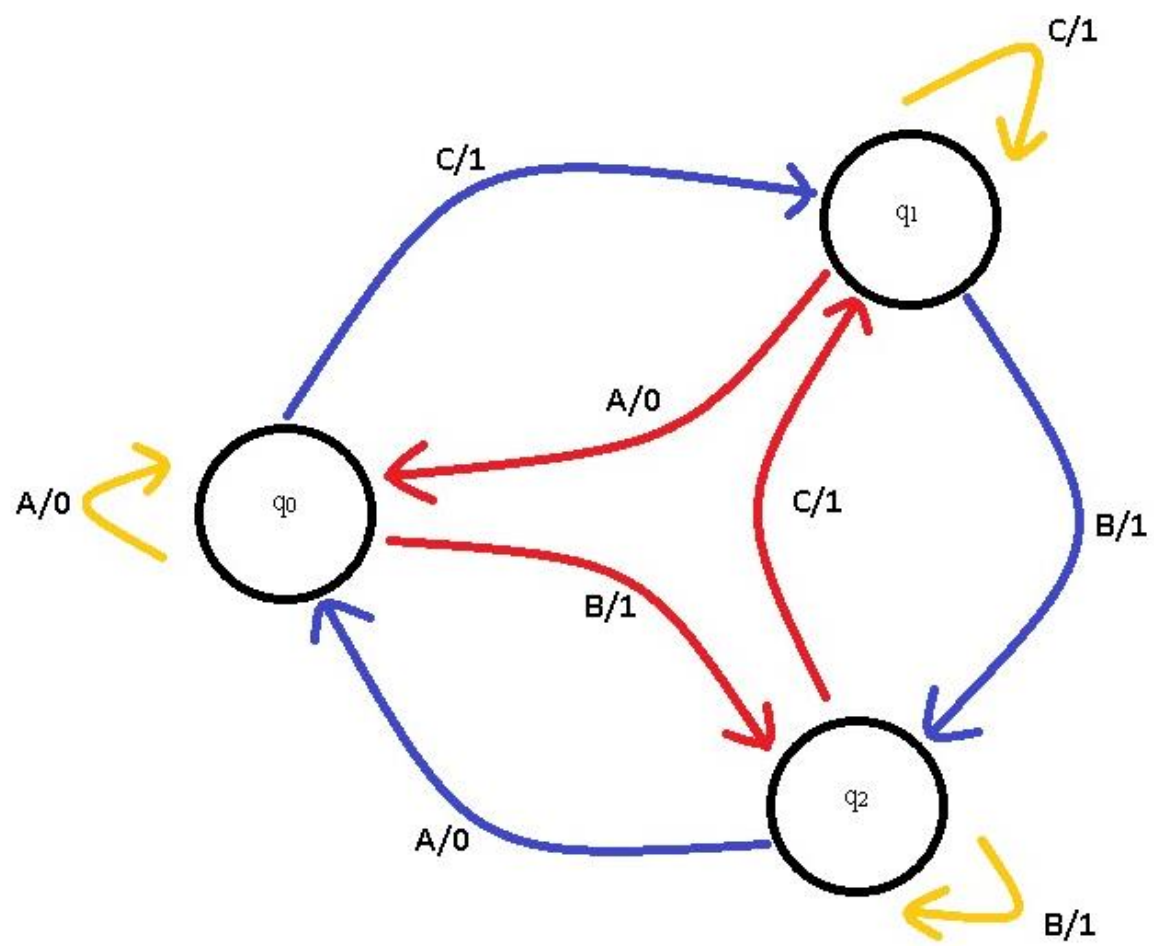
C: enemies & vulnerable

### Output:

0: shoot

1: not shoot

State	Input			Output		
	A	B	C	A	B	C
$q_0$	$q_0$	$q_2$	$q_1$	0	1	1
$q_1$	$q_0$	$q_2$	$q_1$	0	1	1
$q_2$	$q_0$	$q_2$	$q_1$	0	1	1







S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>8</sub>	S <sub>6</sub>	S <sub>9</sub>	0	0	0	0	0	0	0	0	1
S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	S <sub>9</sub>	1	1	1	1	1	1	1	1	1

