



UTM
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Assignment-1

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- **Question 1: Let the universal set be the set R of all real numbers and let**

**$A=\{x \in \mathbb{R} \mid 0 < x \leq 2\}$, $B=\{x \in \mathbb{R} \mid 1 \leq x < 4\}$
and $C=\{x \in \mathbb{R} \mid 3 \leq x < 9\}$. Find each of
the following:**

$$A=\{x \in \mathbb{R} \mid 0 < x \leq 2\} = (1,2)$$

$$B=\{x \in \mathbb{R} \mid 1 \leq x < 4\} = (1,2,3)$$

$$C=\{x \in \mathbb{R} \mid 3 \leq x < 9\} = (3,4,5,6,7,8)$$

- a) $A \cup C = (1,2) \cup (3,4,5,6,7,8)$

$$= (1,2,3,4,5,6,7,8)$$

- b) $(A \cup B)' = ((1,2) \cup (1,2,3))'$

$$= (1,2,3)' = \{x \in \mathbb{R} \mid x < 1 \ \& \ x > 3\}$$

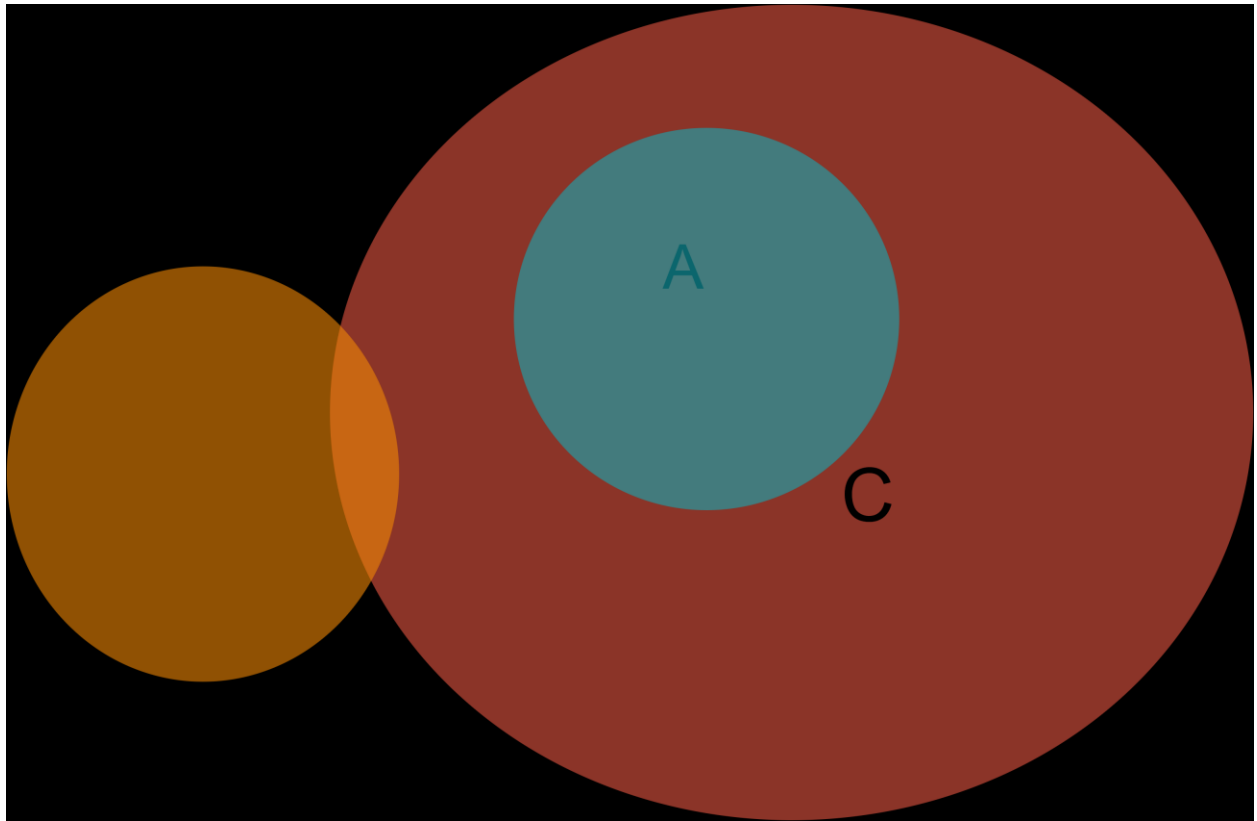
- c) $A' \cup B' = (1,2)' \cup (1,2,3)'$

$$= \{x \in \mathbb{R} \mid x < 1 \ \& \ x > 2\} \cup \{x \in \mathbb{R} \mid x < 1 \ \& \ x > 3\}$$

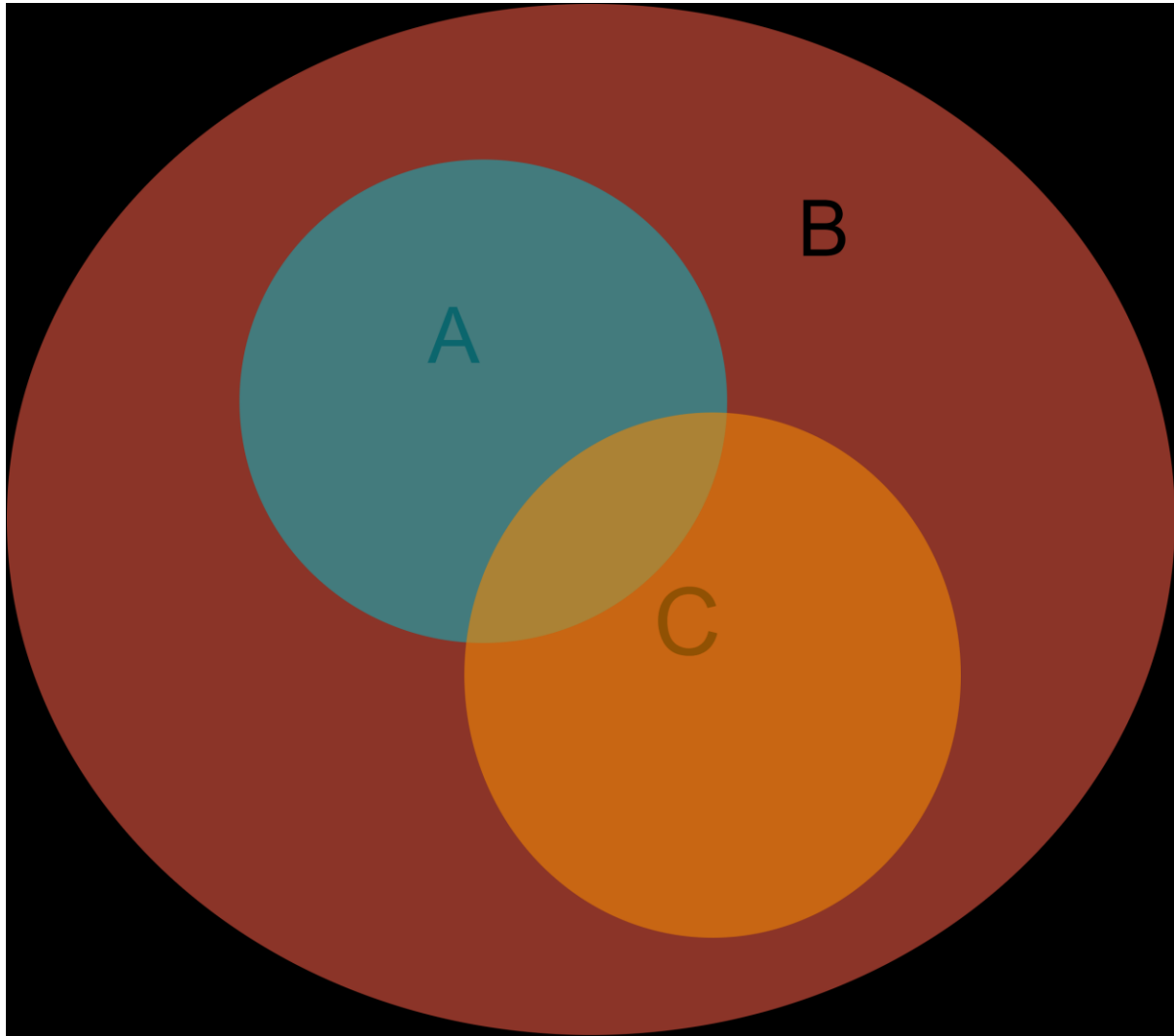
$$= \{x \in \mathbb{R} \mid x < 1 \ \& \ x > 3\}.$$

- Question 2: Draw Venn diagrams to describe sets A, B, and C that satisfy the given conditions:

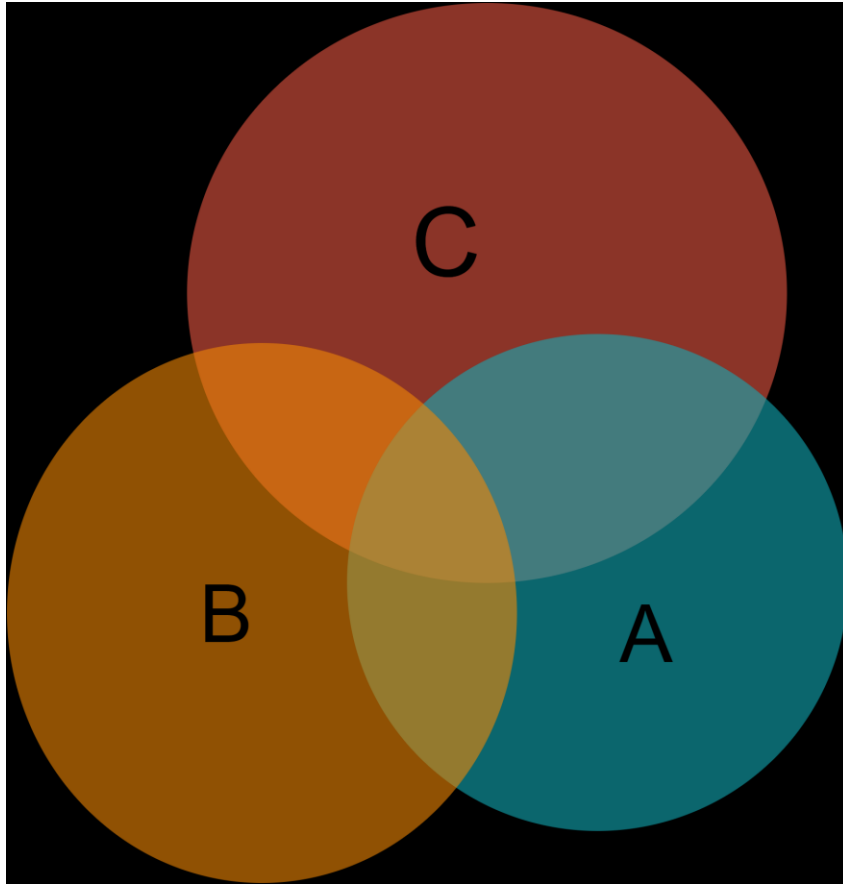
A) $A \cap B = \emptyset$, $A \subseteq C$, $C \cap B \neq \emptyset$



B) $A \subseteq B, C \subseteq B, A \cap C \neq \emptyset$



C) $A \cap B \neq \emptyset, B \cap C \neq \emptyset, A \cap C = \emptyset, A \not\subseteq B, C \not\subseteq B$



Question 3: Given two relations S and T from A to B ,

- $S \cap T = \{(x,y) \in A \times B \mid (x,y) \in S \text{ and } (x,y) \in T\}$

- $S \cup T = \{(x,y) \in A \times B \mid (x,y) \in S \text{ or } (x,y) \in T\}$
- Let $A = \{-1, 1, 2, 4\}$ and $B = \{1, 2\}$ and defined binary relations S and T from A to B as follows:
- For all $(x,y) \in A \times B$, $x S y \leftrightarrow |x| = |y|$
- For all $(x,y) \in A \times B$, $x T y \leftrightarrow x - y$ is even
- State explicitly which ordered pairs are in $A \times B$, S , T , $S \cap T$, and $S \cup T$.

Ans = Here,

$$A \times B = \{(-1,1), (-1,2), (1,1), (1,2), (2,1), (2,2), (4,1), (4,2)\}$$

$$S = \{(-1,1), (1,1), (2,2)\}$$

$$T = \{(-1,1), (1,1), (2,2), (4,2)\}$$

$$S \cap T = \{(-1,1), (1,1), (2,2)\}$$

$$S \cup T = \{(-1,1), (-1,2), (1,1), (1,2), (2,1), (2,2), (4,1), (4,2)\}$$

Discrete Group Assignment

4.

p	q	$\neg p \wedge q$	$\neg p \vee q$	$\neg((\neg p \wedge q) \vee (\neg p \vee q))$	$(p \wedge q)$	P
T	T	F	T	F	T	T

T	F	F	F	T	F	T
F	T	T	F	F	F	F
F	F	F	T	F	F	F

De Morgan's Law

5. Ordering $x, y, z : 1, 2, 3, 4, 5$

$R1 = \{(x, y) | x + y \leq 6\}$

$R1 = \{(1, 1); (1, 2); (1, 3); (1, 4); (1, 5); (2, 1); (2, 2); (2, 3); (2, 4); (3, 1); (3, 2); (3, 3); (4, 1); (4, 2); (5, 1)\}$

a) $A1 =$

1	1	1	1	1
---	---	---	---	---

 reflexive, symmetric, Transitive

1	1	1	1	0
---	---	---	---	---

1	1	1	0	0
---	---	---	---	---

1	1	0	0	0
---	---	---	---	---

1	0	0	0	0
---	---	---	---	---

$R2 = \{(x, y) | y > z\}$

$R2 = \{((2, 1); (3, 1); (3, 2); (3, 3); (4, 1); (4, 2); (4, 3); (5, 1)); (5, 2)); (5, 3)); (5, 4)\}$

b)

$$A2 = \begin{pmatrix} 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 \end{pmatrix}$$

$$1 \ 0 \ 0 \ 0 \ 0$$

$$1 \ 1 \ 1 \ 0 \ 0$$

$$1 \ 1 \ 1 \ 0 \ 0$$

$$1 \ 1 \ 1 \ 1 \ 0$$

c) yes it is. R1 is equivalent relation.
(reflexive, symmetric, Transitive)

d) yes it is. R2 is Partial order relation.
reflexive, asymmetric, Transitive)

6.

$$A1 = \begin{pmatrix} 1 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{pmatrix}; R1 = \{(1,1); (2,2); (2,3); (3,1); (3,3)\}$$

$$0 \ 1 \ 1$$

$$1 \ 0 \ 1$$

$$A2 = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{pmatrix}; R2 = \{(1,2); (2,2); (3,1); (3,3)\}$$

$$0 \ 1 \ 0$$

$$1 \ 0 \ 1$$

a) Matrix of relation $R1 \cup R2$.

$$R1 \cup R2 = \{(1,1); (1,2); (2,2); (2,3); (3,1); (3,3)\}$$

$$R1 \cup R2 \begin{matrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{matrix}$$

$$0 \ 1 \ 1$$

$$1 \ 0 \ 1$$

b) Matrix of relation $R1 \cap R2$.

$$R1 \cap R2 = \{(2,2); (3,1); (3,3)\}$$

$$R1 \cap R2 \begin{matrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{matrix}$$

$$0 \ 1 \ 0$$

$$1 \ 0 \ 1$$

7. If $f : R \rightarrow R$ and $g : R \rightarrow R$ are both one-to-one, is $f + g$ also one-to-one?

Justify your answer.

• Answer :

If $f(x) = x$ and $g(x) = -x$ is one to one.

Ex :

$$f(1) = 1 \quad g(1) = -1$$

$$f(2) = 2 \quad g(2) = -2$$

Etc

But, is $f+g$ also one to one?

$$(f+g): \mathbb{R} \rightarrow \mathbb{R}$$

$$(f+g)(x) = f(x) + g(x) \text{ for all real number } x$$

Ex:

$$(f+g)(1) = f(1) + g(1)$$

$$= 1 + (-1) = 0$$

$$(f+g)(2) = f(2) + g(2)$$

$$= 2 + (-2) = 0$$

Etc

So, this shows that $f+g$ is not one to one

8. With each step you take when climbing a staircase, you can move up either one stair or two stairs. As a result, you can climb the entire

staircase taking one stair at a time, taking two at a time, or taking a combination of one- or two-stair increments. For each integer $n \geq 1$, if the staircase consists of n stairs, let c_n be the number of different ways to climb the staircase. Find a recurrence relation for c_1, c_2, \dots, c_n .

Answer :

When $n=1$, $c(1)=1$

When $n=2$, $c(2)=2$

So its must greater than 1 or 2. When $n \geq 3$, the ways of climbing a staircase can divided into two groups based on the last step taken is either a single stair or two stairs together.

If the last step is a single stair, the number of ways is $c(n-1)$. If the last step is two

stairs together, there are $c(n-2)$ ways.

Therefore, $c(n)=c(n-1)+c(n-2)$.

Result :

$$c(1) = 1$$

$$c(2) = 2$$

$$c(n) = c(n-1) + c(n-2) \text{ when } n \geq 3$$

9. The Tribonacci sequence (t_n) is defined by the equations,

$t_0 = 0, t_1 = t_2 = 1, t_n = t_{n-1} + t_{n-2} + t_{n-3}$ for all $n \geq 3$.

a) Find t_7 .

b) Write a recursive algorithm to compute $t_n, n \geq 3$.

Answer :

a) we start from t_3

$$t_3 = t_{3-1} + t_{3-2} + t_{3-3} = t_2 + t_1 + t_0 = 1 + 1 + 0 = 2$$

$$t_4 = t_{4-1} + t_{4-2} + t_{4-3} = t_3 + t_2 + t_1 = 2 + 1 + 1 = 4$$

$$t_5 = t_{5-1} + t_{5-2} + t_{5-3} = t_4 + t_3 + t_2 = 4 + 2 + 1 = 7$$

$$t_6 = t_{6-1} + t_{6-2} + t_{6-3} = t_5 + t_4 + t_3 = 7 + 4 + 2 = 13$$

$$t_7 = t_{7-1} + t_{7-2} + t_{7-3} = t_6 + t_5 + t_4 = 13 + 7 + 4 = 24$$

$$t_7 = 24$$

b) //Fibonacci Series using Recursion

```
#include<bits/stdc++.h>
```

```
using namespace std;
```

```
int t(int n) t0 = 0, t1 = t2 = 1
```

```
{
```

```
if (n ≥ 3)
```

```
return n;
```

```
return t(n-1) + t(n-2) + t(n-3);
```

```
}
```

