SECI1013: DISCRETE STRUCTURE
2020/2021 – Semester 1

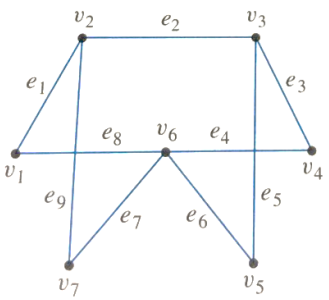
ASSIGNMENT 4

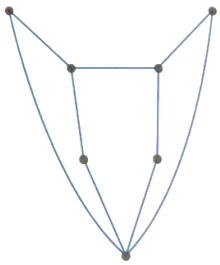
1. Let G be a graph with $V(G) = \{1, 2, \ldots., 10\}$, such that two numbers 'v' and 'w' in $V(G)$ are adjacent if and only if | v – w| ≤ 3. Draw the graph G and determine the numbers of edges, $e(G)$.

2. Model the following situation as graphs, draw each graphs and gives the corresponding adjacency matrix.
   (a) Ahmad and Bakri are friends. Ahmad is also friends with David and Chong. David, Bakri and Ehsan all friends.
   (Note that you may use the representation of A= Ahmad; B = Bakri; C = Chong; D = David; E= Ehsan)

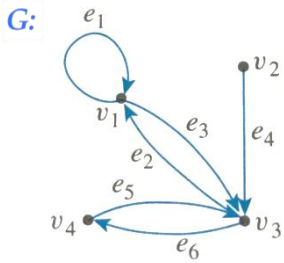
   (b) There are 5 subjects to be scheduled in the exam week: Discrete Mathematics (DM), Programming Technique (PT), Artificial Intelligence (AI), Probability Statistic (PS) and Information System (IS). The following subjects cannot be scheduled in the same time slot:-
      i. DM and IS
      ii. DM and PT
      iii. AI and PS
      iv. IS and AI

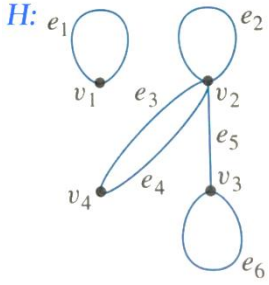
3. Show that the two drawing represent the same graph by labeling the vertices and edges of the right-hand drawing to correspond to left-hand drawing.





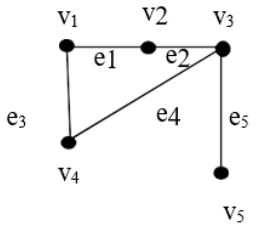
4. Find the adjacency and incidence matrices for the following graphs.



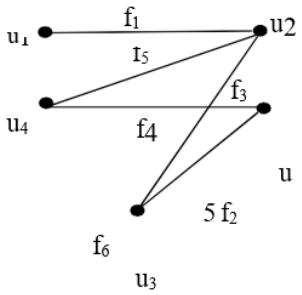


5. Determine whether the following graphs are isomorphic.

a)

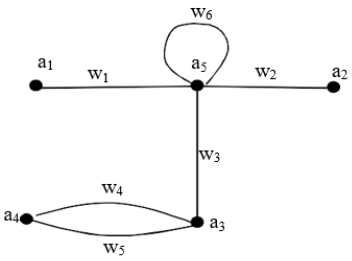


G1

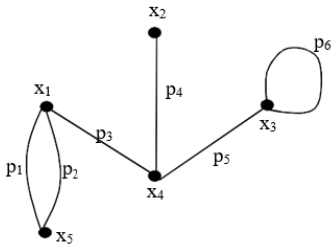


G2

b)

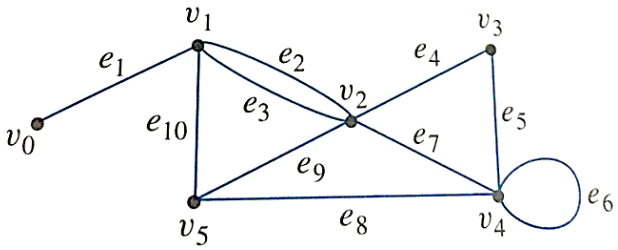


H1



H2

6. In the graph below, determine whether the following walks are trails, paths, closed walks, circuits/cycles, simple circuits or just walks.



a) $v_0 e_1 v_1 e_{10} v_5 e_9 v_2 e_2 v_1$

b) $v_4 e_7 v_2 e_9 v_5 e_{10} v_1 e_3 v_2 e_9 v_5$

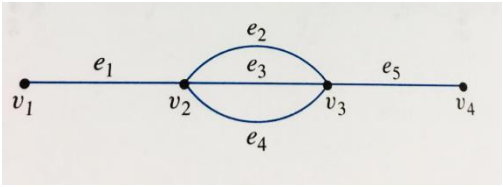
c) v_2

d) $v_5 e_9 v_2 e_4 v_3 e_5 v_4 e_6 v_4 e_8 v_5$

e) $v_2 e_4 v_3 e_5 v_4 e_8 v_5 e_9 v_2 e_7 v_4 e_5 v_3 e_4 v_2$

f) $v_3 e_5 v_4 e_8 v_5 e_{10} v_1 e_3 v_2$

7. Consider the following graph.

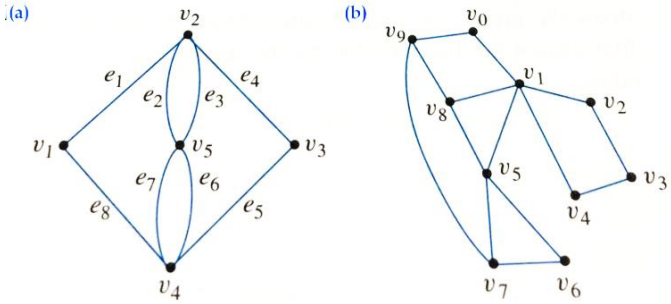


a) How many paths are there from v_1 to v_4?

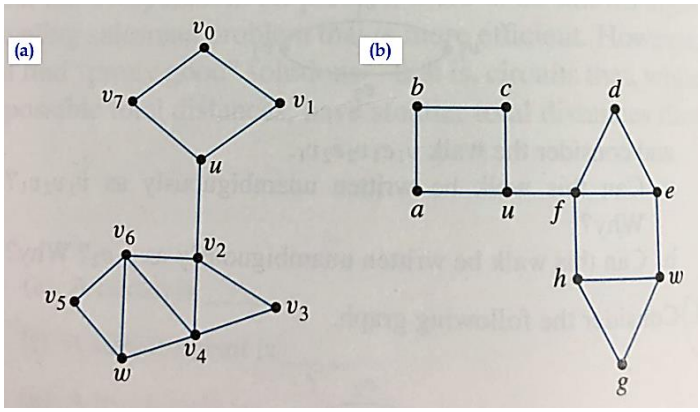
b) How many trails are there from v_1 to v_4?

c) How many walks are there from v_1 to v_4?

8. Determine which of the graphs in (a) – (b) have Euler circuits. If the graph does not have a Euler circuit, explain why not. If it does have a Euler circuit, describe one.



9. For each of graph in (a) – (b), determine whether there is an Euler path from u to w. If there is, find such a path.



10. For each of graph in (a) – (b), determine whether there is Hamiltonian circuit. If there is, exhibit one.

11. How many leaves does a full *3-ary* tree with 100 vertices have?

12. Find the following vertex/vertices in the rooted tree illustrated below.

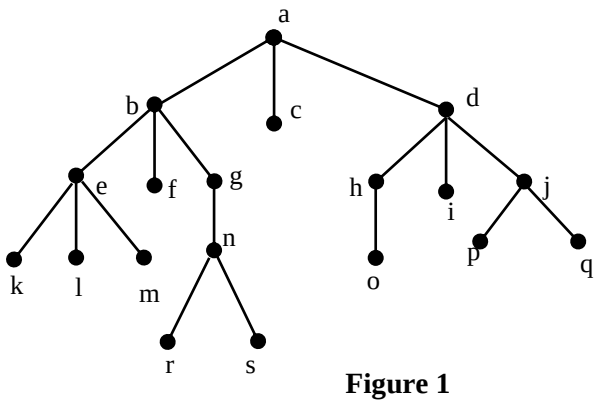
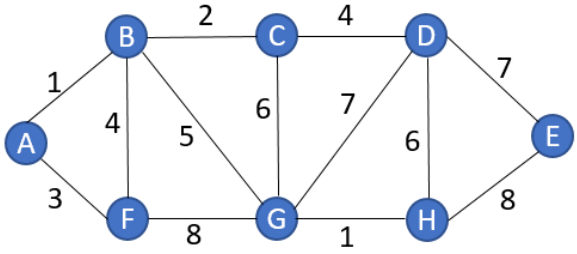


Figure 1

a) Root
b) Internal vertices
c) Leaves
d) Children of *n*
e) Parent of *e*
f) Siblings of *k*
g) Proper ancestors of *q*
h) Proper descendants of *b*

13. In which order are the vertices of ordered rooted tree in **Figure 1** is visited using *preorder*, *inorder* and *postorder*.

14. Find the minimum spanning tree for the following graph using Kruskal's algorithm.



15. Use Dijsktra's algorithm to find the shortest path from **M** to **T** for the following graph.