

Q1: a

How many numbers are there

$$6 \times 6 \times 6 = 216 \text{ numbers}$$

Q1: b

How many numbers are there if the digits are distinct

$$6 \times 5 \times 4 = 120 \text{ numbers}$$

How many numbers are there between 300 to 700 if only odd digit allow?

$$4 \times 6 \times 3 = 72 \text{ numbers}$$

Q2: a

5 men, 5 women

$$(6-1)! \times 5! = 5! \times 5! = 14400 \text{ ways}$$

Q2: b

The couple insisted to sit next to each other

$$(9-1)! \times (2)! = 8! \times 2! = 80640 \text{ ways}$$

Q2: c

Men and women sit alternately

$$(5-1)! \times 5! = 4! \times 5! = 2880 \text{ ways}$$

2/4

Q2: d

How many ways can photographer arrange in a row if Anitha and her husband sit next to each other

$$(11-1)! \times (2)! = 79833600 \text{ ways}$$

Q3: a

If no ties

$$5! = 120 \text{ ways}$$

Q3: b

Two sprinters tie

$$4! \times (5C2) = 24 \times 10 = 240 \text{ ways}$$

Q3: c

Two group of two sprint ties

$$3! \times (5C2) \times (3C2) = 6 \times 10 \times 3 = 180 \text{ ways}$$

Q4: a

dozen of croissants

~~(17C5)~~ = 6188 ways

Q4: b

Two dozen of croissants at least two of each kind

(17C5) = 6188 ways

Q4: c

Two dozen of croissants at least 5 chocolate and at least 3 almond croissants

(21C5) = 20349 ways

Discrete:

Q 4.5

a) each round we have Three options, team A wins the round team B wins the round or Tie.

$$2 \text{ Wins among 4 games } C(4,2) = \frac{4!}{2!(4-2)!} = 6$$

$$1 \text{ Win among 3 games } C(3,1) = \frac{3!}{1!(3-1)!} = 3$$

- we need to know the other games:

$$\text{2 Wins and 1 ties/wins: } C(4,2) \cdot C(3,1) \cdot 2 = 36$$

$$1 \text{ Wins \& 3 ties/wins: } C(3,1) \cdot C(4,3) \cdot 2^3 = 96$$

- we have to obtain number of scenarios.

$$\begin{aligned} \text{number of scenarios} &= 2 \cdot (36 + 96) \\ &= 2 \cdot 132 \\ &= 264 \end{aligned}$$

Q⁵

b. If 10 penalty Kicks are played
there are $2 \cdot 2 \cdot \dots \cdot 2 = 2^{10} = 1024$

- We know that 264 of the 1024 result in the first round of 10 penalty by part a.
- First round: 76
- Second round: 264 by part a

By the product rule:

$$\text{Number of scenarios} = 760 \cdot 264 = 200,640$$

Q⁵. c: we that is not settled after the first round of 10 penalty Kicks.

~~if the game~~

First round: 760 scenarios

Second round: 760

Sudden death: $2+2+2+2+2=10$ scenarios

By the product rule:

$$\text{Number of scenarios} = 760 \cdot 760 \cdot 10 = 5,776,000$$

Q6 A: we have to use Pigeonprinciple

- The pigeonholes are the answer sheets and we need to use the generalized pigeonhole principle to determine the number of pigeons needed for at least one pigeonhole to contain three pigeons. Because we have 4¹⁰ possible answer sheets, $2 \cdot 4^{10} + 1$ is the least possible number of students to make sure that the three answer sheets are the same.

7. A

History: 75% passed the $100 - 75 = 25\%$ Failed

Math: 65% passed so $100 - 65 = 35\%$ Failed

50% passed so 50% failed.

total failed students = $25\% + 35\% - 50\%$

so total passed students = 10%

so 10% of the student is 35

so 90% of the student is 315

so the total is $= 35 + 315 = 350$ students

Q 8: The answer is $\frac{171}{900}$

The numbers that ~~do not~~ does not have one anywhere $q^3 = 729$

There is $9 \times 10^2 = 900$

- There is $900 - 729 = 171$ with at least one

$$\frac{171}{900}$$

minimum 0
~~minimum~~
~~minimum~~

a) $\frac{10C6}{4! \cdot 2!} = 5 \times 21 = 105$

Number of ways = 105

b. From the question, we can only 5 cars.
we are going to Park all cars in the alternative
lots.

a.

10) Probability receives the message = $(0.4 \times 0.6) + (0.1 \times 0.8) + (0.5 \times 1) = 0.82$

b. This can be obtained by Bayes theorem

Required Probability = $(0.4 \times 0.6) \div (0.4 \times 0.6) + (0.1 \times 0.8) + (0.5 \times 1) = \frac{0.24}{0.82} = 0.29$

11) Probability the accident involved a light truck: $\frac{25}{45} \times 100 = 55.5\%$

12) The number of possible ways, without restrictions is $4^8 = 65536$.

$4 \times 3^8 = 26244$ disallowed ways

$4 \times 1^8 = 4$ ways to put all letters into one box twice

The number of allowed assignments is $65536 - 26244 + 4 = 39296$ ways