

Assignment - 2

Discrete Structure (SECI1013)

Group Members :

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■ Math no. done by —

- * Kazi Omeir Mustafa : 1, 2, 3, 12
- * Nazmul : 6, 7, 8, 9
- * Tanshiba : 4, 5, 10, 11

Ans to the Q.N-1

- ① According the question we have to form 3 digit numbers
1st, 2nd and 3rd place can be filled in 6 ways
So total will be $= 6 \times 6 \times 6 = 216$ (Ans)
- ② 1st, 2nd, and 3rd place can be filled as 6, 5, 4
ways
So total will be $= 6 \times 5 \times 4 = 120$
- ③ Between 300-700 only odd number should be
formed in 3 digits.
So 1st place can be filled in 4 ways where
3, 4, 6, 5 is only allowed.
and 2nd place can be filled in 6 ways
and for 3rd place 3, 5, 7 & odd numbers are
allowed, 3rd place can be filled in 3 ways.
Total $= 4 \times 6 \times 3$
 $= 72$

Ans to the Q.N-2

- ⑤ Men insist to sit next to each other $(6-1)! (5)!$
 $= (5)! (5)!$

except Anita, we have 5 men and 5 women

If all men want to sit together, where
6 person around a table $(6-1)!$ ways
and 5 men arranged in $5!$ ways.

If all men sit together then $(6-1)! (5)!$ ways

$$= (5)! (5)!$$
 ways.

$$= 14400$$
 ways

- ⑥ If couple sit next to each other $= (9-1)! (2)!$

If take 1 couple as a group $- (8)! (2)!$

we arrange 8 people around a table
in $(8-1)!$ ways. But in between can be rearranged
in $2!$ ways.

So, we can arrange couple who want
to sit next to each other in $(8-1)! 2!$ ways

$$= (8)! (2)!$$
 ways.

$$= 80640$$
 ways

Ans

- (c) If men, women sit in alternate sit, then $(5-1)!(5)!$
 $= (4)!(5)!$

If 5 women sit in alternate sits, then $(5-1)! \text{ways}$
it can be done.

5 men can be arranged in $5!$ ways.

so we can arrange man and women sit in
alternate sits in $(5-1)!(5)!$ ways

$$= (4)!(5)!$$
 ways.
 $= 2880$ ways

- (d) With Anita and her husband there are 12
people.

If Anita and her husband is group, there are
11 person remaining.

So in a line we can arrange in $11!$ ways
and for Anita and her husband $2!$ ways.

So, all Anita and her husband can stand
together in $(11)!(2)!$ ways.

$$= 79833600$$
 ways

Ans to the Q.N-3

① If no ties, and 5 sprinters
and they can finish in, 1st, 2nd, 3rd, 4th
and 5th positions.

So no. of ways for the sprinters can
finish, if there is no tie = $5! = 120$

② If there is 1 tie and 5 sprinters
and they can finish in 1st, 2nd, 3rd, 4th,
~~5th~~ positions

So number of ways for the sprinters
can finish, if there is 1 tie is $(4!) \times \binom{5}{2}$

$$= 24 \times 10$$

③ If there are 2 ties and 5 sprinters.
and they can finish in 1st, 2nd, 3rd position

So, no of ways for the sprinters can
finish, if there are 2 ties is $(3!) \times \binom{5}{2} \times \binom{3}{2}$

$$= 180$$

A

- (a) croissants = Plain, cherry, chocolate,
Almond, Apple, Broccoli.

∴ Ways to choose a dozen croissants

$$= 12C_6$$

$$= 924 \text{ ways}$$

- (b) Taking at least two of each kind,
in two dozen croissants,

$$\text{we get} = \frac{24!}{2! 2! 2! 2! 2! 2!}$$

$$= 9.69 \times 10^{21}$$

- (c) with at least five chocolate
croissants and at least three
almond croissants, in two
two dozen croissants,

$$\text{we get} = \frac{24!}{5! 3!}$$

$$= 8.62 \times 10^{20}.$$

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(b)

We know, there are 10 penalty kicks in a penalty scenario. For a tie in penalty attempts, in the first round the ways should be $(5,5)$.

∴ Possible ways to settle the game in 2nd round

$$= 10 + 1$$

= 11 scoring scenarios.

(Ans.)

(c)

since from (b) we get,

Possible scoring scenarios

= 11 (excluding $(5,5)$ way).

~~From~~ In the same way, for 2nd round

the total outcomes / possible scenarios = 11 (including $(5,5)$)

∴ Total possible scoring scenarios
for full set of penalty kicks = $11 + 11$
= 22.

(Ans.)

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(a) Let, the two teams be X and Y.
When the teams reaches the situation of penalty attempt, then any of the team need to score the maximum.

There are 10 ways which will determine the win or lose of the teams.

The possible ways for winning -

Team X = $(6, 4), (7, 3), (8, 2), (9, 1)$
 $(10, 0)$.

Team Y = $(4, 6), (3, 7), (2, 8), (1, 9)$
 $(0, 10)$

(Ans)

(x → G)

total number of attempts combination possible for a student "m",

For each question choose any 1 of the 4 option and there are 10 such questions

$$= 4 \times 4 = 1048576$$

It is given that at least 3 answer sheets will be identical.

According to Pigeon hole principle,

$$\left[\frac{(n-1)}{m} \right] + 1 = 3$$

$$\Rightarrow \left[\frac{(n-1)}{1048576} \right] = 3 - 1$$

$$\Rightarrow \frac{n-1}{1048576} \neq 2 \Rightarrow n-1 = 2 \times 1048576$$

$$\Rightarrow n-1 = 2097152$$

$$\Rightarrow n = 2097152 + 1$$

$$\Rightarrow n = 2097153$$

Ans:

Q7/1

The percentage of students that passed at least one subject is →

$$P(\text{History}) + P(\text{Mathematics}) - P(\text{both}) = 75\% + 65\% - 50\% \\ = 90\%$$

The percentage of students that failed both subjects is

$$100 - P(\text{Pass at least one sub}) = 100\% - 90\% = 10\%$$

We know that 35 students failed both

(let, T = total number of students)

$$T \times (10/100) = 35$$

$$\Rightarrow T = \frac{35 \times 100}{10} = 350$$

∴ we get T = 350 students.

Q→8/1

(case 1)

1 at one digit

301, 310, 312, 313, 314, 315, 316, 317, 318, 319, 321,
331, 341, 351, 361, 371, 381, 391 = 18

401, 410, ..., 491 = 18

501, 510, ..., 591 = 18

601, 610, ..., 691 = 18

701, 710, ..., 771 = 16

$$\text{total} = 18 + 18 + 18 + 18 + 16 = 88$$

(case 2)

1 at two digit

311, 411, 511, 611, 711

$$\text{total} = 5$$

∴ Probability of number chosen will have 1 as at

$$\text{least one digit} = \frac{5 + 88}{780 - 299}$$

$$= \frac{93}{481}$$

$$= 0.1933$$

Q29/

(a) ${}^{10}C_2 + {}^8C_4 = 115$

(b) ${}^6C_2 + {}^4C_4 = 16$
 $= 115 - 16 = 99$

\therefore empty lots are next to each other

Prob Probability = $\frac{99}{115} = 0.86$

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(a)

The probability the trainee receives the message

$$= (0.4)(0.6) + (0.1)(0.8) \\ + (0.5)(1)$$

$$= 0.82$$

chance of getting message,
 $P(E) = 0.4$
 $P(L) = 0.1$
 $P(H) = 0.5$

(Ans.)

Probability of trainee receive the message,
 $P'(E) = 0.6$
 $P'(L) = 0.8$
 $P'(H) = 1$

(b) According to Bayes theorem, the conditional probabilities that the trainee receives via email

$$= \frac{(0.4)(0.6) + (0.1)(0.8)}{(0.4)(0.6) + (0.1)(0.8) + (0.5)(1)}$$

$$= \frac{0.24}{0.82}$$

$$= 0.29$$

(Ans.)

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According to the Qus,

$$P\left(\frac{A}{C}\right) = \frac{20}{100000} = 0.00020$$

$$P\left(\frac{A}{T}\right) = \frac{25}{100000} = 0.00025$$

And, therefore,

$$P(T) = 0.4$$

Now,

$$\begin{aligned} P(C) &= 1 - P(T) \\ &= 1 - 0.4 \\ &= 0.6 \end{aligned}$$

Therefore,

the probability of the accident involved a light truck,

$$\begin{aligned} P(T/A) &= \frac{P\left(\frac{A}{T}\right) \cdot P(T)}{P\left(\frac{A}{C}\right) \cdot P(T) + P\left(\frac{A}{C}\right) \cdot P(C)} \\ &= \frac{(0.00025) \cdot (0.4)}{(0.00020) \cdot (0.4) + (0.00020) (0.6)} \\ &= 0.4545 \\ &\quad (\underline{\underline{\text{Ans}}}) \end{aligned}$$

Let us consider,

cars ~~C~~ = C

Light truck = T

And,

Fatal Accident = FA

Not a Fatal

Accident = A'

Ans to the QN-12

Let's say, no. of ways one can distribute the letter is N where one can place each letter in any 4 boxes, $|N| = 4^9$

If shapes have no box,
Let,

Set of tetrahedron = A

Set of cube = B

Set of Polyhedron = C

Set of dodecahedron = D

So,

$$|A| = |B| = |C| = |D| = 2^9$$

and $|A \cup B| = |B \cup C| = |C \cup D| = |D \cup A| = 1^7 = 1$

and, $|A \cap B \cap C \cap D| = 0$

So, $|A \cup B \cup C \cup D| = |A| + |B| + |C| + |D| - |A \cap D| - |B \cap C| - |C \cap D| - |D \cap A| + |A \cap B \cap C \cap D|$

$$\Rightarrow |A \cup B \cup C \cup D| = 2^9 + 2^9 + 2^7 + 2^9 - 1 - 1 - 1 - 1 + 0$$

$$\Rightarrow |A \cup B \cup C \cup D| = 2049$$

So 9 letters can be placed in 4 boxes
where at least one letter, $|N| - |A \cup B \cup C \cup D|$

$$= 4^9 - 4^4$$

$$= 49 - 2049$$

$$= 262144 - 2049$$

$$= 260100$$