

Group:

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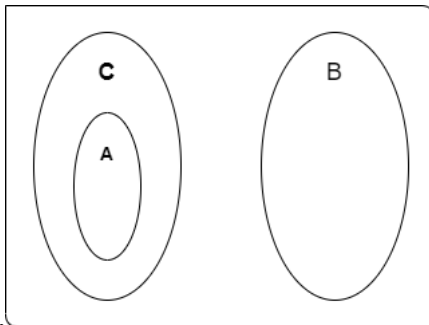
Rizal Rafiuddin

1. $A = \{1, 2\}$
 $B = \{1, 2, 3\}$
 $C = \{3, 4, 5, 6, 7, 8\}$

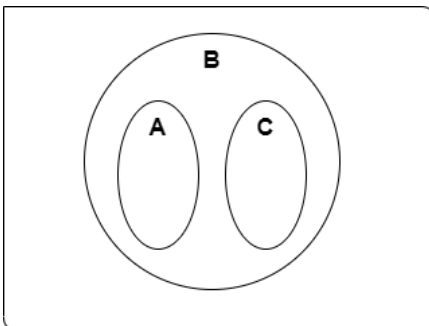
a. $A \cup C = \{1, 2, 3, 4, 5, 6, 7, 8\}$

b. $(A \cup B)' = \{4, 5, 6, 7, 8\}$

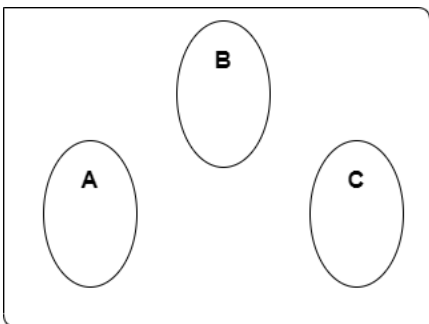
c. $A' \cup B' = \{3, 4, 5, 6, 7, 8\}$



2. A.



B.



C.

$$\begin{aligned}
3. \quad A &= \{-1, 1, 2, 4\} \\
B &= \{1, 2\} \\
A \times B &= \{(-1, 1), (-1, 2), (1, 1), (1, 2), (2, 1), (2, 2), (4, 1), (4, 2)\} \\
S &= \{(-1, 1), (1, 1), (2, 2)\} \\
T &= \{(-1, 1), (1, 1), (2, 2), (4, 2)\} \\
S \cup T &= \{(-1, 1), (1, 1), (2, 2), (4, 2)\} \\
S \cap T &= \{(-1, 1), (1, 1), (2, 2)\}
\end{aligned}$$

$$\begin{aligned}
4. \quad P &\equiv \neg ((\neg p \wedge q) \vee (\neg p \wedge \neg q)) \vee (p \wedge q) \\
P &\equiv \neg (\neg p \wedge q) \wedge \neg (\neg p \wedge \neg q) \vee (p \wedge q) && \text{(De Morgan's Law)} \\
P &\equiv (\neg \neg p \vee \neg q) \wedge \neg \neg (p \vee q) \vee (p \wedge q) && \text{(Double Negation Law)} \\
P &\equiv (p \vee \neg q) \wedge (p \vee q) \vee (p \wedge q) && \text{(Distributive Law)} \\
P &\equiv p \vee (\neg q \wedge q) \vee (p \wedge q) && \text{(Complement Law)} \\
P &\equiv p \vee \emptyset \vee (p \wedge q) && \text{(Property of Empty Set)} \\
P &\equiv p \vee (p \wedge q) && \text{(Absorption Law)} \\
P &\equiv P
\end{aligned}$$

$$\begin{array}{rccccc}
5. \text{ A)} & R1 & 1 & 2 & 3 & 4 & 5 \\
& 1 & 1 & 1 & 1 & 1 & 1 \\
& 2 & 1 & 1 & 1 & 1 & 0 \\
& 3 & 1 & 1 & 1 & 0 & 0 \\
& 4 & 1 & 1 & 0 & 0 & 0 \\
& 5 & 1 & 0 & 0 & 0 & 0
\end{array}$$

	R_2	1	2	3	4	5
	1	0	0	0	0	0
B)	2	1	0	0	0	0
	3	1	1	0	0	0
	4	1	1	1	0	0
	5	1	1	1	1	0

C) R_1 = not reflexive, symmetric, transitive, and not equivalence relation

D) R_2 = not reflexive, antisymmetric, not transitive, and not partial order relation

	1	1	0		0	0	0
6. A)	0	1	1	B)	0	1	0
	1	0	1		1	0	1

7. Let: $x_1, x_2 \in R$ be two distinct elements

then $g(x_1) \neq g(x_2)$, as g is one-to-one function.

And $f(g(x_1)) \neq f(g(x_2))$ as f is also one-one function.

$f+g$ may not one-to-one functions even if f and g are one-to-one.

consider $f(x) = x$ and $g(x) = -x$, then $f+g$ then is not one-to-one.

8.

$$C_1 = 1$$

$$C_2 = 2$$

$$n \geq 1$$

the recurrence:

$$C_n = C_{n-1} + C_{n-2}.$$

9.

a). $T_7 = 13$

b). Recursive algorithm:

Input n

Output $t(n)$

$T(n)\{$

If $(n=0)$

 return 0

Else if $(n=1 \text{ or } n=2)$

 return 1

return $t(t_n = t_{n-1} + t_{n-2} + t_{n-3})$