



## TUTORIAL 4

GROUP NAME : T5

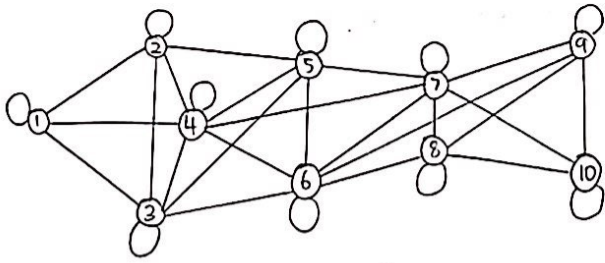
GROUP MEMBERS : SYASYA BINTI AZMAN

TAY WEI JIAN

NURIN SOFIYA BINTI ROSLE

SECTION : SEC11013 – 09

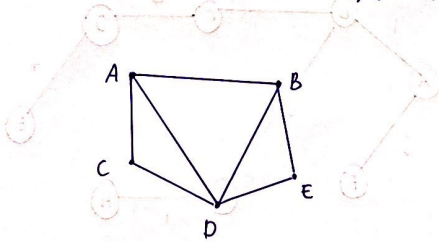
1) Graph G :



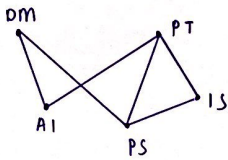
$e(G) = 33$

Question 2

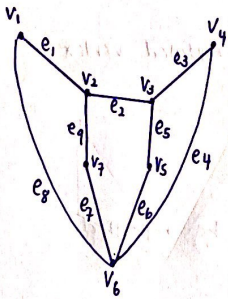
2 a) Let  $A = \text{Ahmad}$ ,  $B = \text{Bakri}$ ,  $C = \text{Chong}$ ,  $D = \text{David}$ ,  $E = \text{Ehsan}$ .



b) Let  $DM = \text{discrete Mathematics}$ ,  $PT = \text{Programming Technique}$ ,  $AI = \text{Artificial Intelligence}$ ,  
 $PS = \text{Probability statistic}$ ,  $IS = \text{Information system}$ .



Question 3



Question 4

Graph G:

$$A_G = \begin{matrix} & v_1 & v_2 & v_3 & v_4 \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{matrix} & \begin{bmatrix} 1 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 \\ 1 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \end{bmatrix} \end{matrix}$$

$$I_G = \begin{matrix} & e_1 & e_2 & e_3 & e_4 & e_5 & e_6 \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{matrix} & \begin{bmatrix} 2 & 1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix} \end{matrix}$$

Graph H:

$$A_H = \begin{matrix} & v_1 & v_2 & v_3 & v_4 \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{matrix} & \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 1 & 2 \\ 0 & 1 & 1 & 0 \\ 0 & 2 & 0 & 0 \end{bmatrix} \end{matrix}$$

$$I_H = \begin{matrix} & e_1 & e_2 & e_3 & e_4 & e_5 & e_6 \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ v_4 \end{matrix} & \begin{bmatrix} 2 & 0 & 0 & 0 & 0 & 0 \\ 0 & 2 & 1 & 1 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 & 2 \\ 0 & 0 & 1 & 1 & 0 & 0 \end{bmatrix} \end{matrix}$$

- 5) a) - Both  $G_1$  and  $G_2$  have 5 vertices and 5 edges
- Both  $G_1$  and  $G_2$  are connected and simple graph
  - Both  $G_1$  and  $G_2$  have 1 vertex with 1 degree, 3 vertices with 2 degrees and 1 vertex with 3 degrees
- $f: G_1 \rightarrow G_2$
- $f(v_1) = u_5$   
 $f(v_2) = u_4$   
 $f(v_3) = u_2$   
 $f(v_4) = u_3$   
 $f(v_5) = u_1$

$$M_{G_1} = \begin{matrix} & v_1 & v_2 & v_3 & v_4 & v_5 \\ \begin{matrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \end{matrix} & \begin{pmatrix} 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{pmatrix} \end{matrix}$$

$$M_{G_2} = \begin{matrix} & u_5 & u_4 & u_2 & u_3 & u_1 \\ \begin{matrix} u_5 \\ u_4 \\ u_2 \\ u_3 \\ u_1 \end{matrix} & \begin{pmatrix} 0 & 1 & 0 & 1 & 0 \\ 1 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 1 & 1 \\ 1 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{pmatrix} \end{matrix}$$

Since  $M_{G_1} = M_{G_2}$

$\therefore G_1$  and  $G_2$  are isomorphic

- b) - Both have 5 vertices and 6 edges
- Both are connected and simple graph
  - Both have 1 loop and 1 pair of parallel edges
- However,  $H_1$  has 2 vertices with 1 degree, 1 vertex with 2 degrees, 1 vertex with 3 degrees and 1 vertex with 5 degrees while  $H_2$  has 1 vertex with 1 degree, 1 vertex with 2 degrees and 3 vertices with 3 degrees
- $\therefore H_1$  and  $H_2$  are not isomorphic

- 6) a) trail  
 b) walk  
 c) trivial walk  
 d) circuit  
 e) closed walk  
 f) path

- 7) a) path 1:  $v_1, e_1, v_2, e_2, v_3, e_5, v_4$   
 path 2:  $v_1, e_1, v_2, e_3, v_3, e_5, v_4$   
 path 3:  $v_1, e_1, v_2, e_4, v_3, e_5, v_4$   
 Total: 3 paths

- b) trail 1:  $v_1, e_1, v_2, e_2, v_3, e_3, v_2, e_4, v_3, e_5, v_4$   
 trail 2:  $v_1, e_1, v_2, e_2, v_3, e_4, v_2, e_3, v_3, e_5, v_4$   
 trail 3:  $v_1, e_1, v_2, e_3, v_2, e_2, v_2, e_4, v_3, e_5, v_4$   
 trail 4:  $v_1, e_1, v_2, e_3, v_3, e_4, v_2, e_2, v_3, e_5, v_4$   
 trail 5:  $v_1, e_1, v_2, e_4, v_3, e_2, v_2, e_3, v_3, e_5, v_4$   
 trail 6:  $v_1, e_1, v_2, e_4, v_3, e_3, v_2, e_2, v_3, e_5, v_4$   
 Total: 6 trails

c)  $\infty$  walks

since all vertices and edges can be repeated as many times as possible  
 $\therefore$  There are infinite numbers of walks

8) a)

Vertex	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$
Degree	2	4	2	4	4

Since the degree of all vertices are even

$\therefore$  The graph has Euler circuit

Euler circuit:  $v_1 e_1 v_2 e_2 v_5 e_3 v_2 e_4 v_3 e_5 v_4 e_6 v_5 e_7 v_4 e_8 v_1$

b)

Vertex	$v_1$	$v_2$	$v_3$	$v_4$	$v_5$	$v_6$	$v_7$	$v_8$	$v_9$
Degree	2	5	2	2	2	4	2	3	3

Since not all vertices have even degrees

( $v_2, v_7, v_8$  and  $v_9$  have odd degree)

$\therefore$  The graph has no Euler circuit

9.

a)  $(u, v_1, v_0, v_7, u, v_2, v_3, v_4, v_6, v_2, v_4, w, v_3, v_6, w)$

b) no euler path



## Question 10

- a) - There is Hamilton circuit in graph (a). Hamilton circuit in this graph is  $V_0, V_7, V_1, V_2, V_3, V_4, V_5, V_6, V_0$ .
- Because there is no repeated vertex other than the first and last vertex.
- b) - There is no Hamilton circuit in graph (b) since there will be repeated vertex other than the first and last vertex.

$$\begin{aligned}
 11. \quad l &= \frac{(m-1)n+1}{m} \\
 &= \frac{(3-1)100+1}{3} \\
 &= \frac{201}{3} \\
 &= 67 \text{ leaves}
 \end{aligned}$$

12. a) a
- b) a, b, d, e, g, h, i, n.
- c) c, f, i, k, l, m, o, p, q, r, s.
- d) r, s.
- e) b
- f) l, m.
- g) i, d, a
- h) e, f, g, k, l, m, n, r, s.

13. preorder:

a, b, e, k, l, m, f, g, n, r, s, c, d,  
h, o, i, j, p, q.

inorder:

k, e, l, m, f, r, n, s, g, b, a, c,  
o, h, d, i, p, j, q

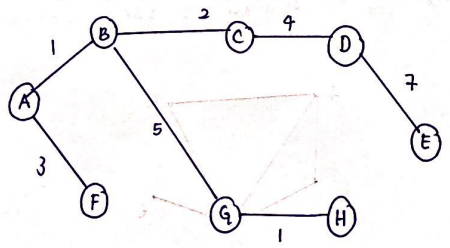
post order:

k, l, m, e, f, r, s, n, g, b, c, o, h,  
i, p, q, j, d, a

Question 14

- ~~AB 1~~
- ~~GH 1~~
- ~~BC 2~~
- ~~AF 3~~
- ~~BF 4~~
- ~~CD 4~~
- ~~BG 5~~
- ~~CG 6~~
- ~~DH 6~~
- ~~DG 7~~
- ~~DE 7~~
- ~~FG 8~~
- ~~HE 8~~

- MST
- AB 1
  - GH 1
  - BC 2
  - AF 3
  - CD 4
  - BG 5
  - DE 7



Total weight =  $1+1+2+3+4+5+7$   
 $= 23$



15.

V	M	N	O	P	Q	R	S	T
M	0	4	$\infty$	2	$\infty$	5	$\infty$	$\infty$
N	0	4	10	2	$\infty$	5	$\infty$	$\infty$
O	0	4	10	2	$\infty$	5	$\infty$	11
P	0	4	10	2	6	5	5	11
Q	0	4	10	2	6	5	5	11
R	0	4	10	2	6	5	5	6
S	0	4	10	2	6	5	5	6

the shortest path from M to T  
is by M, R, T, where the  
length is 6.