

SECI1013: DISCRETE STRUCTURE

Group No: 6

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ASSIGNMENT 2

1.
 - a. $6 \times 6 \times 6 = 216$
 - b. $6 \times 5 \times 4 = 120$
 - c. $2 \times 3 \times 3 = 18$

2.
 - a. $(6 - 1)! \times (5)! = 14400$
 - b. $(9-1)! \times 2! = 80640$
 - c. Men and women sit in alternate seats $= (5-1)!(5)!$
 $= (4)!(5)!$
 $= 2880$
 - d. $11! \times 2! = 79833600$

3.
 - a. $5 \times 4 \times 3 \times 2 \times 1 = 120$
 - b. $4! \times C(5,2) = 24 \times 10$
 $= 240$
 - c. $3! \times C(5,2) \times C(3,2) = 6 \times 10 \times 3$
 $= 180$

4.
 - a. $n = 6, r = 12$
 $C(6 + 12 - 1, 12) = 6188$
 - b. $n = 6, r = 12$
 $C(6 + 12 - 1, 12) = 6188$
 - c. $n = 6, r = 16$
 $C(6 + 16 - 1, 16) = 20349$

5.
 - a. 2 wins and 1 ties/wins: $C(4,2) \times C(3,1) \times 2 = 36$
1 win and 3 ties/wins: $C(3,1) \times C(4,3) \times 2^3 = 96$
 $2 \times (36 + 96) = 264$
 - b. Penalty kicks = $2^{10} = 1024$
First round = $1000 - 264 = 760$
Second round = 264
 $760 \times 264 = 200640$
 - c. First round = Second round = 760
Sudden-death = $2 + 2 + 2 + 2 + 2 = 10$
 $760 \times 760 \times 10 = 577600$

6.

Total 4 possibilities for each question

$$\text{Total possibilities} = 4^{10}, M = 3$$

$$n = k(M - 1) + 1$$

$$= 4^{10} \times (3 - 1) + 1$$

$$= 2097153$$

7. $P(H) = 0.75$ $P(H') = 0.25$

$$P(M) = 0.65$$
 $P(M') = 0.35$

$$P(H \cap M) = 0.50$$
 $H' \cap M' = 35 \text{ participates}$

$$P(H \cup M) = 0.75 + 0.65 - 0.50 = 0.90$$

$$P(H' \cap M') = 1 - 0.90 = 0.10$$

Let T = Numbers of candidates

$$\frac{10}{100} \times T = 35$$

$$T = 350$$

8. Number between 300 to 780 = $780 - 300 + 1 = 481$

1 in 2 digits

$$311,411,511,611,711 = 5$$

1 in 1 digit

$$301-391=18$$

$$401-491=18$$

$$501-591=18$$

$$601-691=18$$

$$701-780=16$$

$$18 \times 4 + 16 = 88$$

$$5 + 88 = 93$$

$$P(\text{at least one digit}) = \frac{93}{481}$$

9. a. $C(10,6) = 210$

$$C(10,6) \times \frac{6!}{4! \times 2!} = 210 \times 15 = 3150$$

b.

$$C(7,6) \times \frac{6!}{4! \times 2!} \times \frac{4!}{4!} = 105$$

$$\text{probability: } \frac{105}{3150} = \frac{1}{30}$$

10. M=message, E=email, L=letter, H=handphone

$$P(E) = 0.4$$
 $P(M|E) = 0.6$

$$P(L) = 0.1$$
 $P(M|L) = 0.8$

$$P(H) = 0.5$$
 $P(M|H) = 1$

a. $P(M) = 0.4(0.6) + 0.1(0.8) + 0.5(1) = 0.82$

b. $P(E|M) = \frac{0.4(0.6)}{0.82} = 0.293$

11. A' = cars

A = light trucks

B = Fatal accident

B' = Not a fatal accident

$$P(B|A') = \frac{20}{100000} = 0.00020$$

$$P(B|A) = \frac{25}{100000} = 0.00025$$

$$P(A) = 0.4$$

$$P(A') = 1 - 0.4 = 0.6$$

$$\begin{aligned} P(A|B) &= \frac{P(B|A)P(A)}{P(B|A)P(A) + P(B|A')P(A')} \\ &= \frac{0.00025(0.4)}{0.00025(0.4) + 0.00020(0.6)} \\ &= 0.4545 \end{aligned}$$

12. Without restrictions: $4^9 = 262144$

Disallowed way:

$$4 \times 3^9 = 78732$$

$$4 \times 2^9 = 2048$$

$$4 \times 1^9 = 4$$

$$262144 - 78732 - 2048 + 4 = 181368$$