



ASSIGNMENT 3



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UNIVERSITI TEKNOLOGI MALAYSIA

SCHOOL OF COMPUTING
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SECTION/COURSE CODE : [SECI1013] [01] – [DISCRETE STRUCTURE]

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Case Study Report submitted to School of Computing, Univerisiti Teknologi Malaysia in partial fulfilment to complete the SECI1013 Assignment for Semester 1 session 2020/2021

Question 1

a) i) $A - B = \{1, 3, 4, 6, 7, 8\}$

ii) $(A \cap B) \cup C = \{2, 5\} \cup \{a, b\}$
 $= \{2, 5, a, b\}$

iii) $A \cap B \cap C = \emptyset$

iv) $B \times C = \{2, 5, 9\} \times \{a, b\}$
 $= \{(2, a), (2, b), (5, a), (5, b), (9, a), (9, b)\}$

v) $P(C) = \{\emptyset, \{a\}, \{b\}, \{a, b\}\}$

b) $(P \wedge ((P' \vee Q')')) \vee (P \wedge Q) = (P \wedge ((P'' \wedge Q')) \vee (P \wedge Q)$
 $= (P \wedge (P \wedge Q')) \vee (P \wedge Q)$
 $= ((P \wedge P) \wedge Q') \vee (P \wedge Q)$
 $= (P \wedge Q') \vee (P \wedge Q)$
 $= P \wedge (Q' \vee Q)$
 $= P \wedge U$
 $= P$

De Morgan's law
 Double complement law
 Associative law
 Idempotent law
 Distributive law
 Complement law
 Identity law

c)

P	Q	$\neg P$	$\neg P \vee Q$	$Q \rightarrow P$	$(\neg P \vee Q) \leftrightarrow (Q \rightarrow P)$
F	F	T	T	T	T
F	T	T	T	F	F
T	F	F	F	T	F
T	T	F	T	T	T

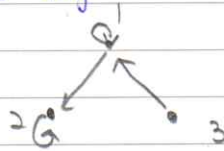
d) Let $n = 2k + 1$,
 $(n+2)^2 = (2k+1+2)^2$
 $= (2k+3)^2$
 $= 4k^2 + 12k + 9$
 $= 2(2k^2 + 6k + 4) + 1$
 $= 2r + 1$, where $r = 2k^2 + 6k + 4$
 $\therefore (n+2)^2$ is odd

e) i) $\exists x \exists y$ such that $y \leq x$, $P(x, y)$ is true, $\exists x \exists y P(x, y)$ is true
 ii) $\forall x \forall y$ such that $y \geq x$, $P(x, y)$ is false, $\forall x \forall y P(x, y)$ is false

Question 2

- a) i) domain = $\{1, 2, 3\}$
range = $\{1, 2\}$

ii) The relation is not reflexive, since it got 1's on main diagonal.
The relation is antisymmetric since all vertices have at least one directed edge and one way.



- b) i) $S = \{(4, 5), (5, 4), (5, 5)\}$

ii) S is not reflexive since

$$2 \in X, (2, 2) \notin S$$

$$3 \in X, (3, 3) \notin S$$

$$4 \in X, (4, 4) \notin S$$

S is symmetric since $(4, 5) \in S, (5, 4) \in S$

S is not transitive since $(4, 5) \in S, (5, 4) \in S$, but $(4, 4) \notin S$

S is not equivalence relation because S is not reflexive, symmetric and not transitive

- c) i) Define f by $f(x) = x$, all domain have it own range, so it is one to one function but it is not onto because 4 has no arrow pointing to it.

ii) Define g by $g(x) = x$, 1, 2 have their own range but 3 has no arrow pointing to range, hence it is not one to one function. Since all value in Z have arrow pointing to it, hence it is onto.

iii) Define h by $h(x) = x+1$, $h = \{(1, 2), (2, 3)\}$. $h(x)$ is not one to one function since 1 has no arrow pointing to range, $h(x)$ is not onto since 1 has no arrow pointing to it.

- d) i) let $y = 4x+3$

$$4x = y-3$$

$$x = \frac{y-3}{4}$$

$$m^{-1}(x) = \frac{x-3}{4}$$

- ii) $n \circ m = n(m(x))$

$$= 2(4x+3)-4$$

$$= 8x+6-4$$

$$= 8x+2$$

Question 3a) i) $a_1 = 1$

$$a_2 = 1 + 2(2)$$

$$= 5$$

$$a_3 = 5 + 2(3)$$

$$= 11$$

$\therefore$ First 3 term = 1, 5, 11

ii) $a(k)$

{

if ($k=1$)

return 1

return $a(k-1) + 2k$

}

b) let r_k = the number of executes with an input size k

$$r_1 = 7,$$

$$r_k = 2r_{(k-1)}, \quad k \geq 2$$

$$r_2 = 2(7)$$

$$= 14$$

$$r_3 = 2(2)(7)$$

$$r_k = 2^{k-1}(r_{(k-1)})$$

$$\therefore r_k = 7(2^{k-1}), \quad k \geq 2$$

c) $S(4), \quad n=4,$

$$S(4) = 675$$

 $n \neq 1,$ return $5S(3)$

$$\text{return} = 675$$

 $S(3), \quad n=3,$

$$S(3) = 175$$

 $n \neq 1,$ return $5S(2)$

$$\text{return} = 175$$

 $S(2), \quad n=2,$

$$S(2) = 25$$

 $n \neq 1,$ return $5S(1)$

$$\text{return} = 25$$

 $S(1), \quad n=1,$

$$S(1) = 5$$

return 5

$$\text{return} = 5$$

Question 4

a) 1st place, (3, 4, 5, 6, 7, 8, 9, A, B)

 $\therefore 9$ ways

4th place, (5, 6, 7, 8, 9, A, B, C, D, E, F)

 $\therefore 11$ ways

$$\underline{9} \quad \underline{16} \quad \underline{16} \quad \underline{11}$$

$$\begin{aligned} \text{ways} &= 9 \times 16 \times 16 \times 11 \\ &= 25344 \end{aligned}$$

b) first letter = 1 first digit = 10

2nd letter = 26 2nd digit = 10

3rd letter = 26 3rd digit = 1

4th letter = 26

$$\begin{aligned} \text{ways} &= 1 \times 26 \times 26 \times 26 \times 10 \times 10 \times 1 \\ &= 1757600 \end{aligned}$$

c) one word = 8

$$\begin{aligned} \text{two word} &= {}^8P_2 \\ &= 56 \end{aligned}$$

$$\begin{aligned} \text{3 word} &= {}^8P_3 \\ &= 336 \end{aligned}$$

$$\begin{aligned} \text{ways} &= 8 + 56 + 336 \\ &= 400 \end{aligned}$$

$$\begin{aligned} \text{d) women} &= {}^7C_4 \\ &= 35 \end{aligned}$$

$$\begin{aligned} \text{men} &= {}^6C_3 \\ &= 20 \end{aligned}$$

$$\begin{aligned} \text{ways} &= 35 \times 20 \\ &= 700 \end{aligned}$$

$$\begin{aligned} \text{e) ways} &= \frac{11!}{2! \times 2!} \\ &= 9979200 \end{aligned}$$

$$\begin{aligned} \text{f) } n &= 6, r = 10 \\ \text{ways} &= C(6+10-1, 10) \\ &= \frac{15!}{10! (6-1)!} \\ &= 3003 \end{aligned}$$

Question 5

a) first and last name combination = 3×2
 $= 6$

pigeons = 18

pigeonholes = 6

$$\frac{18}{6} = 3$$

$\therefore$ at least 3 persons have the same first and last name.

b) numbers = 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20

odd numbers = 1, 3, 5, 7, 9, 11, 13, 15, 17, 19

since got 10 odd number, hence even number = 10

pigeonholes = 10

pigeon $\geq n > 10$

$\therefore$ 11 integers must pick to be sure getting at least one is odd.

c) divisible by 5 = 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, 90, 95, 100

$$= 20$$

not divisible by 5 = 80

pigeonholes = 80

pigeon, $n > 80$

$\therefore$ 81 integers must pick in order to get one that is divisible by 5