



**UTM**  
UNIVERSITI TEKNOLOGI MALAYSIA

**SCHOOL OF COMPUTING**  
Faculty of Engineering

## **ASSIGNMENT 1**

### **DISCRETE STRUCTURE-07**

**GROUP-01:**

**Muhammad Aqila Karindra Daffa (A19EC3010)**

**Zhou Chenxing (A19EC4034)**

**Muhammad Najib bin Jamaludin (A20EC0215)**

Q<sub>1</sub>

a)  $A \cup C = \{x \in \mathbb{R} \mid 0 < x < 9\}$

b)  $A \cup B = \{x \in \mathbb{R} \mid 0 < x < 4\}$

$(A \cup B)' = \{x \in \mathbb{R} \mid x \leq 0, x \geq 4\}$

c)  $A' = \{x \in \mathbb{R} \mid x \leq 0, x \geq 2\}$

$B' = \{x \in \mathbb{R} \mid x < 1, x \geq 4\}$

$A' \cup B' = \{x \in \mathbb{R} \mid x < 1, x \geq 2\}$

Q<sub>2</sub>

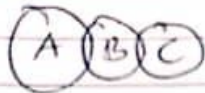
a)  $A \cap B = \emptyset, A \subseteq C, C \cap B = \emptyset$



b)  $A \subseteq B, C \subseteq B, A \cap C \neq \emptyset$



$\Rightarrow A \cap B \neq \emptyset, B \cap C \neq \emptyset, A \cap C = \emptyset, A \not\subset B, C \not\subset B$



~~Q4~~

~~Q5~~

~~$$((\neg p \wedge q) \vee (\neg p \wedge \neg q)) \vee (p \wedge q) = p$$~~

Q<sub>3</sub>

$$A = \{-1, 1, 2, 4\} \quad B = \{1, 2\}$$

1)  $A \times B$

$$= \{(-1, 1), (-1, 2), (1, 1), (1, 2), (2, 1), (2, 2), (4, 1), (4, 2)\}$$

2)  $S$

$$|X| = |Y|$$

$$= \{(-1, 1), (1, 1), (2, 2)\}$$

3)  $T$

$$x-y \text{ is even} = \{(-1, 1), (1, 1), (2, 2), (4, 2)\}$$

$$4) S \cap T = \{(-1, 1), (1, 1), (2, 2)\}$$

$$5) S \cup T = \{(-1, 1), (1, 1), (2, 2), (4, 2)\}$$

Q4) Show that  $\neg((\neg P \wedge Q) \vee (\neg P \wedge \neg Q)) \vee (P \wedge Q) \equiv P$

$$* \neg((\neg P \wedge Q) \vee (\neg P \wedge \neg Q)) \vee (P \wedge Q) \equiv P$$

$$* \neg(\neg P \wedge (Q \vee \neg Q)) \vee (P \wedge Q) \equiv P$$

$$\hookrightarrow // \text{Distributive laws: } [(P \wedge Q) \vee (P \wedge \neg Q) \equiv P \wedge (Q \vee \neg Q)]$$

$$* P \vee \neg(Q \vee \neg Q) \vee (P \wedge Q) \equiv P$$

$$\hookrightarrow // \text{De Morgan's Law: } [\neg(P \wedge Q) \equiv (\neg P) \vee (\neg Q)]$$

$$* P \vee (P \wedge Q) \equiv P$$

$$\hookrightarrow // \text{Logic \& sets: } [P \wedge \neg(Q \wedge \neg Q) \equiv P]$$

$$* P \equiv P //$$

$$\hookrightarrow // \text{Absorption Laws: } [P \vee (P \wedge Q) \equiv P]$$

$$\text{Thus, } \neg((\neg P \wedge Q) \vee (\neg P \wedge \neg Q)) \vee (P \wedge Q) \equiv P$$

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## Question 5

$$a) R_1 = \{ \cancel{x+y} (x, y) \mid x+y \leq 6 \}$$

$$X \text{ to } Y$$

$$X = \{1, 2, 3, 4, 5\}$$

$$Y = \{1, 2, 3, 4, 5\}$$

$$A_1 = \begin{array}{|ccccc|} \hline 1 & 1 & 1 & 1 & 1 \\ 1 & 1 & 1 & 1 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ \hline \end{array}$$

$$b) R_2 = \{ (y, z) \mid y > z \}$$

$$Y \text{ to } Z$$

$$Z = \{1, 2, 3, 4, 5\}$$

$$A_2 = \begin{array}{|ccccc|} \hline 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 1 & 1 & 0 & 0 & 0 \\ 1 & 1 & 1 & 0 & 0 \\ 1 & 1 & 1 & 1 & 0 \\ \hline \end{array}$$

$$c) A_1 = \text{Transitive}$$

$$d) A_2 = \text{Transitive}$$

Question 6

$$a) R_1 \cup R_2 = \begin{vmatrix} 1 & 1 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \end{vmatrix}$$

$$b) R_1 \cap R_2 = \begin{vmatrix} 0 & 0 & 0 \\ 0 & 1 & 0 \\ 1 & 0 & 1 \end{vmatrix}$$

Question 7

$f+g$  might not be one to one.

consider,

$$f(x) = x, \quad g(x) = -x$$

$$\begin{aligned} (f+g)(x) &= f(x) + g(x) \\ &= x + (-x) \\ &= 0 \end{aligned}$$

$$\begin{aligned} \text{let } (f+g)(2) &= f(2) + g(2) \\ &= 2 + (-2) \\ &= 0 \end{aligned}$$

We can see that  $(f+g)(x) = 0$ ; for all real number of  $x$ .

$\therefore f+g$  is not one to one.

Q 8)  $n =$  The stairs

$C_n =$  The number of different ways to climb the stairs

Let  $C_1 = 1$ ,  $C_2 = 2$

if  $C_n =$  The number of different ways to climb the stairs  
then:

$C_1, C_2, C_3, C_4, C_5, C_6$

1, 2, 3, 5, 8, 13

because it can be 1 stair at a time, 2 stairs at a time,  
or taking a combination of one or two stair increments.

So, Since  $C_1 - C_6 =$

$$\begin{array}{ccccccc} & & 2+1 & 3+2 & 5+3 & 8+5 & \\ & & \uparrow & \uparrow & \uparrow & \uparrow & \\ 1, & 2, & 3, & 5, & 8, & 13 & \\ \hline & 1 & 1 & 2 & 3 & 5 & \end{array}$$

$\Rightarrow C_n = C_{n-1} + C_{n-2}, n \geq 3$



Q 9) The tribonacci sequence  $(t_n)$  is defined by equation  
 $t_0 = 0, t_1 = t_2 = 1, t_n = t_{n-1} + t_{n-2} + t_{n-3}, n \geq 3$

(a)  $t_7$  ?

$$t_3 = t_2 + t_1 + t_0$$

$$= 1 + 1 + 0 = 2$$

$$t_4 = t_3 + t_2 + t_1$$

$$= 2 + 1 + 1 = 4$$

$$t_5 = t_4 + t_3 + t_2$$

$$= 4 + 2 + 1 = 7$$

$$t_6 = t_5 + t_4 + t_3$$

$$= 7 + 4 + 2 = 13$$

$$t_7 = t_6 + t_5 + t_4$$

$$= 13 + 7 + 4 = \underline{\underline{20}}$$

(b)

\* Input =  $n$

\* Output =  $t_n$

\*  $t(n)$  {

if  $(n = 0)$  {

return 0

return  $t(n) = t(n-1) + t(n-2) + t(n-3)$  }

\* if  $(n = 1 \text{ and } n = 2)$  {

return 1

return  $t(n) = t(n-1) + t(n-2) + t(n-3)$  }}