



UTM BACHELOR OF COMPUTING SCIENCE (DATA ENGINEERING) COMPUTING PROGRAMME

DATA STRUCTURE AND ALGORITHM

(SECJ2013-02)

ASSIGNMENT 4

ALGORITHMS EFFICIENCY

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SIGNATURE AND SCORE =

Question 2

a)

Statements	Number of steps
For (i=2 ; i<n;i++)	$n-2+1+1$ $=n-2$
Cout << l;	$1.(n-2)$ $=n-2$
For (j=1;j<=n;j=j*2)	$1+\log_2 n$
Cout << j;	$1.(1+\log_2 n)$ $=1+\log_2 n$
Total execution	$2(n-2)+2(1 + \log_2 n)$
Time complexity	$O(\log_2 n)$

b)

Statements	Number of steps
Int i=1	1
While (i<=n)	n-1+1 =n
{ for (j=1;j<=i;j++)	n =n
Cout << i ;	n.(n) = n^n
Cout << j;	1.(n^n) = n^n
i++ ; }	1.(n) =n
Total execution	$1+2n+n^n$
Time complexity	$O(n^n)$

c)

Statements	Number of steps
Int i	1
J=1	1
For (i=1;i<=n;i++) {	n-1+1 =n
J=j*2; }	$n.\log_2 n$ = $n\log_2 n$
For (i=1;i<=j;i++) {	2^n
Cout << j << "\n";	1.(2^n) = 2^n
Total execution	$2+n+n\log_2 n+2(2^n)$
Time complexity	$O(2^n)$

d)

Statements	Number of steps
For (a=3;i<=n;a++)	$n-3+1$ $=n-2$
For (b=1;b<n;b++)	$(n-2).n$ $=n^2-2n$
Cout << a;	$1.(n^2-2n)$ $=n^2-2n$
Total execution	$n-2+2(n^2-2n)$
Time complexity	$O(n^2)$

Question 3

Code Segment

```
for(int i = 1; i <= 5; ++i)
{
    for(int j = 1; j <= i; ++j)
    {
        cout << "# ";
    }
    cout << "\n";
}
```

Statements	Number of steps
for(int i = 1; i <= 5; ++i){	$n-1+1$ $=n$
for(int j = 1; j <= i; ++j)	$n.n$ $=n^2$
cout << "# "; }	$1. n^2$ $=n^2$
cout << "\n";	$1.n$ $=n$
Total execution	$2n + 2(n^2)$
Time complexity	$O(n^2)$

Question 4

STATEMENT	Number of Steps
Int i=0	1
For (i=4 ;i<=n;i=i*4)	$1+\log_4 n$
Cout << "Current I value is " << I << endl;	$1.(1 + \log_4 n)$ $=(1 + \log_4 n)$
Cout << "Current n value is " << I << endl;	=1
Total steps	$2 + 2(1 + \log_4 n)$
Algorithm complexity	$O(\log_2 n)$

Calculation

$$\log_4 n = \frac{\log_2 n}{\log_2 4}$$

$$=\log_2 n / 2$$

$$=O(\log_2 n)$$

Question 5

STATEMENT	Number of Steps
For (i=4;i<n;i++)	$n-4-1+1$ $=n-4$
Cout << l;	$1.(n-4)$ $= n-4$
For (j=1;j<=n;j=j*2) {	$1+(\log_2 n)$
Cout << j;	$1.(1+(\log_2 n))$ $=1+(\log_2 n)$
For (k=1;k<=n;k++)	$(n-1+1).(1+(\log_2 n))$ $=n.(1+\log_2 n)$
Cout << k }	$1. ((n-1+1).(1+(\log_2 n)))$ $1.n.(1+\log_2 n)$ $= n.(1+\log_2 n)$
Total steps	$2(n-4)+2(\log_2 n)+2(n \log_2 n)$
Algorithm complexity	$O(n \log_2 n)$

Question 6

a)

Value of l	Number of steps for in the internal loop For (j=1;j<=l;j++)
1	1= 1 time
2	1,2 = times
3	1,2,3= 3 times
:	:
n-1	1,2,3,...n-2,n-1=n-1 times
n	1,2,3,...n-1,n=n+1 times

B) Total steps = $1+n+(n(n+1)/2)+(n+1)/2+n$

$$=1+n+\frac{n^2+n+n^2+n}{2}+n$$

$$=1+n+n^2+n+n$$

$$=1+3n+n^2$$

c) Big O notation = $O(n^2)$

d) Bubble sort has big O notation of $O(n^2)$

Question 7

Statement	Number of steps
for (j=1;j<=l;j=j*2)	$\log_2 n$
Cout << "EXCELLENT!";	$1.(\log_2 n)$
for (i=4;i<=n;i++)	$n - 4 + 1$ $=n-3$
Cout << "GREAT!!!";	$1.(n-3)$ $=n-3$
for (k=1;k<=n;k++)	$(n-1+1)$ $=n$
Cout << "*****";	$n.1$ $=n$
Total steps	$2\log_2 n + n - 3 + n - 3 + 2n$ $=2\log_2 n + 4n - 6$
Algorithm complexity	$O(\log_2 n)$

Question 8

i)

Value of I	Number of steps for in the internal loop For (j=1;j<=I;j++)
N	n time
n-1	n-1 time
:	:
3	3 times
2	2 times
1	1 time

li) Total steps

$$=n + 1 + (n(n-1)/2) + (n(n-1)/2) + n$$

$$=1+2n + \frac{n^2 - n + n^2 - n}{2}$$

$$=1+2n + \frac{2n^2 - 2n}{2}$$

$$=1+2n+n^2-n$$

$$=1+n+n^2$$

iii) Big O notation = $O(n^2)$