

PROJECT 2  
PROBABILITY AND STATISTICAL DATA ANALYSIS  
SECI / SCS1 2143



**UTM**  
UNIVERSITI TEKNOLOGI MALAYSIA

**Title:**

**USA House Sales Price & How other factors  
affect its Variation**

**Name:** Lee Sze Yuan

**Subject:** Probability & Statistical Data Analysis

**Section:** 02

**Lecturer:** Dr. Chan Weng Howe

**Date:** 28/06/2020 (Sunday)

# Table of Contents

|  |    |
|--|----|
| 1.0 Introduction.....  | 3  |
| 1.1 Dataset.....   | 3  |
| 1.2 Aim of Study .....   | 4  |
| 2.0 Hypothesis Testing.....                                    | 5  |
| Commonly Used Value .....                                      | 5  |
| 2.1 1 Sample Hypothesis testing .....                          | 5  |
| 2.2 Correlation.....   | 7  |
| 2.3 Regression .....   | 9  |
| 2.4 Chi Square test of independence .....                      | 12 |
| 2.5 2 Two Means, independent samples, unknown $\sigma^2$ ..... | 13 |
| 3.0 Discussion .....   | 14 |
| 4.0 Conclusion .....   | 18 |
| 5.0 References.....  | 19 |

# 1.0 Introduction

## 1.1 Dataset

For this project 2, we have visited a few websites and go through a few datasets which is suitable for this project. Since project 2 require us to conduct lots of hypothesis tests like linear regression, correlation etc. So, we look for dataset which have many numerical variables. These are the 2 datasets I found on Kaggle (<https://www.kaggle.com/>) and plan to use.

|    | A        | B        | C        | D        | E        | F           | G        | H      | I          | J    | K         | L     | M          | N          | O        | P          | Q       | R       | S        | T           | U          |
|----|----------|----------|----------|----------|----------|-------------|----------|--------|------------|------|-----------|-------|------------|------------|----------|------------|---------|---------|----------|-------------|------------|
| 1  | id       | date     | price    | bedrooms | bathroom | sqft_living | sqft_lot | floors | waterfront | view | condition | grade | sqft_abovs | sqft_baser | yr_built | yr_renovat | zipcode | lat     | long     | sqft_living | sqft_lot15 |
| 2  | 7.13E+09 | 20141013 | 221900   | 3        | 1        | 1180        | 5650     | 1      | 0          | 0    | 3         | 7     | 1180       | 0          | 1955     | 0          | 98178   | 47.5112 | -122.257 | 1340        | 5650       |
| 3  | 6.41E+09 | 20141209 | 538000   | 3        | 2.25     | 2570        | 7242     | 2      | 0          | 0    | 3         | 7     | 2170       | 400        | 1951     | 1991       | 98125   | 47.721  | -122.319 | 1690        | 7639       |
| 4  | 5.63E+09 | 20150225 | 180000   | 2        | 1        | 770         | 10000    | 1      | 0          | 0    | 3         | 6     | 770        | 0          | 1933     | 0          | 98028   | 47.7379 | -122.233 | 2720        | 8062       |
| 5  | 2.49E+09 | 20141209 | 604000   | 4        | 3        | 1960        | 5000     | 1      | 0          | 0    | 5         | 7     | 1050       | 910        | 1965     | 0          | 98136   | 47.5208 | -122.393 | 1360        | 5000       |
| 6  | 1.95E+09 | 20150218 | 510000   | 3        | 2        | 1680        | 8080     | 1      | 0          | 0    | 3         | 8     | 1680       | 0          | 1987     | 0          | 98074   | 47.6168 | -122.045 | 1800        | 7503       |
| 7  | 7.24E+09 | 20140512 | 1.23E+06 | 4        | 4.5      | 5420        | 101930   | 1      | 0          | 0    | 3         | 11    | 3890       | 1530       | 2001     | 0          | 98053   | 47.6561 | -122.005 | 4760        | 101930     |
| 8  | 1.32E+09 | 20140627 | 257500   | 3        | 2.25     | 1715        | 6819     | 2      | 0          | 0    | 3         | 7     | 1715       | 0          | 1995     | 0          | 98003   | 47.3097 | -122.327 | 2238        | 6819       |
| 9  | 2.01E+09 | 20150115 | 291850   | 3        | 1.5      | 1060        | 9711     | 1      | 0          | 0    | 3         | 7     | 1060       | 0          | 1963     | 0          | 98198   | 47.4095 | -122.315 | 1650        | 9711       |
| 10 | 2.41E+09 | 20150415 | 229500   | 3        | 1        | 1780        | 7470     | 1      | 0          | 0    | 3         | 7     | 1050       | 730        | 1960     | 0          | 98146   | 47.5123 | -122.337 | 1780        | 8113       |
| 11 | 3.79E+09 | 20150312 | 323000   | 3        | 2.5      | 1890        | 6560     | 2      | 0          | 0    | 3         | 7     | 1890       | 0          | 2003     | 0          | 98038   | 47.3684 | -122.031 | 2390        | 7570       |
| 12 | 1.74E+09 | 20150403 | 662500   | 3        | 2.5      | 3560        | 9796     | 1      | 0          | 0    | 3         | 8     | 1860       | 1700       | 1965     | 0          | 98007   | 47.6007 | -122.145 | 2210        | 8925       |
| 13 | 9.21E+09 | 20140527 | 468000   | 2        | 1        | 1160        | 6000     | 1      | 0          | 0    | 4         | 7     | 860        | 300        | 1942     | 0          | 98115   | 47.69   | -122.292 | 1330        | 6000       |
| 14 | 1.14E+08 | 20140528 | 310000   | 3        | 1        | 1430        | 19901    | 1.5    | 0          | 0    | 4         | 7     | 1430       | 0          | 1927     | 0          | 98028   | 47.7558 | -122.229 | 1780        | 12697      |
| 15 | 6.05E+09 | 20141007 | 400000   | 3        | 1.75     | 1370        | 9680     | 1      | 0          | 0    | 4         | 7     | 1370       | 0          | 1977     | 0          | 98074   | 47.6127 | -122.045 | 1370        | 10208      |
| 16 | 1.18E+09 | 20150312 | 530000   | 5        | 2        | 1810        | 4850     | 1.5    | 0          | 0    | 3         | 7     | 1810       | 0          | 1900     | 0          | 98107   | 47.67   | -122.394 | 1360        | 4850       |
| 17 | 9.3E+09  | 20150124 | 650000   | 4        | 3        | 2950        | 5000     | 2      | 0          | 3    | 3         | 9     | 1980       | 970        | 1979     | 0          | 98126   | 47.5714 | -122.375 | 2140        | 4000       |
| 18 | 1.88E+09 | 20140731 | 395000   | 3        | 2        | 1890        | 14040    | 2      | 0          | 0    | 3         | 7     | 1890       | 0          | 1994     | 0          | 98019   | 47.7277 | -121.962 | 1890        | 14018      |
| 19 | 6.87E+09 | 20140529 | 485000   | 4        | 1        | 1600        | 4300     | 1.5    | 0          | 0    | 4         | 7     | 1600       | 0          | 1916     | 0          | 98103   | 47.6648 | -122.343 | 1610        | 4300       |
| 20 | 16000397 | 20141205 | 189000   | 2        | 1        | 1200        | 9850     | 1      | 0          | 0    | 4         | 7     | 1200       | 0          | 1921     | 0          | 98002   | 47.3089 | -122.21  | 1060        | 5095       |
| 21 | 7.98E+09 | 20150424 | 230000   | 3        | 1        | 1250        | 9774     | 1      | 0          | 0    | 4         | 7     | 1250       | 0          | 1969     | 0          | 98003   | 47.3343 | -122.306 | 1280        | 8850       |
| 22 | 6.3E+09  | 20140514 | 385000   | 4        | 1.75     | 1620        | 4980     | 1      | 0          | 0    | 4         | 7     | 860        | 760        | 1947     | 0          | 98133   | 47.7025 | -122.341 | 1400        | 4980       |
| 23 | 2.52E+09 | 20140826 | 2.00E+06 | 3        | 2.75     | 3050        | 44867    | 1      | 0          | 4    | 3         | 9     | 2330       | 720        | 1968     | 0          | 98040   | 47.5316 | -122.233 | 4110        | 20336      |
| 24 | 7.14E+09 | 20140703 | 285000   | 5        | 2.5      | 2270        | 6300     | 2      | 0          | 0    | 3         | 8     | 2270       | 0          | 1995     | 0          | 98092   | 47.3266 | -122.169 | 2240        | 7005       |
| 25 | 8.09E+09 | 20140516 | 252700   | 2        | 1.5      | 1070        | 9643     | 1      | 0          | 0    | 3         | 7     | 1070       | 0          | 1985     | 0          | 98030   | 47.3533 | -122.166 | 1220        | 8386       |
| 26 | 3.81E+09 | 20141120 | 329000   | 3        | 2.25     | 2450        | 6500     | 2      | 0          | 0    | 4         | 8     | 2450       | 0          | 1985     | 0          | 98030   | 47.3739 | -122.172 | 2200        | 6865       |
| 27 | 1.2E+09  | 20141103 | 233000   | 3        | 2        | 1710        | 4697     | 1.5    | 0          | 0    | 5         | 6     | 1710       | 0          | 1941     | 0          | 98002   | 47.3048 | -122.218 | 1030        | 4705       |
| 28 | 1.29E+09 | 20140626 | 927000   | 3        | 1.75     | 2450        | 2681     | 2      | 0          | 0    | 3         | 8     | 1750       | 700        | 1915     | 0          | 98110   | 47.6386 | -122.36  | 1760        | 3573       |

Figure 1.0: USA House Sales Price

The first dataset here is USA house Sales Price. This dataset contains the house sale prices for the County, USA. It includes homes sold in USA during the time between May 2014 and May 2015. This dataset is definitely great to conduct linear regression and correlation test. We will use this dataset as my main dataset and perform most of the data analysis and hypothesis testing on the data of this dataset.

Link: <https://www.kaggle.com/harlfoxem/housesalesprediction>

|    | A         | B        | C                  | D           | E              | F          | G          | H             | I                  | J               |          |
|----|-----------|----------|--------------------|-------------|----------------|------------|------------|---------------|--------------------|-----------------|----------|
| 1  | longitude | latitude | housing_median_age | total_rooms | total_bedrooms | population | households | median_income | median_house_value | ocean_proximity |          |
| 2  | -122.23   | 37.88    |                    | 41          | 880            | 129        | 322        | 8.3252        | 452600             | NEAR BAY        |          |
| 3  | -122.22   | 37.86    |                    | 21          | 7099           | 1106       | 2401       | 1138          | 8.3014             | 358500          | NEAR BAY |
| 4  | -122.24   | 37.85    |                    | 52          | 1467           | 190        | 496        | 177           | 7.2574             | 352100          | NEAR BAY |
| 5  | -122.25   | 37.85    |                    | 52          | 1274           | 235        | 558        | 219           | 5.6431             | 341300          | NEAR BAY |
| 6  | -122.25   | 37.85    |                    | 52          | 1627           | 280        | 565        | 259           | 3.8462             | 342200          | NEAR BAY |
| 7  | -122.25   | 37.85    |                    | 52          | 919            | 213        | 413        | 193           | 4.0368             | 269700          | NEAR BAY |
| 8  | -122.25   | 37.84    |                    | 52          | 2535           | 489        | 1094       | 514           | 3.6591             | 299200          | NEAR BAY |
| 9  | -122.25   | 37.84    |                    | 52          | 3104           | 687        | 1157       | 647           | 3.12               | 241400          | NEAR BAY |
| 10 | -122.26   | 37.84    |                    | 42          | 2555           | 665        | 1206       | 595           | 2.0804             | 226700          | NEAR BAY |
| 11 | -122.25   | 37.84    |                    | 52          | 3549           | 707        | 1551       | 714           | 3.6912             | 261100          | NEAR BAY |
| 12 | -122.26   | 37.85    |                    | 52          | 2202           | 434        | 910        | 402           | 3.2031             | 281500          | NEAR BAY |
| 13 | -122.26   | 37.85    |                    | 52          | 3503           | 752        | 1504       | 734           | 3.2705             | 241800          | NEAR BAY |
| 14 | -122.26   | 37.85    |                    | 52          | 2491           | 474        | 1098       | 468           | 3.075              | 213500          | NEAR BAY |
| 15 | -122.26   | 37.84    |                    | 52          | 696            | 191        | 345        | 174           | 2.6736             | 191300          | NEAR BAY |
| 16 | -122.26   | 37.85    |                    | 52          | 2643           | 626        | 1212       | 620           | 1.9167             | 159200          | NEAR BAY |
| 17 | -122.26   | 37.85    |                    | 50          | 1120           | 283        | 697        | 264           | 2.125              | 140000          | NEAR BAY |
| 18 | -122.27   | 37.85    |                    | 52          | 1966           | 347        | 793        | 331           | 2.775              | 152500          | NEAR BAY |
| 19 | -122.27   | 37.85    |                    | 52          | 1228           | 293        | 648        | 303           | 2.1202             | 155500          | NEAR BAY |
| 20 | -122.26   | 37.84    |                    | 50          | 2239           | 455        | 990        | 419           | 1.9911             | 158700          | NEAR BAY |
| 21 | -122.27   | 37.84    |                    | 52          | 1503           | 298        | 690        | 275           | 2.6033             | 162900          | NEAR BAY |
| 22 | -122.27   | 37.85    |                    | 40          | 751            | 184        | 409        | 166           | 1.3578             | 147500          | NEAR BAY |
| 23 | -122.27   | 37.85    |                    | 42          | 1639           | 367        | 929        | 366           | 1.7135             | 159800          | NEAR BAY |
| 24 | -122.27   | 37.84    |                    | 52          | 2436           | 541        | 1015       | 478           | 1.725              | 113900          | NEAR BAY |
| 25 | -122.27   | 37.84    |                    | 52          | 1688           | 337        | 853        | 325           | 2.1806             | 99700           | NEAR BAY |
| 26 | -122.27   | 37.84    |                    | 52          | 2224           | 437        | 1006       | 422           | 2.6                | 132600          | NEAR BAY |
| 27 | -122.28   | 37.85    |                    | 41          | 535            | 123        | 317        | 119           | 2.4038             | 107500          | NEAR BAY |
| 28 | -122.28   | 37.85    |                    | 40          | 1130           | 244        | 607        | 230           | 2.6507             | 93800           | NEAR BAY |

## Figure 2.0: California Housing Price

Then, the second dataset here, we have this dataset “California Housing Price”. Based on the description given on Kaggle. This is a dataset used in the second chapter of Aurélien Géron's recent book 'Hands-On Machine learning with Scikit-Learn and TensorFlow'. The author of this book used this dataset to show how to perform various data analysis and also implementing machine learning algorithm. This dataset contains information from the 1990 California census. We will use this dataset as my second dataset. So that we can perform data analysis and hypothesis tests which require 2 samples together with the first dataset.

Link: <https://www.kaggle.com/camnugent/california-housing-prices>

### 1.2 Aim of Study

The purpose of this study is to study the house sales price in USA and California. This study wishes to find out the trend of the house sale price in USA and to see how house sales price are affected by other factors like total square feet, number of bedrooms etc. Then, if possible, to see how the house sales price has changed over time when compared to the house sales price in USA nowadays. Below is a list of purposes we have summarised for this study

- First, this study hopes to find out whether the claim of actual population parameter of USA houses sales prices can be rejected or should not be rejected. Or to
- Tests whether there is a change in the population parameters or not. These questions or hypothesis will be tested out by using the sample statistic of USA houses sales prices in between May 2014 and May 2015.
- Besides, this study also aims to observe and study the relationships between house sales price value and other variables. Example of variables include number of floors, number of bedrooms, number of bedrooms etc.
- This study aims to find out how each variable affect each other. Lastly, this study will also focus in studying whether there is difference in house sales price when the houses have different characteristics.

The target population we will use in this study is the Prices of house sales in USA and California.

## 2.0 Hypothesis Testing

### Commonly Used Value

| No | Dataset    | $\bar{x}$ | S        | $\mu$  | N     |
|----|------------|-----------|----------|--------|-------|
| 1  | USA        | 54008.1   | 367127.2 | 385000 | 21613 |
| 2  | California | 206855.1  | 115395.8 | -      | 20604 |

### 2.1 1 Sample Hypothesis testing

#### 2.1.1

To test whether the sample mean has any different from the claim of population mean

$$H_0: u = 385000$$

$$H_1 : u \neq 385000$$

$$\alpha = 0.05$$

$$Z = \frac{\bar{x} - u}{s / \sqrt{n}} = 62.104$$

$$c. v. z_{0.05} = 1.960$$

$$p(z > 62.104) = 0$$

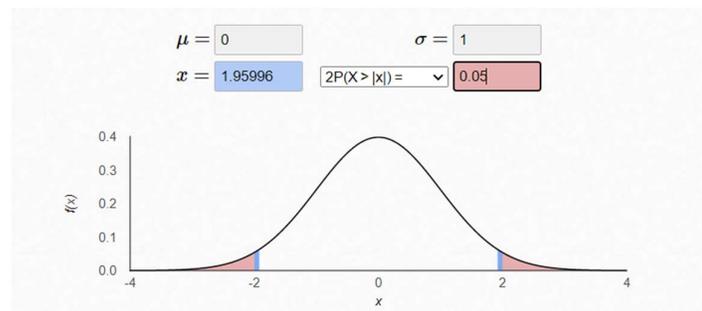


Figure 3.0 Critical Region

**Analysis:** Since statistic value = 62.104 > 1.960 and P-value is less than 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that population mean of house sales price is not equal to 385000.

## 2.1.2

To test whether the sample variance has any different from the claim of population variance

$$H_0: \sigma = 400000$$

$$H_1: \sigma < 400000$$

$$\alpha = 0.05$$

$$df = n-1 = 21612$$

$$\chi^2 = \frac{(n-1)s^2}{\sigma^2} = 18205.73$$

$$c. v. \chi^2_{0.05, n-1} = 21955.1$$

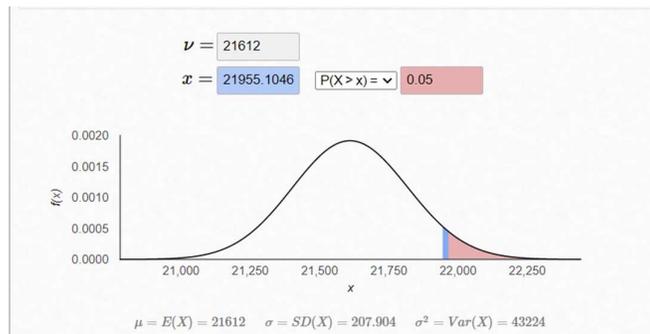


Figure 4.0 Critical Region

**Analysis:** Since statistic value = 18205.73 < 21955.1. We do not reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is insufficient evidence that population variance of house sales price is less than 400000.

## 2.2 Correlation

### 2.2.1

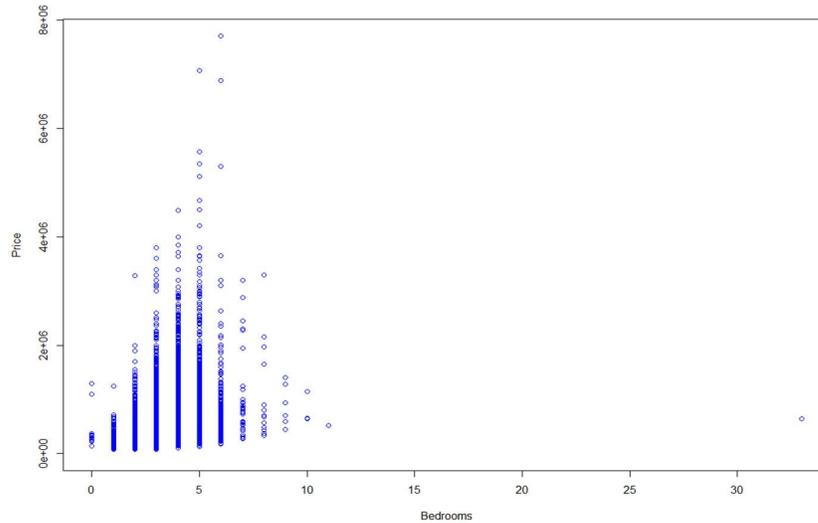
To measure strength of the linear relationship between price and number of bedrooms

X: No of Bedrooms

Y: House Sales Price

$$H_0: \rho = 0$$

$$H_1: \rho \neq 0$$



$$r = 0.3083496$$
$$\alpha = 0.05$$
$$df = n-2 = 21611$$

Figure 5.0: Correlation of No of Bedrooms VS House Sales Price

$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}} = 47.65139$$

$$P\text{-value} = 0$$

$$c. v. t_{df, -\alpha/2} = -1.960$$

$$c. v. t_{df, \alpha/2} = 1.960$$

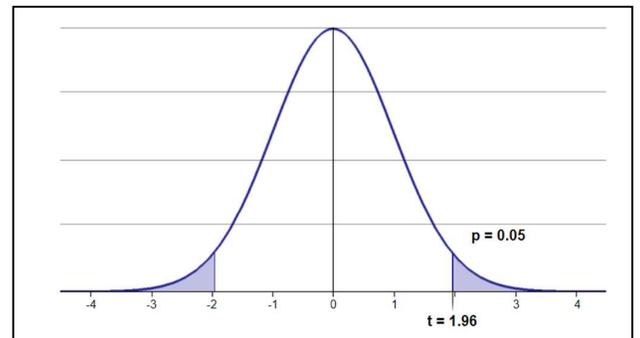


Figure 6.0: Critical Region

**Analysis:** Since statistic value = 47.65139 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence of a linear relationship between No of Bedrooms and House Sales Price

### 2.2.2

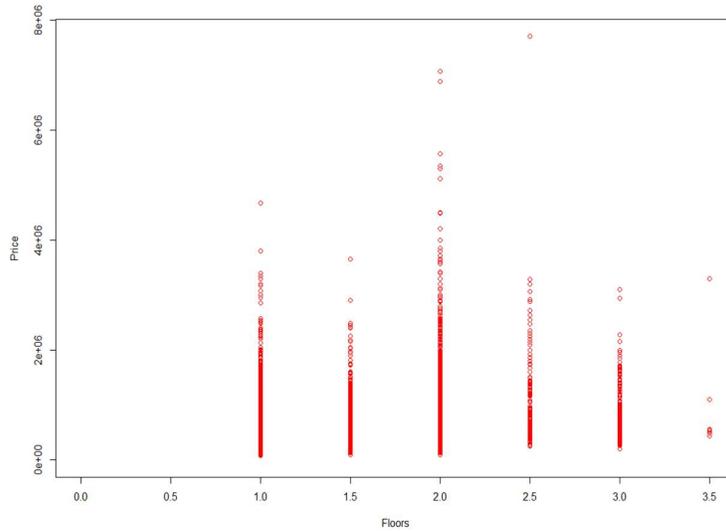
To measure strength of the linear relationship between price and number of floors

X: No of Floors

Y: House Sales Price

$$H_0: \rho = 0$$

$$H_1: \rho \neq 0$$



$r = 0.2567939$   
 $\alpha = 0.05$   
 $df = n-2 = 21611$

Figure 7.0: Correlation of No of Floors VS House Sales Price

$$t = \frac{r}{\sqrt{\frac{1-r^2}{n-2}}} = 39.06029$$

$$P\text{-value} = 1.58101e-322$$

$$c. v. t_{df, -\alpha/2} = -1.960$$

$$c. v. t_{df, \alpha/2} = 1.960$$

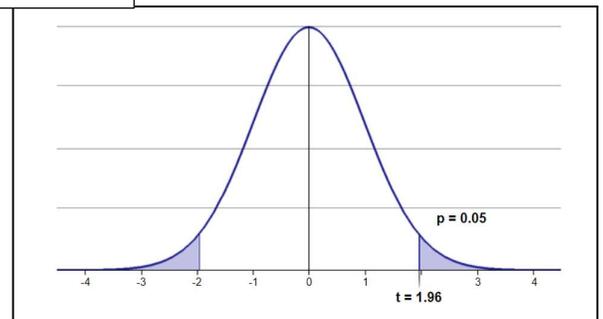


Figure 8.0: Critical Region

**Analysis:** Since statistic value = 39.06029 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence of a linear relationship between No of Floors and House Sales Price

## 2.3 Regression

### 2.3.1

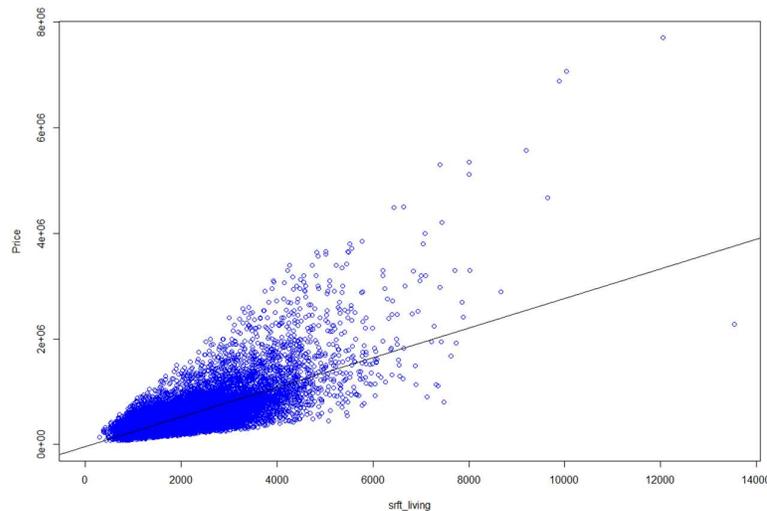
To predict the value of house price based on the value of sqft\_living

Dependent: House Sales Price

Independent: sqft\_living

$$H_0: \beta_1 = 0$$

$$H_1: \beta_1 \neq 0$$



$$\hat{y} = -43580.7 + 280.6x$$

$$b_0 = -43580.7$$

$$b_1 = 280.6$$

$$R^2 = 0.4928532$$

$$\alpha = 0.05$$

$$df = n-2 = 21611$$

Figure 9.0: Regression of sqft\_living VS House Sales Price

$$S_{b_1} = 1.936$$

$$t = \frac{b_1 - \beta_1}{S_{b_1}} = 144.920$$

$$P\text{-value} = 0$$

$$c. v. t_{df, -\alpha/2} = -1.960$$

$$c. v. t_{df, \alpha/2} = 1.960$$

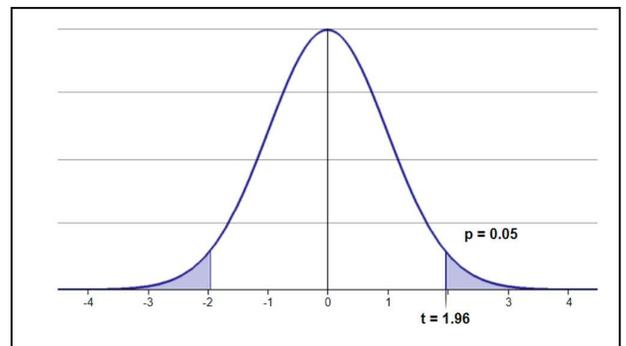


Figure 10.0: Critical Region

**Analysis:** Since statistic value = 144.920 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that the variable, sqft\_living affects House Sales Price.

### 2.3.2

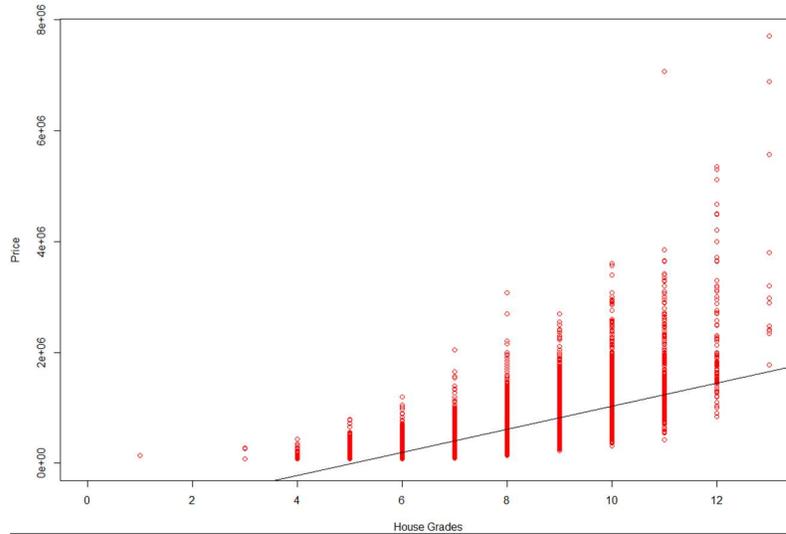
To predict the value of house price based on the value of house grade

Dependent: House Sales Price

Independent: House Grade

$$H_0: \beta_1 = 0$$

$$H_1: \beta_1 \neq 0$$



$$\hat{y} = -1056045 + 208458x$$

$$b_0 = -1056045$$

$$b_1 = 208458$$

$$R^2 = 0.4454685$$

$$\alpha = 0.05$$

$$df = n - 2 = 21611$$

Figure 11.0: Regression of House Grade VS House Sales Price

$$S_{b_1} = 1582$$

$$t = \frac{b_1 - \beta_1}{S_{b_1}} = 131.76$$

$$P\text{-value} = 0$$

$$c. v. t_{df, -\alpha/2} = -1.960$$

$$c. v. t_{df, \alpha/2} = 1.960$$

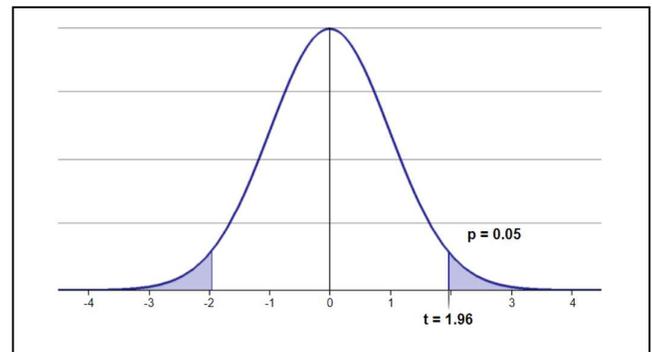


Figure 12.0: Critical Region

**Analysis:** Since statistic value = 131.76 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that the variable, House Grade affects House Sales Price.

### 2.3.3

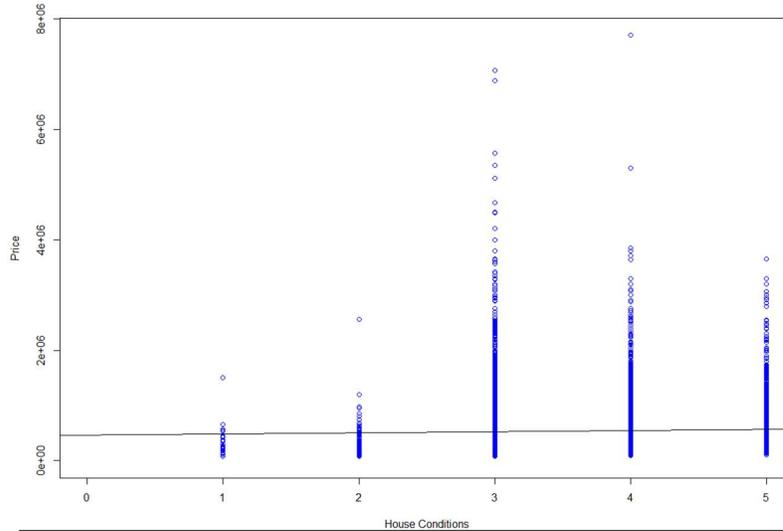
To predict the value of house price based on the house condition ratings

Dependent: House Sales Price

Independent: House Condition

$$H_0: \beta_1 = 0$$

$$H_1: \beta_1 \neq 0$$



$$\hat{y} = 470147 + 20514x$$

$$b_0 = 470147$$

$$b_1 = 20514$$

$$R^2 = 0.00132218$$

$$\alpha = 0.05$$

$$df = n-2 = 21611$$

Figure 13.0: Regression of House Condition VS House Sales

$$S_{b_1} = 3835$$

$$t = \frac{b_1 - \beta_1}{S_{b_1}} = 5.349$$

$$P\text{-value} = 0$$

$$c. v. t_{df, -\alpha/2} = -1.960$$

$$c. v. t_{df, \alpha/2} = 1.960$$

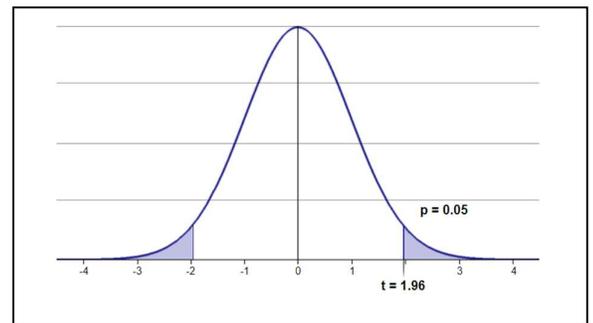


Figure 14.0: Critical Region

**Analysis:** Since statistic value = 5.349 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that the variable, House Condition affects House Sales Price.

## 2.4 Chi Square test of independence

### 2.4.1

To test whether grade and condition is independent or not

$H_0$ : Grade is independent of the condition

$H_1$ : Grade is dependent of the condition

$$\alpha = 0.05$$

$$df = (R-1)(C-1) = 44$$

$$\chi^2 = \sum \frac{(O-E)^2}{E} = 2225.6$$

$$P\text{-value} = 0$$

$$\chi^2_{df,\alpha} = 60.481$$

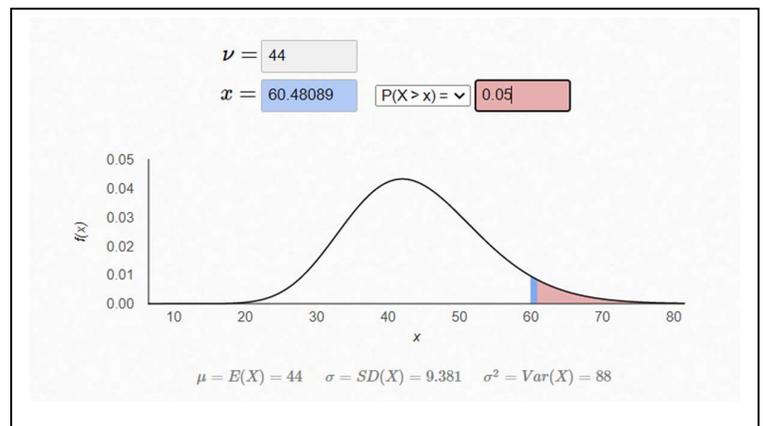


Figure 15.0: Critical Region

**Analysis:** Since statistic value = 2225.6 > 60.481 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that the variable, House Grade is independent of the variable, House Condition

## 2.5 2 Two Means, independent samples, unknown $\sigma^2$

### 2.5.1

To test whether USA has same population of House Sales Price as California

$H_0$ :  $\mu_1$  of House Sales Price in USA =  $\mu_2$  of House Sales Price in California

$H_1$ :  $\mu_1$  of House Sales Price in USA  $\neq$   $\mu_2$  of House Sales Price in California

$$\alpha = 0.05$$

$$t_0 = \frac{\bar{x}_1 - \bar{x}_2 - 0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}} = 127.0313$$

$$v = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\frac{\left(\frac{s_1^2}{n_1}\right)^2}{n_1 - 1} + \frac{\left(\frac{s_2^2}{n_2}\right)^2}{n_2 - 1}} = 26023.39$$

$$P\text{-value} = 0$$

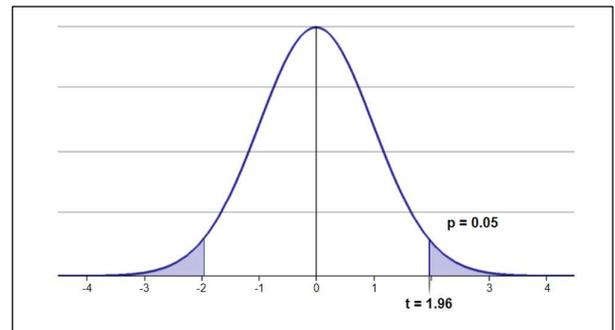


Figure 16.0: Critical Region

$$c. v. t_{df, -\alpha/2} = -1.960 \quad c. v. t_{df, \alpha/2} = 1.960$$

**Analysis:** Since statistic value = 127.0313 > 1.960 and P-value < 0.05. We reject  $H_0$  at a significance level of 0.05

**Conclusion:** There is sufficient evidence that the mean of House Sales Price in USA is not equal to mean of House Sales Price in California

## 3.0 Discussion

The focus of my study and analysis is to study the house sales price in USA. My study aims to study the house sales price data found on Kaggle and to see in what way, different factors affect the house sales price. After conducting several hypothesis tests, there are several findings to be discussed.

### (A) Is House Sale Price in USA really as low as 385000?

To validate this claim from the **statista** website ([link](#)), I decide to run a 1-Sample Hypothesis testing on the mean of the house sales price in the dataset. For this test, the null hypothesis here will be 385000 and we want to find out whether this hypothesis should be accepted or should be rejected in a significance level of 0.05.

Then, throughout the process of Hypothesis testing, firstly, I found that the sample house sales price mean of the dataset is 540088.1 which deviates a lot from the claim by the website. Then, after further calculation, I obtain a result that showing the House Sales Price in USA has changed significantly over these few years because I obtain a P-value of roughly 0 (can't be calculated by RStudio). This result led to a conclusion that we should reject null hypothesis. There is insufficient evidence that the House Sales Price is equal to 38500. The house sales price in USA is much higher than the claim which mean the house sales price was more expensive back in the time.

### (B) Is the deviation of house sale price in USA very big?

First, I claim that the house sale price in USA has a population standard deviation of 400000 based on the sample standard deviation of 367127.2 that I calculated in 1<sup>st</sup> test. Again, I decide to run a 1-sample Chi-square on the Hypothesis of the standard deviation at a significance level of 0.05. The critical value for this test is 21955.1

After calculation, I get a test statistic of 18205.73. So, as we can see, the test statistic is smaller than 21955.1 by around 10000. So, I can conclude that the null hypothesis on the population standard deviation is 400000 should not be rejected. The house sales price has this deviation.

### (C) Is number of floors or bedrooms related to the house sales price?

As we commonly knew, the total square feet of a house is related to the house price in a linear proportional relationship. Because higher square feet mean more usable space and there will be more rooms for some purposes like study room, entertainment room, garage etc. (Gomez, 2019) But what wonders me next is will the number of rooms or floors related to the house sales price in the same way as total square feet do. The reason I have this question is because with more rooms, people can create different rooms of different purposes. Then, with more floors, the usable space also increases.

So, I decide a do a correlation analysis on No of Bedrooms VS Price and No of Floors VS Price. This is to check whether there is relationship between these 2 variables and the House Sales Price.

The independent variables will be No of Bedrooms and No of Floors and dependent variables will be Price.

As what was shown on the last section 2.0, I managed to get the Sample Correlation Coefficient,  $r$  for both  $(x, y)$  pairs. For the first  $(x, y)$  pair: No of Bedrooms VS Price. The  $r$  value is only 0.3083496. And for the second  $(x, y)$  pair: No of Floors VS Price. The  $r$  value is 0.2567939. The  $r$  value for each  $(x, y)$  pair indicates that the linear relationship between independent variable,  $x$  and dependent variable,  $y$  is POSTIVE but WEAK. But before I make a conclusion that there is a correlation exists between each  $(x, y)$  pairs.

I have done significance test for correlation on each  $(x, y)$  pair at a significance level of 0.05 and degree of freedom of 21611. Then, the  $t$ -value test statistic for both test (1<sup>st</sup> Pair: 47.65139, 2<sup>nd</sup> Pair: 39.06029) has exceeded the critical value 1.960 a lot. This indicates that there is correlation exists in both pair, but the relationship is just a weak positive relationship.

The possible reason behind this result is there could be some house that have more rooms or floors, but the total square feet is still small. So, people less prefer this kind of house and they still prefer house with bigger total square feet even if there is less rooms or floors

**(D) Can we predict the house sales price based on the sqft\_living, grade and house conditions to predict the house sales price?**

After I finished in studying the relationship between No of Bedrooms and Price and the relationship between No of Floors and Price. I want to see whether can we predict the house sales price based on the sqft\_living, grade and house. Can sqft\_living, grade and condition helps people to predict the house price easily.

So, I will do a fit a linear regression model to predict the house sales price based on these 3 variables. These 3 variables are sqft\_living, grades and conditions. My expectation for these tests is that great portion of the total variation in the house sales price is explained by variation in the sqft\_living, grade and house conditions.

After I execute the analysis on R Studio to try to find the coefficient of determination value,  $R^2$ , I get quite a different result from my expectation. Only 49.29% and 44.54% of the variation of house sales price can be explained by sqft\_living and grade respectively. However, for house condition, this independent variable can only explain less than 1% of the variation of house sales price which is 00.13%.

For further confirmation, I have conducted t test on each linear regression models. The result of t test shows that all 3 variables have a linear relationship with the house sales price. Just 2 of the variables have a stronger linear relationship than another one.

First, I expect that sqft\_living could explain like 80% of the variation in the house sales price. However, it turns out that sqft\_livig could only explain roughly 50% of that. This shows that sqft\_living is not the biggest factor that are causing the variation in the house sales price. This also shows that there is other factor affecting the variations of house sales price. This is something interesting for further investigation.

Then, I expect that grade and house conditions could explain roughly 60% of the variation in the house sales price. But it turns out that Grade could only explain 44.54%. So, just like sqft\_living, grade can only a portion of the variations.

For house conditions, it is the weirdest one. According to Opendoor.com, homes that are newer appraise at a higher value (in better condition). But the house condition could only explain 00.13%. This shows that house condition is not an important factor in affecting the house sales price. House sales price will be affected more by the grade and sqft\_living than the factor, house conditions

#### (E) Is grade related to conditions in any ways?

After I found out that Grade and house conditions affect the variation of house sales price differently. I want to further investigate these 2 variables which seem connected in some ways. My hypothesis is that a house with good house conditions will have a high grade too. So, I decided to run a Chi Square test of Independence on the grade variables and house conditions variable on a significance level of 0.05 and a degree of freedom of 44.

To do this Chi Square test of Independence, I have calculated the  $X^2$  value which is 2225.6 and the critical value is 60.481. So, the  $X^2$  value is more than the critical value a lot, this shows that Grade is dependent of the house conditions. House Conditions have some kind of relationship with the Grade.

#### (F) Mean house sales price in USA and Mean house sales price in California

So, I also decide to do a test between USA and California. The purpose I do this test is to study is the mean house sales price in USA same as that in California. So, I decided to do a Two Means, independent samples, unknown  $\sigma^2$  test at a significance level of 0.05. Then the result I get is that the t value is much higher than that of critical value and the p-value is less than 0.05. So, the mean of house sales price in USA is different from that of California. The reason behind this result could be that the location, economic, market and other factors causing the difference between mean of house sales price in USA and California. (Unknown, 2019)

#### (G) Possible Factor in affecting the house sales price

First, according to Opendoor.com, Economic and local market (if there is a lot of buyer) is a factor that might affect house sales price. For example, if employment or wage growth slows, then fewer people might be able to afford a home. Then, there will be less demand for house. SO, this will affect the house sales price. (Gomez, 2019) Then, the location of a property is also an important factor. For instance, if it is close to places or things like public transport, shops, schools and restaurants. Then the price will be higher. (Unknown, 2019) Lastly, if the house is at an areas with good reputations, low crime ratesm then it will have a higher price too. (Whitten, 2017)

## 4.0 Conclusion

In this project, I learned a lot of things and can make a few conclusions:

- First, the USA house price has varied a lot from the past
- And there are many factors affecting & also not affecting the house sales price. The price is not necessarily affected by the factors like total square feet, grade, No of floors only. There are other factors that are not obvious like location, economic and market which are affecting house sales price
- And the general price in USA is different from that of California

In a nutshell, although we might be able to predict house sales price based on these factors, but there is a lot of unforeseen variables we need to take in consider also before predicting the house sales price.

## 5.0 References

- Bognar, M. (2019). *Normal Distribution*. Retrieved from Department of Statistics and Actuarial Science: <https://homepage.divms.uiowa.edu/~mbognar/applets/normal.html>
- Bognar, M. (2019). *Student's t-Distribution*. Retrieved from Department of Statistics and Actuarial Science: <https://homepage.divms.uiowa.edu/~mbognar/applets/t.html>
- Bognar, M. (2020). *Chi-Square Distribution*. Retrieved from Department of Statistics and Actuarial Science: <https://homepage.divms.uiowa.edu/~mbognar/applets/chisq.html>
- Gomez, J. (27 3, 2019). *8 critical factors that influence a home's value*. Retrieved from opendoor.com: <https://www.opendoor.com/w/blog/factors-that-influence-home-value>
- Unknown. (03 May, 2019). *7 Factors Impacting Price in Malaysia's Property Market*. Retrieved from propertyguru.com.my: <https://www.propertyguru.com.my/property-guides/7-factors-impacting-price-in-malaysia-s-property-market-13759>
- Whitten, R. (2017). *What influences a property's value?* Retrieved from finder.com: <https://www.finder.com.au/what-influences-a-property-s-value>