



UTM
UNIVERSITI TEKNOLOGI MALAYSIA

**PROBABILITY & STATISTICAL DATA
ANALYSIS**

SEC12143-10
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ASSIGNMENT 4

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PSDA (Assignment 4)

Ref:

Date:

Question 1

$$(a) \text{ i) } \hat{p} = \frac{990}{1100}$$

$$= 0.9$$

$$\text{ii) confidence interval} = p \pm 2.575 (SE)$$

$$SE = \sqrt{\frac{(0.9)(0.1)}{1100}}$$

$$CI = (0.9) \pm (2.575) (9.045 \times 10^{-3})$$

$$= 0.9 \pm (0.023)$$

$$= 9.045 \times 10^{-3}$$

$$= (0.877, 0.923)$$

$$(b) \quad n=16, \text{ mean} = 18.6, \text{ s.d} = 9.486$$

$$\bar{x} \pm (1.341) (s/\sqrt{n})$$

$$= 18.6 \pm (1.341) (9.486/\sqrt{16})$$

$$= 18.6 \pm (1.341) (2.372)$$

$$= 18.6 \pm 3.18$$

$$= (15.42, 21.78)$$

Question 2

(a) A type I error is the rejection of the null hypothesis when it is true. So, the allergist could commit a type I error if he concludes that less than 30% of the public is allergic to some cheese products, but in fact it is true that 30% of the public is allergic to some cheese products.

(b) mean = 35, s.d = 4.3

i) $H_0: \mu = 35$, $H_1: \mu < 35$

ii) $\alpha = 0.05$

$$\text{Test statistic, } t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

$$= \frac{33.1 - 35}{4.3/\sqrt{20}}$$

$$t = -1.976$$

$$P\text{-value} = P(Z < -1.98) = 0.0239$$

* Conclusion = Since $0.0239 < 0.05$, fail to reject H_0 . There is sufficient evidence to support that the mean is less than 35 minutes.

(c) i) $H_0: \sigma = 0.470$, $H_1: \sigma < 0.470$

ii) $\chi^2 = \frac{(n-1)s^2}{\sigma^2}$

mean = 3.675

$$\chi^2 = \frac{(16-1)(2.55)^2}{(0.470)^2}$$

$$s = \sqrt{6.481}$$

$$\chi^2 = 441.55$$

$$= 2.55$$

$$\chi^2 = 21.01$$

iii) Critical value = $t_{0.05, 15} = 7.261$

iv) Conclusion = Since $7.261 < 21.01$, reject H_0 . The vitamin supplement does appear to affect the variation among birth weights.

Question 3

$$(a) \hat{p} = \frac{130}{350} = 0.371$$

$$95\% \text{ CI} = 0.371 \pm 1.960 \left(\sqrt{\frac{(0.371)(0.629)}{350}} \right)$$

$$= 0.371 \pm 0.05$$

$$= (0.321, 0.421)$$

$\therefore$ I am 95% confident that the population of all food shops with special offers is between 0.321 and 0.421.

$$(b) \text{ Margin of error} = 1.960 \left(\sqrt{\frac{(0.371)(0.629)}{n}} \right)$$

$$1.960 \left(\sqrt{\frac{(0.371)(0.629)}{n}} \right) = 0.04$$

$$\left(\sqrt{\frac{(0.371)(0.629)}{n}} \right) = \frac{1}{49}$$

$$\frac{(0.371)(0.629)}{n} = \frac{1}{2401}$$

$$n = 560.29$$

$$n \approx 561$$

$\therefore$ The new size, n of the random sample is 561.

Question 4

$$(a) \text{ mean} = 58392, \sigma = 648, n = 6, \alpha = 0.05, z = \frac{58392 - 58000}{648/\sqrt{6}}$$

$$H_0: \mu = 58000$$

$$z = 1.48$$

$$H_1: \mu \neq 58000$$

$$P(z > 1.48) = 1 - P(z \leq 1.48)$$

$$= 1 - 0.9306$$

$$= 0.0694$$

* Fail to reject H_0 . There is sufficient evidence that shows $\mu = 58000$, since P value $0.0694 \geq 0.025$

$$(b) \sigma^2 = 0.18, n = 101, s^2 = 0.13, \alpha = 0.05, \chi^2 = \frac{(n-1)s^2}{\sigma^2}$$

$$H_0: \sigma^2 = 0.18$$

$$= \frac{(101-1)(0.13)}{0.18}$$

$$H_1: \sigma^2 \neq 0.18$$

$$\chi^2 = 72.22$$

$$\text{Critical value} \Rightarrow \chi^2_{0.025, 100} = 124.342$$

$$\chi^2_{0.975, 100} = 74.22$$

* Since $72.22 < 74.22$, reject H_0 . There is sufficient evidence that support the variance of measurement that is not equal to $0.18(\text{inch})^2$.

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Question 5

$$a) \hat{p} = \frac{y}{n} = \frac{280}{418}$$

$$n = 418$$

$$y = 280$$

$$\hat{p} = 0.67$$

$$\hat{p} \pm (z) \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = 0.67 \pm (1.96) \sqrt{\frac{0.67(1-0.67)}{418}}$$

$$= 0.67 \pm (0.045) = (0.625, 0.715)$$

95% confident that the true proportion of all insured patients who blame rising insurance rates on large court settlements against doctors is between 0.625 and 0.715

$$b) n = 126$$

$$\bar{x} = 29.2$$

$$\sigma = 7.5$$

$$CI = 90\% = 1.645$$

$$\bar{x} \pm (z) \left(\frac{\sigma}{\sqrt{n}} \right)$$

$$= 29.2 \pm (1.645) \left(\frac{7.5}{\sqrt{126}} \right)$$

$$= 29.2 \pm 1.1 = (28.1, 30.3)$$

90% confident that the blood lead level is between 28.1 and 30.3

Question 6

a) $n = 64$

$H_0: \mu = 40 \text{ months}$

$\bar{x} = 38$

$H_1: \mu < 40 \text{ months}$

$\sigma = 5.8$

$\alpha = 0.05$

$\mu = 40$

$$Z = \frac{\bar{x} - \mu}{(\sigma / \sqrt{n})} = \frac{38 - 40}{(5.8 / \sqrt{64})}$$

$Z = -2.76$

$P(Z < -2.76) = 0.0029$

H_0 is rejected. $\mu < 40$ months is proven with evidence. advise given in manual is not good.

b) $\mu = 10$

$n = 10$

$\alpha = 0.01$

$$\bar{x} = \frac{10.2 + 9.7 + 10.1 + 10.3 + 10.1 + 9.8 + 9.9 + 10.4 + 10.3 + 9.8}{10}$$

$\bar{x} = 10.06$

$$s = \sqrt{\frac{[(10.2 - 10.06)^2 + (9.7 - 10.06)^2 + (10.1 - 10.06)^2 + (10.3 - 10.06)^2 + (10.1 - 10.06)^2 + (9.8 - 10.06)^2 + (9.9 - 10.06)^2 + (10.4 - 10.06)^2 + (10.3 - 10.06)^2 + (9.8 - 10.06)^2]}{9}}$$

$s = 0.246$

$$t = \frac{10.06 - 10}{0.246 / \sqrt{10}} = 0.77 (2) = 1.54$$

Fail to reject H_0 . Evidence that the mean content of container containing particular lubricant is 10 l.

Question 7

$$a) SE = \frac{52.7 - 50.3}{2} = 1.2$$

$$\hat{p} = (\text{upper} - SE)$$

$$\hat{p} = 52.7 - 1.2$$

$$\hat{p} = 51.5$$

$$q = 100 - 51.5$$

$$q = 48.5$$

$$n = \frac{51.5(48.5)}{1.2}$$

$$n = 45.6$$

$$SE = \frac{50.6 - 49.8}{2} = 0.4$$

$$\hat{p} = \text{upper} - SE$$

$$\hat{p} = 50.6 - 0.4$$

$$\hat{p} = 50.2$$

$$q = 100 - 50.2$$

$$q = 49.8$$

$$n = \frac{(50.2)(49.8)}{(0.4)}$$

$$n = 79$$

$(50.3, 52.7) = 45.6$, $(49.8, 50.6) = 79$. $(49.8, 50.6)$ has larger sample.

b) Statistic 2 is recommended due to it being unbiased. Distribution is centered at true value and it has a smaller std. deviation. Value doesn't deviate much, making it accurate.

$$c) \hat{p} \pm (z) \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} = 0.15 \pm 1.645 \sqrt{\frac{0.15(1-0.15)}{500}}$$

$$= 0.15 \pm (0.03) = (0.12, 0.18)$$

90% confident that the true proportions of the market share for the new brand is between 0.12 and 0.18.