
 **SECI 2143 / SCSI 2143**
PROBABILITY & STATISTICAL
DATA ANALYSIS

CHAPTER 1

Introduction to Statistics

innovative • entrepreneurial • global www.utm.my


 **Introduction to Statistics**

- Statistics?


Dad, is this completely safe?

Research in 500 theme parks in 2010 showed that 1 in 10,000 of the carriages were found to be malfunctioning, which can lead to 1 out of 50,000 kids falling out ... So your chances are okay, but there's always a risk, honey ...

People working in statistics are not always the perfect parents




innovative • entrepreneurial • global www.utm.my



Introduction to Statistics

Number of fatal road accidents up in 2016, more than 7,000 lives lost



KUALA LUMPUR: In 2016, total of 7,152 people died in road accidents in Malaysia, an alarming jump from 6,706 deaths in the year before, Transport Minister Datuk Seri Liow Tiong Lai announced today.

"Despite the number of campaigns and initiatives conducted by the government, the painful reality is that the accident rate keeps increasing every year.

"It's too late when tragic accidents like the bus crash in Pagoh, which claimed 14 lives, occur. There is no use accusing anyone and finger pointing then," he said at the launch of the Chinese New Year Road Safety campaign in Sunway Pyramid here.

He added that of that number, 62.7 per cent of the deaths involved motorcyclists in 2016.

"In 2016, 6,570 fatal road accidents involving were recorded while in 2015 there were 6,193 of such cases.

Liow said a total of 521,466 accidents were recorded in 2016, an increase from 489,606 in 2015.

"A total of 80.6 per cent of the road accidents are caused by human error.


"I hope that those on the road this festive season do not speed to their destination (just) to arrive early and gamble their lives or that of their loved ones. It's okay to be late as long as you are safe," he advised.

The joint campaign involving the police and other transport authorities like the Road Transport Department will begin on Jan 21 and end on Feb 5.

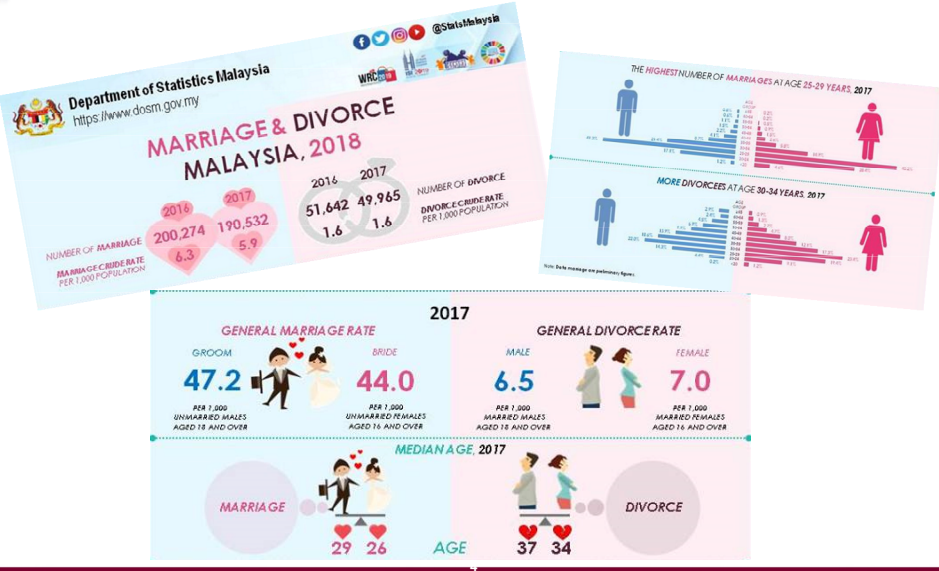
He also said that there would be increased patrols by authorities at 102 road accident hotspots nationwide.

innovative • entrepreneurial • global

www.utm.my



Introduction to Statistics



Department of Statistics Malaysia
https://www.dosm.gov.my

MARRIAGE & DIVORCE MALAYSIA, 2018

2018	2017	2016	2017
200,274	190,532	51,642	49,965
6.3	5.9	1.6	1.6
NUMBER OF MARRIAGE		NUMBER OF DIVORCE	
MARRIAGE CRUDE RATE PER 1,000 POPULATION		DIVORCE CRUDE RATE PER 1,000 POPULATION	

GENERAL MARRIAGE RATE 2017

GROOM: 47.2
BRIDE: 44.0

PER 1,000 UNMARRIED MALES AGED 15 AND OVER

PER 1,000 UNMARRIED FEMALES AGED 15 AND OVER

GENERAL DIVORCE RATE

MALE: 6.5
FEMALE: 7.0

PER 1,000 MARRIED MALES AGED 15 AND OVER

PER 1,000 MARRIED FEMALES AGED 15 AND OVER

MEDIAN AGE 2017

MARRIAGE: 29 (Male), 26 (Female)

DIVORCE: 37 (Male), 34 (Female)

AGE

innovative • entrepreneurial • global

www.utm.my



Introduction to Statistics



facebook Community Update 4.27.2016

Platform	User Base
Facebook	1.65 Billion on Facebook each month
WhatsApp	1 Billion on WhatsApp each month
Messenger	900 Million on Messenger each month
Instagram	400 Million on Instagram each month

LIVE Live Video Launched worldwide

Connectivity 25 million connected via Internet.org


Artificial Intelligence Access for the blind and visually impaired

Oculus Rift Shipped with 50+ games and apps

Introduced Reactions

Reaction	Emoji
Like	👍
Love	❤️
Haha	😂
Wow	😮
Sad	😞
Angry	😡


innovative • entrepreneurial • global www.utm.my



Introduction to Statistics

- Even though you may not have realized it, you probably have made some statistical statements in your everyday conversation or thinking.
- Statements like "I sleep for about eight hours per night on average" and "You are more likely to pass the exam if you start preparing earlier" are actually statistical in nature.


innovative • entrepreneurial • global www.utm.my



Introduction to Statistics

- We encounter data and conclusions based on data every day.
- Statistics is the scientific discipline that provides methods to help us make sense of data.
- Statistical methods are used in business, medicine, agriculture, social sciences, natural sciences, and applied sciences, such as engineering.
- The field of statistics teaches us how to make intelligent judgments and informed decisions in the presence of uncertainty and variation.

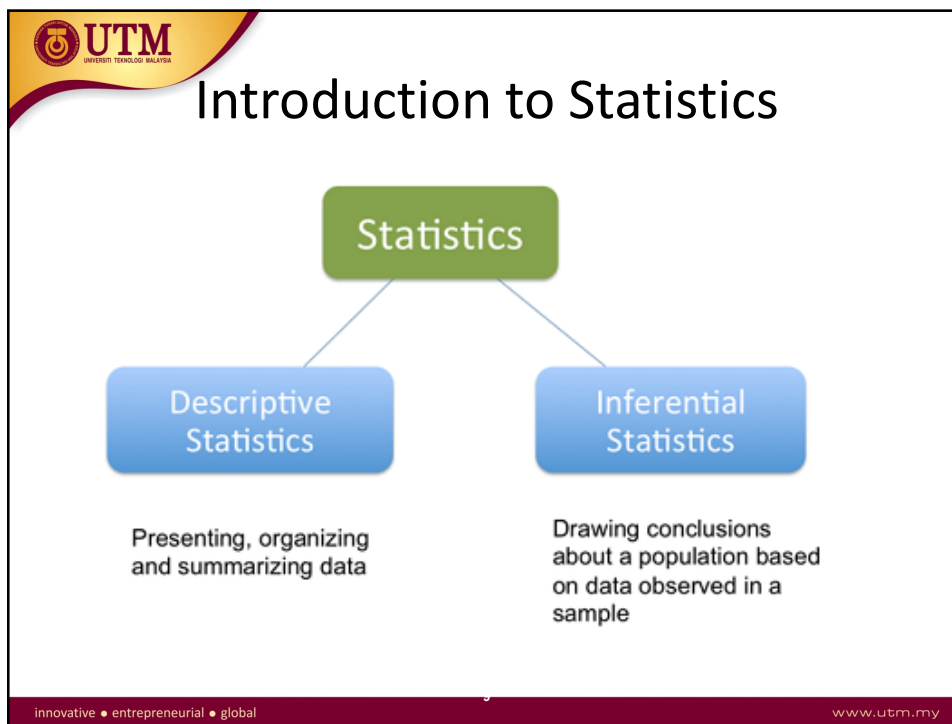
innovative • entrepreneurial • global www.utm.my



Introduction to Statistics

- Statistics is the scientific application of mathematical principles to the collection, analysis, and presentation of numerical data.
- Statistics is a discipline which is concerned with:
 - designing experiments and other data collection,
 - summarizing information to aid understanding,
 - drawing conclusions from data, and
 - estimating the present or predicting the future.
- There are 2 main branches of statistics:
 - Descriptive
 - Inferential

innovative • entrepreneurial • global www.utm.my




The slide contains a list of bullet points describing descriptive statistics and their classification techniques.

Introduction to Statistics

- **Descriptive statistics** are used to describe the basic features of the data gathered from an experimental study in various ways.
- The techniques are commonly classified as:
 - Graphical description in which we use graphs to summarize data.
 - Tabular description in which we use tables to summarize data.
 - Parametric description in which we estimate the values of certain parameters which we assume to complete the description of the set of data.

UTM UNIVERSITI TEKNOLOGI MALAYSIA


innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA


Descriptive Statistics

Graphical description

Example:
Graph
Bar chart
Pie chart



innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Descriptive Statistics

Tabular description

Example:
Frequency Table

Score	Frequency
0	2
1	5
2	8
3	6
4	4
5	3

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Descriptive Statistics

Parametric description

Mean	μ
Median	μ
Mode	μ
Range	Infinity in both directions.
Standard Deviation	σ
Skewness	0
Kurtosis	3

Normal PDF

Probability Density

x

innovative • entrepreneurial • global

www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Example

	A	B	C	D
1	Respondent #	Age	Gender	Favorite Ice Cream Flavor
2	1	36	m	Vanilla
3	2	22	f	Chocolate
4	3	61	m	Strawberry
5	4	88	m	Other
6	5	31	m	N/A
7	6	53	m	N/A
8	7	30	f	Chocolate
9	8	64	f	Chocolate
10	9	18	m	Vanilla
11	10	16	f	Vanilla
12	11	83	m	Strawberry
13	12	16	f	Strawberry
14	13	94	m	Strawberry
15	14	55	m	Vanilla
16	15	42	f	Chocolate
17	16	18	f	Vanilla
18	17	21	f	Vanilla

Raw Data

Age	
Mean	42.6
Standard Dev.	21.9

Descriptive Statistics

Age

Mean 42.6

Standard Dev. 21.9

Other 14%

N/A 6%

Vanilla 37%

Chocolate 26%

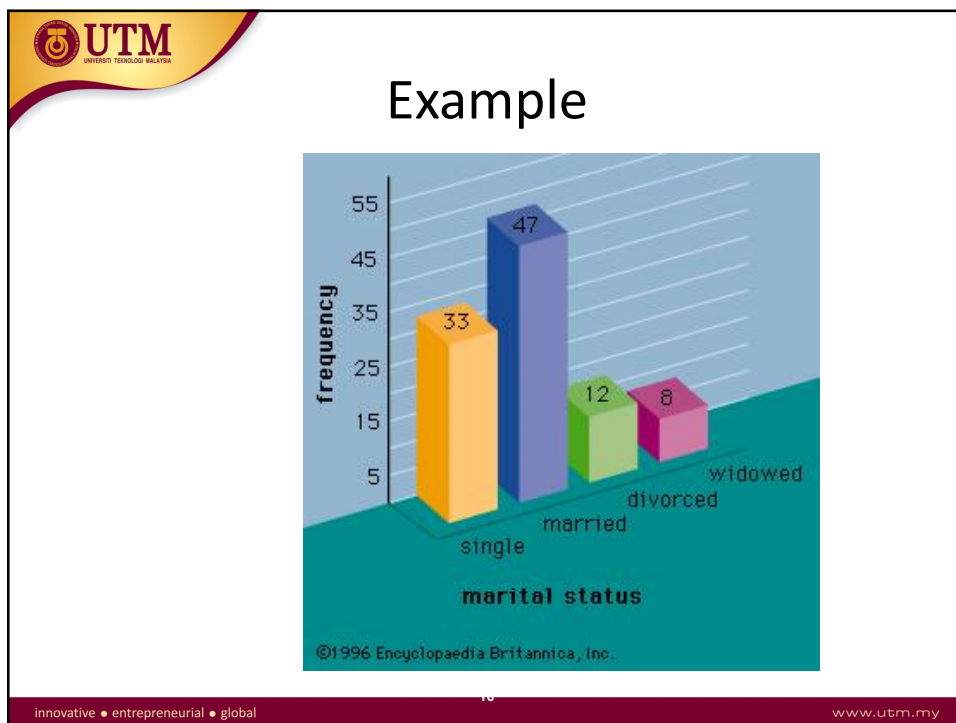
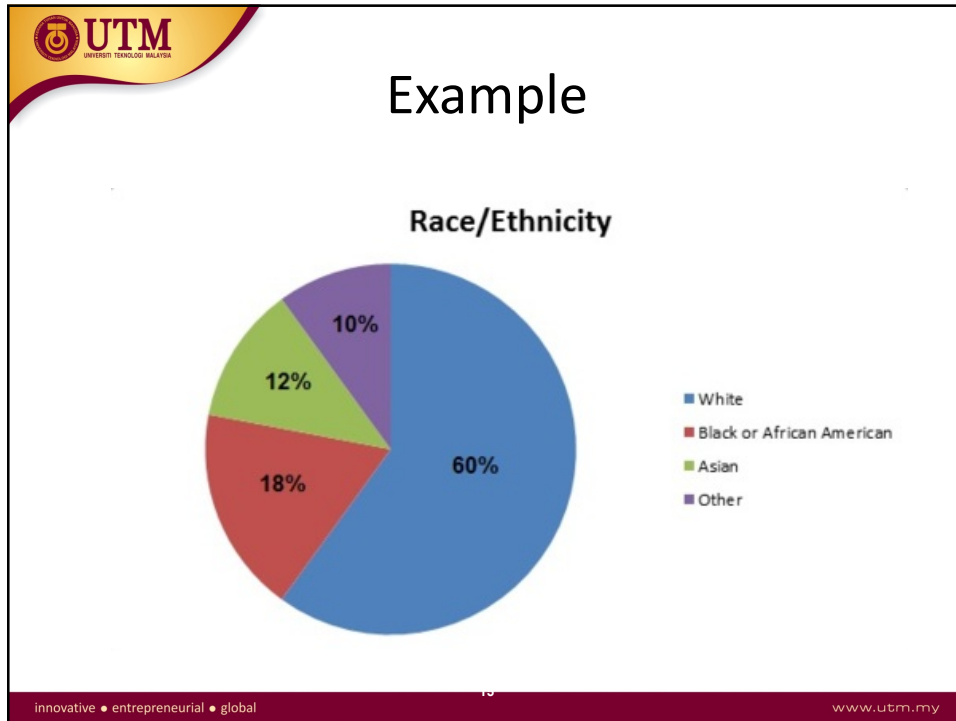
Strawberry 17%

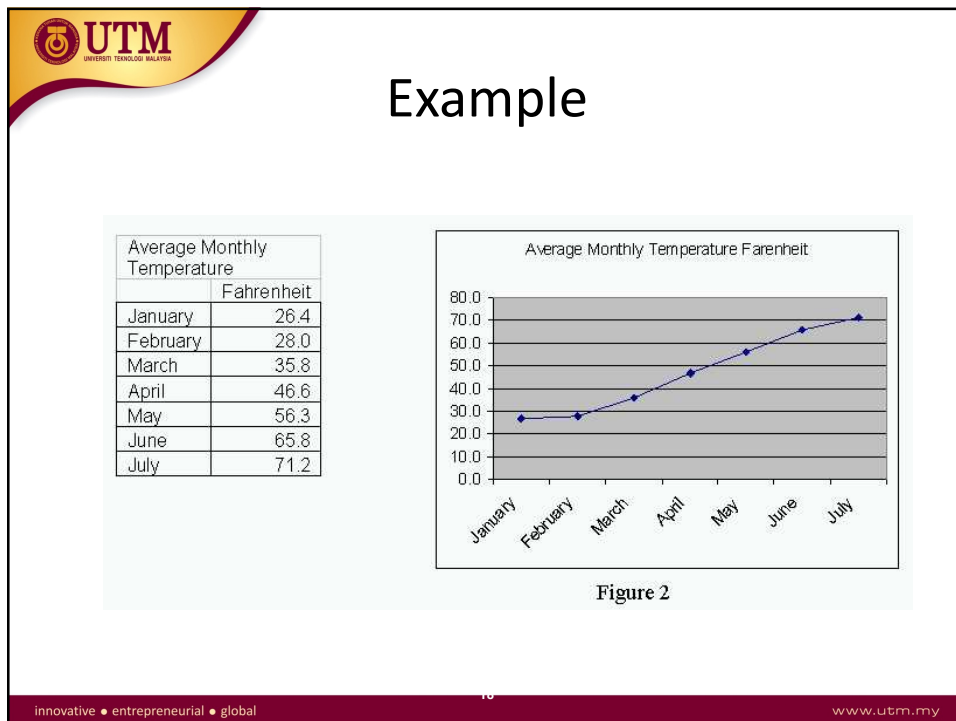
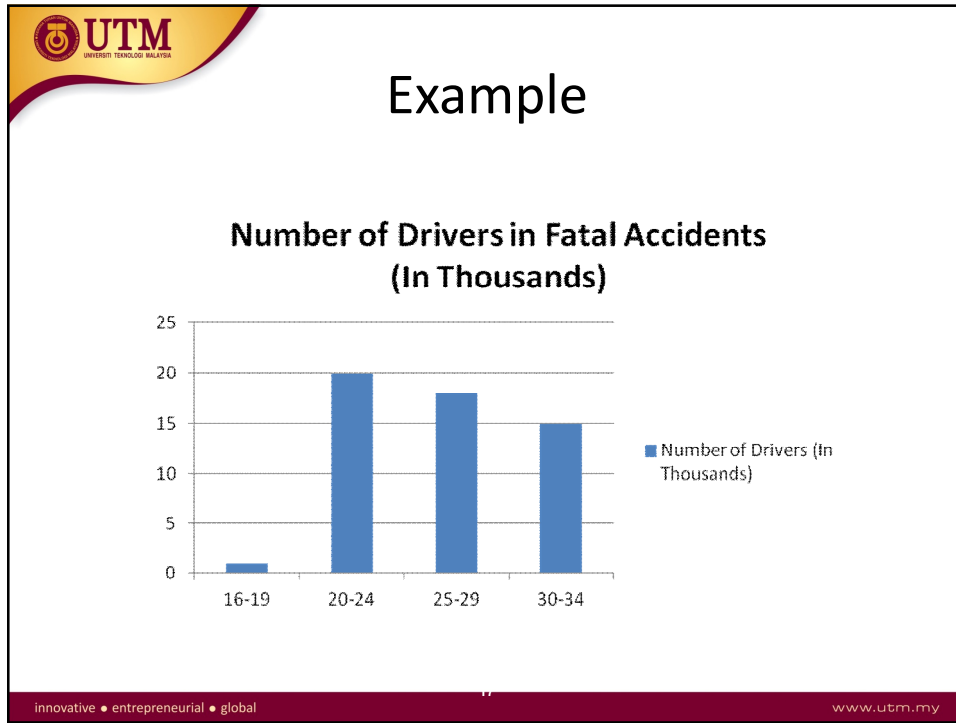
Male

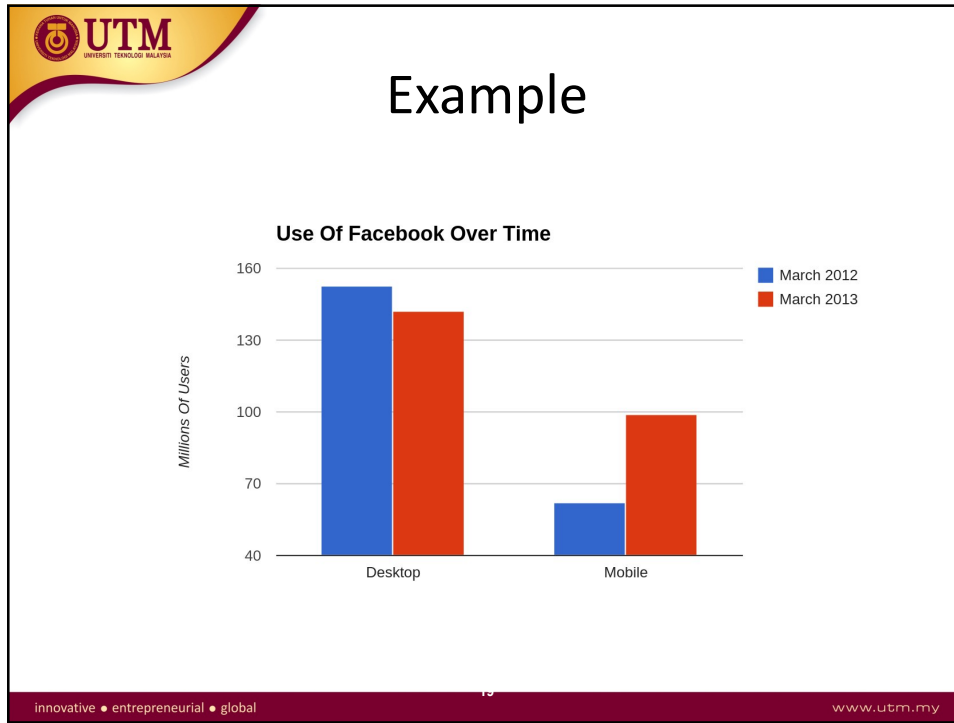
Female

innovative • entrepreneurial • global


www.utm.my







	A	B	C	D	E	F	G
5	Sample 1	Sample 2		Sample 1		Sample 2	
6	19	12					
7	41	27		Mean	30.46154	Mean	30.61538
8	29	18		Standard Error	4.673459	Standard Error	5.447345
9	18	23		Median	29	Median	27
10	8	72		Mode	29	Mode	27
11	29	27		Standard Deviation	16.8504	Standard Deviation	19.64068
12	11	27		Sample Variance	283.9359	Sample Variance	385.7564
13	59	53		Kurtosis	-1.15073	Kurtosis	0.062841
14	41	3		Skewness	0.265601	Skewness	0.78698
15	48	45		Range	51	Range	69
16	53	53		Minimum	8	Minimum	3
17	29	13		Maximum	59	Maximum	72
18	11	25		Sum	396	Sum	398
19				Count	13	Count	13



Example


Table 2 – Clinical and demographic characteristics of patients undergoing pharmacological prophylaxis.

Variable	n = 357			
	Minimum	Maximum	Average	Standard deviation
Age (years)	24	71	40.35	8.829
Weight (kg)	50	130	71.43	12.211
Height (cm)	148	184	162.75	5.980
BMI (kg/m ²)	17.93	52.07	26.9731	4.43736
Weight of the flap (g)	650	9200	1422.82	573.049
Surgery time (min)	55	240	135.30	41.267

BMI = body mass index; n = number of patients.

21

innovative • entrepreneurial • global www.utm.my



Example


TABLE 4
Descriptive statistics of students' attitudes toward statistics

	N	Mode	s.d.	Skewness	Kurtosis
Affect	234	4.6	1.32	-0.45	0.17
Cognitive Competence	232	5.33	1.16	-0.19	-0.62
Value	234	4.88	1.12	-0.62	0.25
Difficulty	233	3.4	1.13	-0.13	-0.65
Interest	231	7	1.26	-1.03	1.09
Effort	235	7	0.98	-2.32	7.85

s.d. = standard deviation
Higher value = more positive attitude

22

innovative • entrepreneurial • global www.utm.my




Example

Variable	Mean	Std. Dev	Min	Max
Loans	0.204E + 07	0.234E + 07	0.000	0.178E + 08
Deposits	0.370E + 07	0.430E + 07	0.000	0.368E + 08
Physical capital	0.488E + 07	0.534E + 07	0.000	0.422E + 08

Source: Banking Supervision Department, Bank of Ghana, and the ARB Apex Bank.

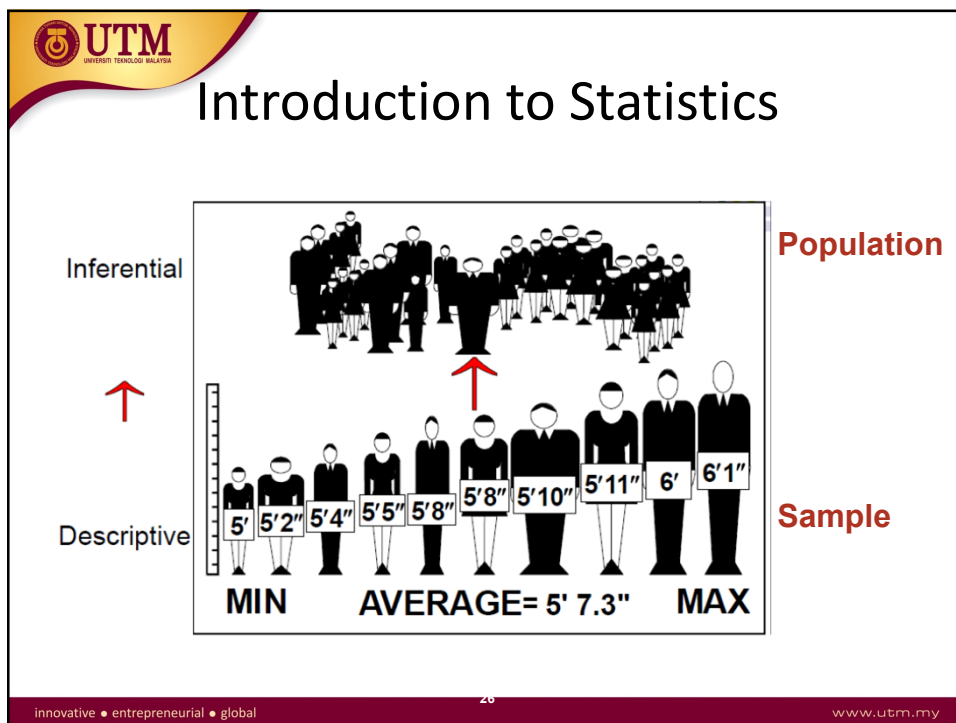
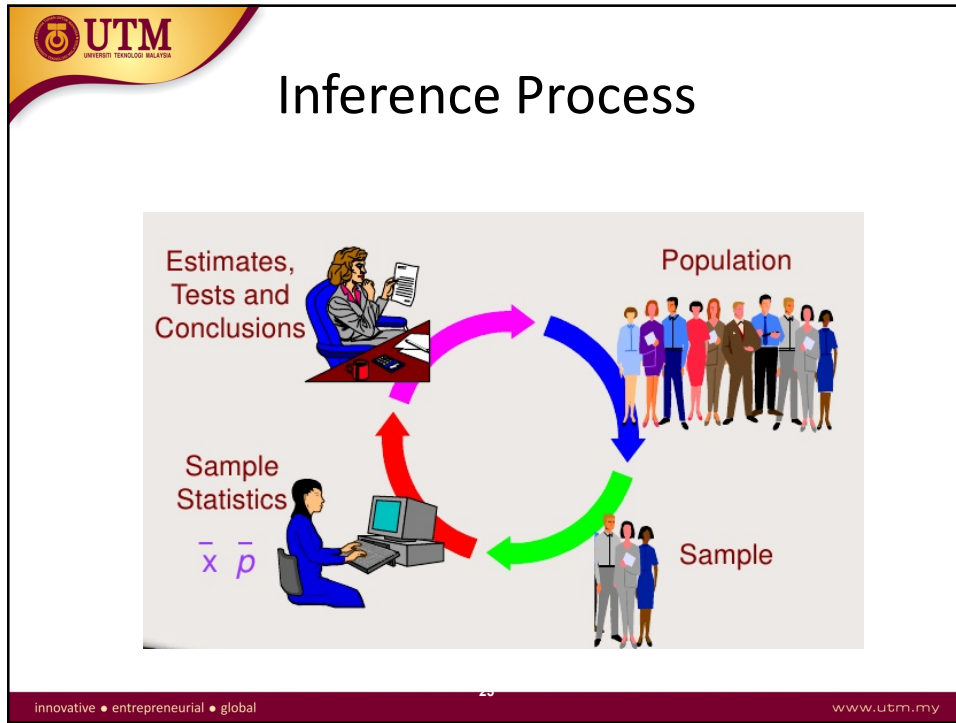
innovative • entrepreneurial • global
www.utm.my




Introduction to Statistics


- **Inferential statistics** are used to draw inferences about a population from a sample.
- It includes:
 - point estimation
 - interval estimation
 - hypothesis testing (or significance testing)
 - prediction

innovative • entrepreneurial • global
www.utm.my




 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Population & Sample



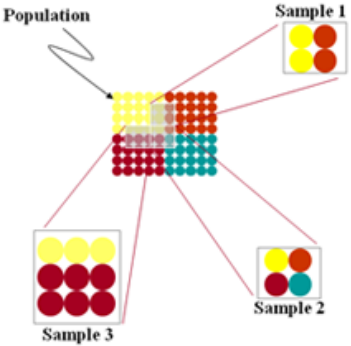
I can't ask everyone here. I think I'll need to get a sample.

innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Population & Sample

- The entire collection of individuals or object about which information is desired is called the **population** of interest.
- A **sample** is a subset of the population, selected for study in some prescribed manner



Population

Sample 1

Sample 2

Sample 3

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Population & Sample

Population (N)

Sample (n)

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Population & Sample

Who do you want to generalize to?

What population can you get access to?

How can you get access to them?

Who is in your study?


The Theoretical Population

The Study Population


The Sampling Frame

The Sample


innovative • entrepreneurial • global www.utm.my



Population & Sample




Population
 quantity (count) = N
 mean = μ
 variance = σ^2
 standard deviation = σ




Sample
 quantity (count) = n
 mean = \bar{x}
 variance = s^2
 standard deviation = s

innovative • entrepreneurial • global
www.utm.my



Population & Sample


We want to know about these



Population

Parameter μ
(Population mean)


We have these to work with




Sample

Statistic \bar{x}
(Sample mean)

Random selection



Inference



innovative • entrepreneurial • global
www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Example

Variable | response | 1 2 3 **4** 5

Statistic | sample | Average = 3.75

Parameter | population | Average = 3.72

33

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Example

Population

Mean, μ , is unknown

Sample

Random Sample

Mean $\bar{X} = 50$

I am 95% confident that μ is between 40 & 60.

34

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Example

A new milk formulation designed to improve the psychomotor development of infants was tested on randomly selected infants. Based on the results, it was concluded that the new milk formulation is effective in improving the psychomotor development of infants.

STATISTICAL RESEARCH TRAINING CENTER

UNIVERSITI TEKNOLOGI MALAYSIA

innovative • entrepreneurial • global

www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Data Analysis Process

```

graph TD
    Population[Population] --> RandomSample[Random Sample]
    RandomSample --> SampleStatistics[Sample Statistics]
    SampleStatistics --> Population
    RandomSample -- Describe --> SampleStatistics
    SampleStatistics -- Make Inferences --> Population
  
```

Describe

Make Inferences


Population

Random Sample

Sample Statistics

innovative • entrepreneurial • global


www.utm.my



Data Analysis Process

- Statistics involves the **collection** and **analysis** of data.
- Both task are critical.
- Raw data without analysis are of little value, and even a sophisticated analysis cannot extract meaningful information from data that were not collected in a sensible way.
- The data analysis process can be viewed as a sequence of steps that lead from planning to data collection to informed conclusions based on the resulting data.


innovative • entrepreneurial • global www.utm.my



Data Analysis Process

- 6 steps:
 - Understanding the nature of the problem
 - Deciding what to measure and how to measure it
 - Data collection
 - Data summarization and preliminary analysis
 - Formal data analysis
 - Interpretation of results


innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Data Analysis Process


1. Understanding the nature of the problem
 - An understanding of the research problem
 - Know the goal of the research and what questions we hope to answer
 - Have a clear direction before gathering data to lessen the chance of being unable to answer the questions of interest using the data collected.

innovative • entrepreneurial • global www.utm.my


 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Data Analysis Process

2. Deciding what to measure and how to measure it
 - In some cases, the choice is obvious, e.g. in a study of the relationship between the weight of a football player and position played, you would need to collect data on player weight and position.




innovative • entrepreneurial • global www.utm.my



Data Analysis Process

- but in other cases the choice of information is not as straightforward, e.g. in a study of the relationship between preferred learning style and intelligence, how would you define learning style and measure it and what measure of intelligence would you use?
- It is important to carefully define the variables to be studied and to develop appropriate methods for determining their values.

innovative • entrepreneurial • global www.utm.my




Data Analysis Process

3. Data collection

- Decide whether an existing data source is adequate or whether new data must be collected.
- If a decision is made to use existing data (secondary data), it is important to understand how the data were collected and for what purpose.
- If new data are to be collected (primary data), a careful plan must be developed.
- The type of analysis that is appropriate and subsequent conclusions that can be drawn depend on how the data are collected.


innovative • entrepreneurial • global www.utm.my



Data Analysis Process

4. Data summarization and preliminary analysis
 - Summarizing the data graphically and numerically
 - This initial analysis provides insight into important characteristics of the data and can provide guidance in selecting appropriate methods for further analysis.

innovative • entrepreneurial • global www.utm.my



Data Analysis Process

5. Formal data analysis
 - Select and apply the appropriate inferential statistical methods.
6. Interpretation of results
 - What conclusions can be drawn from the analysis?
 - How do the result of the analysis inform us about the stated research problem or question?
 - How can our results guide future research?

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Primary & Secondary Data

- **Secondary data** is data which has been collected by individuals or agencies for purposes other than those of our particular research study.
 - For example, if a government department has conducted a survey of, say, family food expenditures, then a food manufacturer might use this data in the organization's evaluations of the total potential market for a new product.
- **Primary data**, by contrast, are collected by the investigator conducting the research.

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Primary & Secondary Data

```

graph LR
    Data[Data  
• Facts and figures pertinent to the problem] --> Secondary[Secondary data  
• Facts and figures already recorded prior to the project]
    Data --> Primary[Primary data  
• Facts and figures newly collected for the project]
    Secondary --> Internal["Internal data  
(inside the firm)"]
    Secondary --> External["External data  
(outside the firm)"]
    Primary --> Observational["Observational data  
(watching people)"]
    Primary --> Questionnaire["Questionnaire data  
(asking people)"]
  
```

Data
• Facts and figures pertinent to the problem

Secondary data
• Facts and figures already recorded prior to the project

Primary data
• Facts and figures newly collected for the project

Internal data (inside the firm)
• Financial statements, research reports, files, customer letters, sales call reports, and customer lists

External data (outside the firm)
• U.S. Census reports, trade association studies and magazines, business periodicals, and Internet-based reports

Observational data (watching people)
• Mechanical and electronic approaches
• Personal approaches

Questionnaire data (asking people)
• Idea generation through in-depth interviews and focus groups
• Idea evaluation by mail, online, telephone, and personal surveys

innovative • entrepreneurial • global www.utm.my

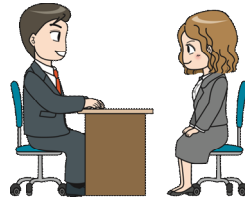
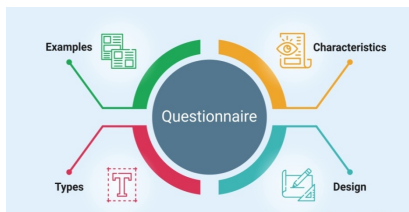

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Data Sources

Primary data: Experiment

Experiments

Primary data: Survey (Questionnaire, Interview)








innovative • entrepreneurial • global www.utm.my


UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Data Sources

Secondary data: existing databases, record review




innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Qualitative & Quantitative Data

Qualitative Data	Quantitative Data
<p>Overview:</p> <ul style="list-style-type: none"> ■ Deals with descriptions. ■ Data can be observed but not measured. ■ Colors, textures, smells, tastes, appearance, beauty, etc. ■ Qualitative → Quality 	<p>Overview:</p> <ul style="list-style-type: none"> ■ Deals with numbers. ■ Data which can be measured. ■ Length, height, area, volume, weight, speed, time, temperature, humidity, sound levels, cost, members, ages, etc. ■ Quantitative → Quantity


innovative • entrepreneurial • global 49
www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Qualitative & Quantitative Data

Example 1:

- *Oil Painting*



<p>Qualitative data:</p> <ul style="list-style-type: none"> • blue/green color, gold frame • smells old and musty • texture shows brush strokes of oil paint • peaceful scene of the country • masterful brush strokes 	<p>Quantitative data:</p> <ul style="list-style-type: none"> • picture is 10" by 14" • with frame 14" by 18" • weighs 8.5 pounds • surface area of painting is 140 sq. in. • cost \$300
--	---


innovative • entrepreneurial • global 50
www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Qualitative & Quantitative Data

Example 2:

- **Latte**




<p>Qualitative data:</p> <ul style="list-style-type: none"> • robust aroma • frothy appearance • strong taste • burgundy cup 	<p>Quantitative data:</p> <ul style="list-style-type: none"> • 12 ounces of latte • serving temperature 150° F. • serving cup 7 inches in height • cost \$4.95
---	---

innovative • entrepreneurial • global www.utm.my


UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Qualitative & Quantitative Data




She looks 'beautiful'..
her dress is 'awesome'.. and
She dresses 'very well' !!

I can give 9.5/10 for her looks,
9/10 for her choice of dress and
10/10 for her dressing sense !!




Qualitative Analysis !!
(Purely "Subjective")

WWW.MYBIZMASTER.COM

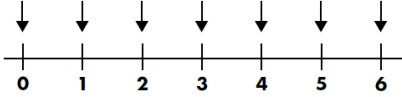


Quantitative Analysis !!
(Purely "Objective")

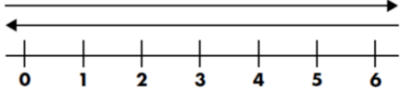
innovative • entrepreneurial • global www.utm.my

 **Discrete & Continuous Data**


Discrete data can only take on certain individual values.




Continuous data can take on any value in a certain range.



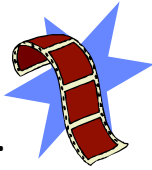
innovative • entrepreneurial • global www.utm.my

 **Discrete & Continuous Data**


Example 1
Number of pages in a book is a **discrete variable**.



Example 2
Length of a film is a **continuous variable**.



Example 3
Shoe size is a **Discrete variable**.
E.g. 5, 5½, 6, 6½ etc. Not in between.

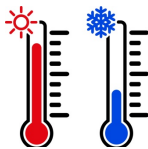


innovative • entrepreneurial • global www.utm.my


UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Discrete & Continuous Data


Example 4
Temperature is a **continuous variable**.



Example 5
Number of people in a gathering is a **discrete variable**.



Example 6
Time taken to run a race is a **continuous variable**.

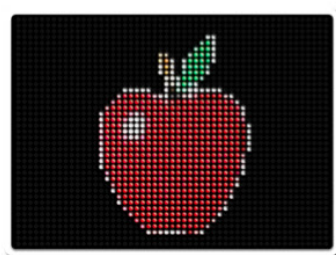


innovative • entrepreneurial • global www.utm.my


UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Discrete & Continuous Data

Discrete vs. Continuous



LITE BRITE
discrete



ETCH-A-SKETCH
continuous

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Discrete & Continuous Data

Group the following as either discrete or continuous data.

Speed of a car

Population of a town

Length of a crocodile

Number of matches in a box

Temperature of oven

Number of goals in a season

Shirt collar size

Volume of a cereal box

Discrete?
Continuous?


innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Discrete & Continuous Data


Discrete	Continuous
<p>Population of a town</p> <p>Number of matches in a box</p> <p>Shirt collar size</p> <p>Number of goals in a season</p>	<p>Volume of a cereal box</p> <p>Top speed of a car</p> <p>Length of a crocodile</p> <p>Temperature of oven</p>

innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA


Discrete & Continuous Data

- How about money? Is it a discrete or continuous data?



Discrete!!
But why?


innovative • entrepreneurial • global www.utm.my

 **UTM**
UNIVERSITI TEKNOLOGI MALAYSIA

Levels of Measurement

- There are four levels of data measurement. Ranked from top to bottom in order of complexity and information content these are:
 - Nominal scale
 - Ordinal scale
 - Interval scale
 - Ratio scale


innovative • entrepreneurial • global www.utm.my



Levels of Measurement

- Each level of measurement is characterized by its properties.
 - Nominal measurement has just one property: CLASSIFICATION.
 - Ordinal measurement has two properties: CLASSIFICATION and ORDER.
 - Interval measurement has three properties: CLASSIFICATION, ORDER and EQUAL INTERVALS.
 - Ratio data has four properties: CLASSIFICATION, ORDER, EQUAL INTERVALS and TRUE ZERO.

innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Nominal Scales

- **Properties:** classification
- **Observations reflect:** differences in kind
- **Examples:** gender, ethnic background, major in college
- Nominal measurement is simply concerned with sorting observations into categories.
- Because the single property of nominal data is classification it tells us nothing about differences in degree or amount.

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Levels of Measurement - Nominal Scales

- Numbers assigned to categories (as identification codes) have no numeric value (we cannot add, subtract, divide or multiply nominal data) and any ordering of categories is arbitrary.
- This is the most primitive form of measurement. The presence vs. absence of something is a form of nominal measurement (“do you smoke?” YES, NO).
- Although it is considered a form of measurement the collection of nominal data is more easily thought of as a sorting method.

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Levels of Measurement - Nominal Scales

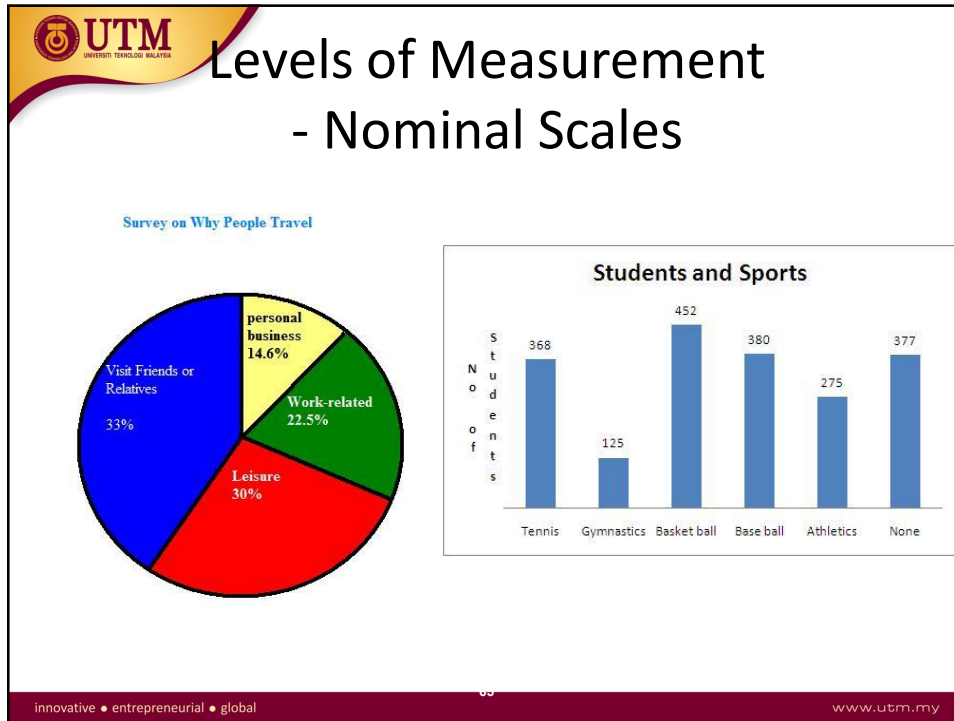
Example

Nominal Data

Point	airport ✕	town ●	mine ⚡	capital ★
Line	river —	road —	boundary - - -	pipeline
Area	orchard 🌳	desert 🏜️	forest 🌲	water 💧

The bar chart displays the percentage of people for four different occupations. The y-axis is labeled '% of People' and ranges from 0 to 40 in increments of 5. The x-axis is labeled 'Type of Occupation' and lists four categories: Students, Politicians, Executives, and Athletes. The bars show the following percentages: Students at 10%, Politicians at 30%, Executives at 40%, and Athletes at 20%.

innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Nominal Scales

What is your gender?

M - Male

F - Female

What is your hair color?

1 - Brown

2 - Black

3 - Blonde

4 - Gray

5 - Other

Where do you live?

A - North of the equator

B - South of the equator

C - Neither: In the international space station


Sometimes numbers are used to designate category membership

Example:

Country of Origin	
1 = United States	3 = Canada
2 = Mexico	4 = Other

However, in this case, it is important to keep in mind that the numbers do not have intrinsic meaning


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ordinal Scales

- **Properties:** classification, order
Observations reflect: differences in degree
Examples: Likert scale categories, rankings, academic letter grade, stages in development
- The distinctive property of ordinal measurement is order.
- On a typical Likert Scale “strongly agree” represents more agreement than “agree”. However, we do not know how much more.

innovative • entrepreneurial • global www.utm.my




Levels of Measurement - Ordinal Scales

Example: The Likert Scale

	Strongly Agree	Agree	Neither	Disagree	Strongly Disagree
If the price of raw materials fell firms would reduce the price of their food products.	1	2	3	4	5
Without government regulation the firms would exploit the consumer.	1	2	3	4	5
Most food companies are so concerned about making profits they do not care about quality.	1	2	3	4	5
The food industry spends a great deal of money making sure that its manufacturing is hygienic.	1	2	3	4	5
Food companies should charge the same price for their products throughout the country	1	2	3	4	5


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ordinal Scales

- Similarly if Comedian A is ranked 1st for funniness, and Comedian B is ranked 4th we have no way of knowing how much funnier Comedian A is than Comedian B.
- We cannot assume that they are four times funnier.
- They may be more or less than four times funnier.
- But we do know that they are more funny than Comedian B, and more funny than the comedians ranked 2nd and 3rd places as well.
- We know about order but we have no information about the size of the interval between points.

innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ordinal Scales

Example

Ordinal Data

Point	Airports international national regional	Oil well production high medium low	Populated places large medium small
Line	Roads expressway major local	Drainage river stream creek	Boundaries international provincial county
Area	Soil quality good fair poor	Cost of living high medium low	Industrial regions major minor

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Levels of Measurement - Ordinal Scales

Example

An ordinal data example

How often do you eat cheese for breakfast?

	Code
always	6
usually	5
often	4
sometimes	3
occasionally	2
rarely	1
never	0

"always" is clearly more frequent than "sometimes" but not necessarily twice as frequent, even though $6 = \text{twice } 3$

innovative • entrepreneurial • global www.utm.my

UTM
UNIVERSITI TEKNOLOGI MALAYSIA

Levels of Measurement - Ordinal Scales

Example


Hot

Hotter

Hottest

The " Hot" Scale


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Interval Scales

- **Properties:** classification, order, equal intervals
Observations reflect: measurable differences in amount
Examples: IQ scores, degrees of temperature,
- Essentially, interval data are ordinal, but they have an extra property - the ability to meaningfully add and subtract measurements.
- In interval-scaled data, the gaps between the numbers are comparable, unlike with ordinal data.
- Any interval has the same meaning regardless of its location on the scale. "X is five inches longer than Y" has meaning regardless of the values of X and Y.


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Interval Scales

- However, ratios are meaningless on an interval scale because an interval scale has no true zero.
- Temperature scales are an example of this, so are decibel scales.
- Zero degrees Fahrenheit does not mean the total absence of temperature.
- Zero decibels does not mean there is no sound.


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Interval Scales

- Furthermore, if it is 80 degrees outside today and it was only 40 degrees outside yesterday we cannot say that today is twice as hot as yesterday.
- Similarly a sound level of 80 dB is not twice as loud as a sound level of 40 dB.
- In short, if the data can be ordered and the arithmetic difference is meaningful, then the data are at least interval data.


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ratio Scales

- **Properties:** classification, order, equal intervals, true zero
Observations reflect: measurable differences in total amount
Examples: weight, income, family size, number of cows in a field
- Ratio data are the highest form of data measurement and the form we are most familiar with.
- For ratio data both differences and ratios are interpretable.
- Ratio data have a natural zero.


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ratio Scales

- Examples of ratio scale data are number of computers you own, weight, height, a bank balance, number of people watching a movie, goals scored by Brazil in the World Cup, etc.
- Ratio data look a lot like interval data.
- However, the zero point has a special meaning in ratio-scaled data: it indicates the absence of whatever property is being measured.


innovative • entrepreneurial • global www.utm.my



Levels of Measurement - Ratio Scales

- Ratio data always have the flavor of counting: when you measure the amount of money that you have, you are counting up coins and bills.
- When you are measuring your height, you are counting the number of inches off the ground to the top of your head.
- Both ratio and interval data make use of a wide range of statistical analysis tools.

innovative • entrepreneurial • global www.utm.my




Levels of Measurement

	NOMINAL	ORDINAL	INTERVAL	RATIO
Indicates Difference	X	X	X	X
Indicates Difference & Direction		X	X	X
Indicates Amount of Difference			X	X
Absolute Zero				X

OK to compute....	Nominal	Ordinal	Interval	Ratio
frequency distribution.	Yes	Yes	Yes	Yes
median and percentiles.	No	Yes	Yes	Yes
add or subtract.	No	No	Yes	Yes
mean, standard deviation, standard error of the mean.	No	No	Yes	Yes
ratio, or coefficient of variation.	No	No	No	Yes

innovative • entrepreneurial • global www.utm.my



Level of Measurement	Properties	Examples	Descriptive statistics	Graphs
Nominal / Categorical	Discrete Arbitrary (no order)	Dichotomous <ul style="list-style-type: none"> • Yes / No • Gender Types / Categories <ul style="list-style-type: none"> • colour • shape 	Frequencies Percentage Mode	Bar Pie
Ordinal / Rank	Ordered categories Ranks	Ranking of favourites Academic grades	Frequencies Mode Median Percentiles	Bar Pie Stem & leaf
Interval	Equal distances between values Discrete (e.g., Likert scale) Metric (e.g., deg. F) Interval scales >5 can usually be treated as ratio	Discrete - Thoughts, behaviours, feelings, etc. on a Likert scale Metric - Deg. C or F	Frequencies (if discrete) Mode (if discrete) Median Mean SD Skewness Kurtosis	Bar (if discrete) Pie (if discrete) Stem & Leaf Boxplot Histogram (if metric)
Ratio	Continuous / Metric / Meaningful 0 allows ratio statements (e.g., A is twice as large as B)	Age Weight VO ₂ max Deg. Kelvin	Mean SD Skewness Kurtosis	Histogram Boxplot Stem&Leaf (may need to round leafs)

innovative • entrepreneurial • global www.utm.my

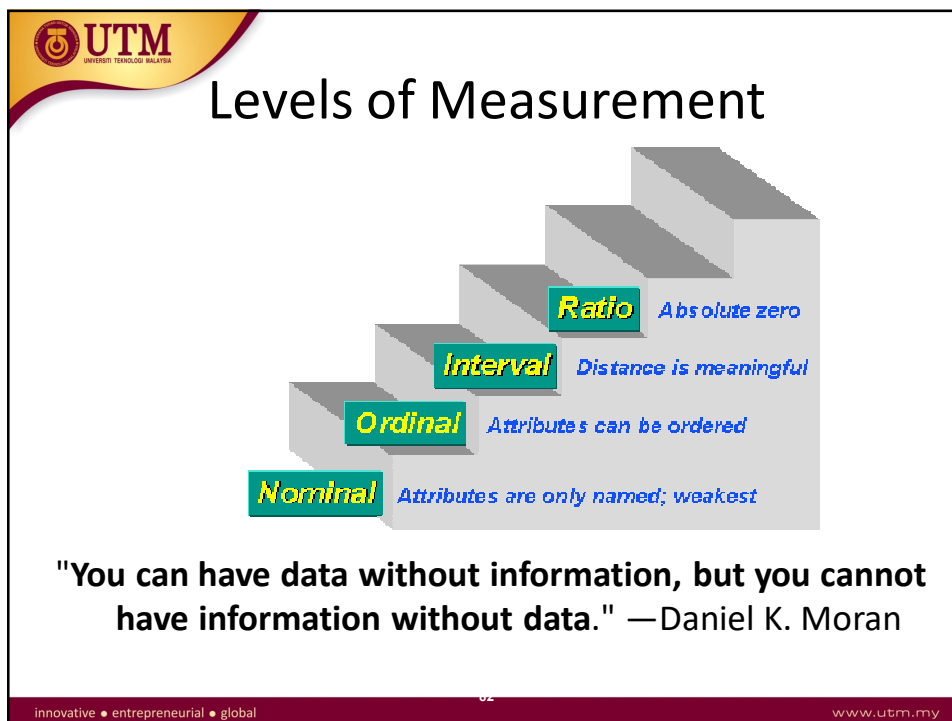
UTM
UNIVERSITI TEKNOLOGI MALAYSIA


Levels of Measurement

Statistic	Nominal	Ordinal	Interval	Ratio
Mode	√	√	√	If meaningful
Median	X	√	√	√
Range, Min. Max	X	√	√	√
Mean	X	X	If metric	√
SD	X	X	If metric	√

Graph	Nominal	Ordinal	Interval	Ratio
Bar / Pie	√	√	If discrete	X
Stem & Leaf	X	√	√	√
Boxplot	X	√	√	√
Histogram	X	X	If metric	√

innovative • entrepreneurial • global www.utm.my






Example

Scales to classify different measurements

	Nominal	Ordinal	Interval	Ratio
<i>Sex</i>	x			
<i>Hair colour</i>	x			
<i>Pulse</i>				x
<i>Temp. °C</i>			x	
<i>Team number</i>	x			
<i>Shoe size</i>		x		

83

innovative • entrepreneurial • globalwww.utm.my



Exercise

Identify the following as nominal level, ordinal level, interval level, or ratio level data.

1. Flavours of frozen yogurt
2. Amount of money in savings accounts
3. Students classified by their reading ability: Above average, Below average, Normal
4. Letter grades on an English essay
5. Religions
6. Commuting times to work
7. Ages (in years) of art students
8. Ice cream flavour preference
9. Years of important historical events
10. Instructors classified as: Easy, Difficult or Impossible

84

innovative • entrepreneurial • globalwww.utm.my

