

SUMMARY OF CHAPTER 5 TO CHAPTER 8

SCSI 2143 PROBABILITY & STATISTICAL DATA ANALYSIS

CHAPTER	TOPICS	H ₀ & H ₁	TEST STATISTICS / FORMULA
5 (P1) Point and Interval Estimator	Confidence Interval	-	$\hat{p} \pm (z_{cv}) \sqrt{\frac{\hat{p}(1-\hat{p})}{n}}$ $\bar{x} \pm (z_{cv}) \left(\frac{\sigma}{\sqrt{n}} \right)$ $s \pm (t_{cv}) \left(\frac{s}{\sqrt{n}} \right)$
5 (P2) Hypothesis Testing 1-sample	Test for Proportion	$H_0: p = \text{value}$ $H_1: p \neq \text{value}$ $H_1: p < \text{value}$ $H_1: p > \text{value}$	$z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$
	Test for Mean	$H_0: \mu = \text{value}$ $H_1: \mu \neq \text{value}$ $H_1: \mu < \text{value}$ $H_1: \mu > \text{value}$	$\sigma^2 \text{ known}$ $z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$ $\sigma^2 \text{ unknown and } n \leq 30$ $t = \frac{\bar{x} - \mu}{s / \sqrt{n}}$ $\sigma^2 \text{ unknown and } n > 30$ $z = \frac{\bar{x} - \mu}{s / \sqrt{n}}$
	Test for Variance / Standard Deviation	$H_0: \sigma = \text{value}$ $H_1: \sigma \neq \text{value}$ $H_1: \sigma < \text{value}$ $H_1: \sigma > \text{value}$	$\chi^2 = \frac{(n-1)s^2}{\sigma^2}$

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5 (P3) Hypothesis Testing 2- Sample	Test for 2-Propotions	$H_0: p_1 = p_2$ $H_1: p_1 \neq p_2$ $H_1: p_1 < p_2$ $H_1: p_1 > p_2$	$\bar{p} = \frac{x_1 + x_2}{n_1 + n_2}$ $z = \frac{(\hat{p} - \bar{p}) - (p_1 - p_2)}{\sqrt{\frac{\bar{p}\bar{q}}{n_1} + \frac{\bar{p}\bar{q}}{n_2}}}$
	Test on Difference Between 2-Mean	$H_0: \mu_1 - \mu_2 = \Delta_0$ $H_1: \mu_1 \neq \mu_2$ $H_1: \mu_1 > \mu_2$ $H_1: \mu_1 < \mu_2$	<p>σ_1^2 and σ_2^2 known</p> $z = \frac{\bar{X}_1 - \bar{X}_2 - \Delta_0}{\sqrt{\frac{\sigma_1^2}{n_1} + \frac{\sigma_2^2}{n_2}}}$ <p>σ_1^2 and σ_2^2 unknown</p> <p>Case 1: $\sigma_1^2 = \sigma_2^2$</p> $S_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$ $t = \frac{\bar{X}_1 - \bar{X}_2 - \Delta_0}{S_p \sqrt{\frac{1}{n_1} + \frac{1}{n_2}}}$ <p>σ_1^2 and σ_2^2 unknown</p> <p>Case 2: $\sigma_1^2 \neq \sigma_2^2$</p> $t = \frac{\bar{X}_1 - \bar{X}_2 - \Delta_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$ $v = \frac{\left(\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}\right)^2}{\frac{\left(s_1^2/n_1\right)^2}{n_1 - 1} + \frac{\left(s_2^2/n_2\right)^2}{n_2 - 1}}$

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5 (P3) Hypothesis Testing 2-Sample	Test on Difference Between 2-Variance / Standard Deviation	$H_0: \sigma_1 = \sigma_2$ $H_1: \sigma_1 \neq \sigma_2$ $H_1: \sigma_1 > \sigma_2$ $H_1: \sigma_1 < \sigma_2$	$F = \frac{S_1^2}{S_2^2}$
	Test on 2-Dependent Samples (Matched Pair)	$H_0: \mu_D = 0$ $H_1: \mu_D \neq 0$ $H_1: \mu_D > 0$ $H_1: \mu_D < 0$	$s_D = \sqrt{\frac{\sum D^2 - \frac{(\sum D)^2}{n}}{n-1}}$ $t = \frac{\bar{D} - \mu_D}{\frac{s_D}{\sqrt{n}}}$
6 Chi-Square & Cont. Table	1-Way Contingency	Equal Frequencies $H_0: p_1 = p_2 = \dots = p_k$ $H_1: \text{at least one } p \text{ is different}$	$E = \frac{n}{k}$
		Unequal Frequencies $H_0: p_1 = p_2 = \dots = p_k \text{ as claimed}$ $H_1: \text{at least one } p \text{ is different}$	$E = np$
	2-way Contingency	$H_0: \text{Variables are independent}$ $H_1: \text{Variables are dependent}$	$E = \frac{(i^{\text{th}} \text{ Row Total})(j^{\text{th}} \text{ Column Total})}{\text{Total Sample Size}}$ $\chi^2 = \sum \frac{(O_{i,j} - E_{i,j})^2}{E_{i,j}}$

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7 (P1)	Correlation		<p>Both Interval/Ratio Data</p> $r = \frac{\sum xy - \frac{(\sum x \sum y)}{n}}{\sqrt{\left(\sum x^2 - \frac{(\sum x)^2}{n}\right)\left(\sum y^2 - \frac{(\sum y)^2}{n}\right)}}$ <p>Both Ordinal Data</p> $r_s = 1 - \frac{6 \sum d_i^2}{n(n^2 - 1)}$
		<p>$H_0: \rho = 0$ (no correlation)</p> <p>$H_1: \rho \neq 0$ (correlation exists)</p>	$t = \frac{r}{\sqrt{\frac{1 - r^2}{n - 2}}}$
7 (P2)	Regression		$\hat{y} = b_0 + b_1x$ $b_1 = \frac{\sum xy - \frac{\sum x \sum y}{n}}{\sum x^2 - \frac{(\sum x)^2}{n}}$ $b_0 = \bar{y} - b_1\bar{x}$
		<p>$H_0: \beta_1 = 0$</p> <p>$H_1: \beta_1 \neq 0$</p>	$t = \frac{b_1 - \beta_1}{s_{b_1}}$
8 ANOVA	1-way ANOVA with Equal Sample Sizes	<p>$H_0: \mu_1 = \mu_2 = \mu_3 = \dots = \mu_n$</p> <p>$H_1$: At least one mean is different</p>	$F = \frac{ns_{\bar{x}}^2}{s_p^2}$ <p>Numerator = $k - 1$</p> <p>Denominator = $k(n - 1)$</p>