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Example

- i) The temperature on the surface of the planet Venus is 800 F.
- ii) The sun will come out tomorrow.

Propositions? Why?

- i) Is a statement since it is either true or false, but not both.
- ii) However, we do not know at this time to determine whether it is true or false.



CONJUNCTIONS

Conjunctions are:

- Compound propositions formed in English with the word "and",
- Formed in logic with the caret symbol (" \land "), and
- True only when both participating propositions are true.

TRUTH TABLE: This tables aid in the evaluation of compound propositions.								
	p	q	<mark>₽∧q</mark>					
	Т	Т	Т					
	Т	F	F					
	F	Т	F					
	F	F	F					







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DISJUNCTION

- Compound propositions formed in English with the word "or",
- Formed in logic with the caret symbol (" V "), and,
- True when one or both participating propositions are true.





DISJUNCTION (cont.)

Let *p* and *q* be propositions. The **disjunction** of *p* and *q*, written *p* V *q* is the statement formed by putting statements *p* and *q* together using the word "or". The symbol V is called "or"

The truth table for $p \lor q$:								
	<u> </u>	9	<u> </u>					
	Т	Т	Т					
	Т	F	Т					
	F	Т	Т					
	F	F	F					
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The	truth table o	f $p \leftrightarrow a$:					
		- <u>-</u>					
	n	a	$n \leftrightarrow a$				
	Ρ	9	<i>P</i> \ 7 9				
	Т	Т	Т				
	Т	F	F				
	F	Т	F				
	F	F	Т				
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LOGICAL EQUIVALENCE

• The compound propositions **Q** and **R** are made up of the propositions $p_1, ..., p_n$.

• **Q** and **R** are logically equivalent and write, $Q \equiv R$

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provided that given any truth values of $p_1, ..., p_n$, either **Q** and **R** are **both true** or **Q** and **R** are **both false**.

6	$\mathbf{Q} = p \rightarrow q$ Example						
	$R = \neg q \rightarrow$	- p					
	Show that	$at, Q \equiv R$	chows the	a + O = P			
	n n		shows the $n \rightarrow a$	at, $Q = R$			
	μ	9	$p \rightarrow q$	$\eta \rightarrow \eta p$			
	Т	Т	Т	Т			
	Т	F	F	F			
	F	Т	Т	Т			
	F	F	Т	Т			
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O U1	ГМ		Exam	ole				
Show that, $\neg (p \rightarrow q) \equiv p \land \neg q$								
T -	The truth table shows that, $\neg (p \rightarrow q) \equiv p \land \neg q$							
	p	q	ר (<i>p</i> → <i>q)</i>	<i>p</i> ∧ ¬ <i>q</i>				
	Т	Т	F	F				
	Т	F	Т	Т				
	F	Т	F	F				
incrutive e er	F	F	F	F	MONIAL LITERS POLY			

OUTM PRECEDENCE OF LOGICAL CONNECTIVES						
	Precedenc	e of logical c is as follows:	onnectives			
not	-	^	Highest			
and	\wedge					
or	\vee					
lfthen	\rightarrow					
If and only if	\leftrightarrow	I	Lowest			
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	Construct $\mathbf{A} = \neg (p \setminus Solution)$	ct the / q) → n:	truth table → (q ∧ p)	Example e for,	,			
	p	q	(p∨q)	¬(p∨q)	(q∧p)	Α		
	Т	Т	Т	F	Т	Т		
	Т	F	Т	F	F	Т		
	F	Т	Т	F	F	Т		
	F	F	F	Т	F	F		
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Logic ar	nd Sets
are closel	v related
Tautology	Set Operation Identity
$p \lor q \leftrightarrow q \lor p$	$A \cup B = B \cup A$
$p \land q \leftrightarrow q \land p$	$A \cap B = B \cap A$
$p \lor (q \lor r) \leftrightarrow (p \lor q) \lor r$	$A \cup (B \cup C) = (A \cup B) \cup C$
$p \land (q \land r) \leftrightarrow (p \land q) \land r$	A∩(B∩C)=(A∩B)∩C
$p \lor (q \land r) \leftrightarrow (p \lor q) \land (p \lor r)$	A∪(B∩C)=(A∪B)∩(A∪C
$p \land (q \lor r) \leftrightarrow (p \land q) \lor (p \land r)$	A∩(B∪C)=(A∩B)∪(A∩C
$p \land \neg q \leftrightarrow p \land \neg (p \land q)$	$A-B=A-(A\cap B)$
$p \land \neg (q \lor r) \leftrightarrow (p \land \neg q) \land (p \land \neg r)$	$A - (B \cap C) = (A - B) \cup (A - C)$
$p \land \neg (q \land r) \leftrightarrow (p \land \neg q) \lor (p \land \neg r)$	A-(B∪C)=(A-B)∩(A-C)
$p \land (q \land \neg r) \leftrightarrow (p \land q) \land \neg (p \land \neg r)$	$A \cap (B - C) = (A \cap B) - (A \cap C)$
$p \lor (q \land \neg r) \leftrightarrow (p \lor q) \land \neg (r \land \neg p)$	A∪(B-C)=(A∪B)-(C-A)
$p \land \neg \lor (q \land \neg r) \leftrightarrow (p \land \neg q) \lor (p \land r)$	$A - (B - C) = (A - B) \cup (A \cap C)$
The above identities serve as the b	asis for an "algebra of sets".









OUTM Prove: Distributive Laws							
						-	
	р	q	r	$p \vee (q \wedge r)$	(pvq) ^ (pvr)	
	Т	Т	Т	T	T		
	Т	Т	F	T	Т		
	Т	F	Т	T	Т		
	Т	F	F	T	Т		
	F	Т	Т	Т	Т		
	F	Т	F	F	F		
	F	F	Т	F	F		
	F	F	F	F	F		
				0 00	5		
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GUTM					
Prove:	Absc	orptic	on Laws		
	р	q	p∧(p∨q)	p∨(p∧q)	
	Т	T	т	т	
	T	F	T	T	
	F	Т	F	F	
	F	F	F	F	
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6	OUTM Theorem for Logic (cont.)								
De Morgan's laws:									
	$\neg (p \land q) \equiv (\neg p) \lor (\neg q)$ $\neg (p \lor q) \equiv (\neg p) \land (\neg q)$								
	The	truth	table	for ¬(<i>p</i> ∨ <i>q</i>)	≡ (¬ p) ∧	(- q)			
		р	q	¬(p∨q)	- p ^ - c	7			
		T	Т	F	F				
		T	F	F	F				
		F	Т	F	F				
	F F T T								
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