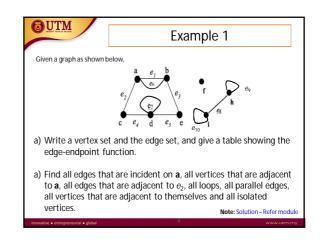
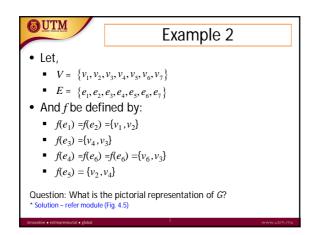
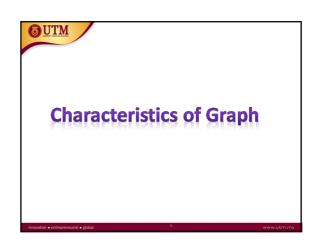


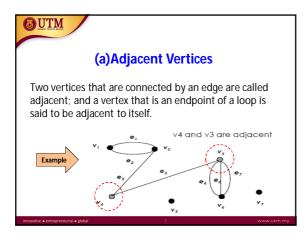
## **OUTM**

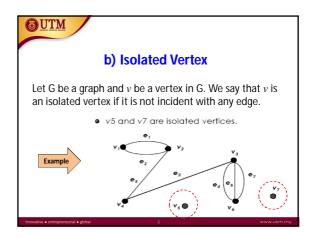
- A graph G consists of two finite sets:
  - a nonempty set *V*(*G*) of vertices.
  - a set *E*(*G*) of edges, where each edge is associated with a set consisting of either one or two vertices called its endpoints.
  - *f* is a function, called an incidence function, that assign to each edge, *e* ∈ *E*, a one element subset {*v*} or two elements subset {*v*, *w*}, where *v* and *w* are vertices.
- We can write *G* as (*V*, *E*, *f*) or (*V*, *E*) or simply as *G*.

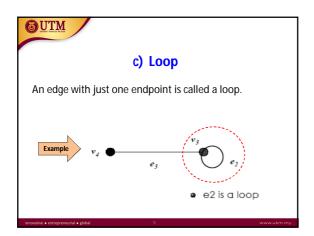


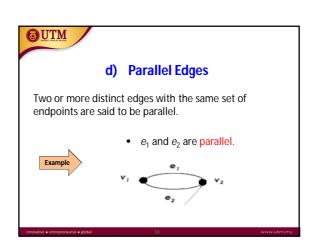








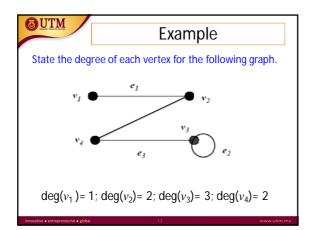


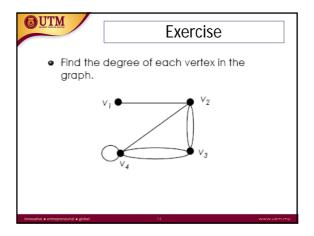


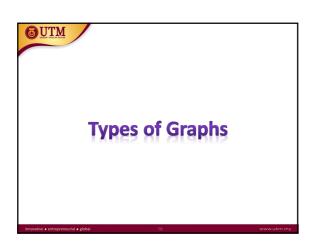


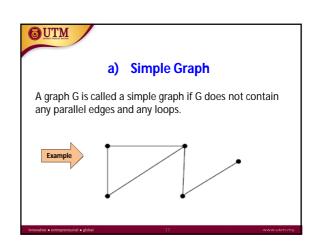


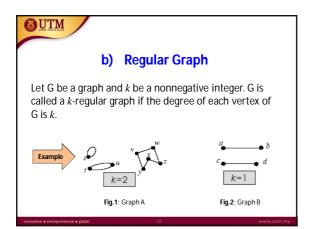
- Let G be a graph and v be a vertex in G.
- The degree of v, written deg(v) or d(v) is the number of edges incident with v.
- Each loop on a vertex v contributes 2 to the degree of v.

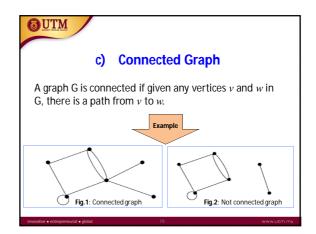


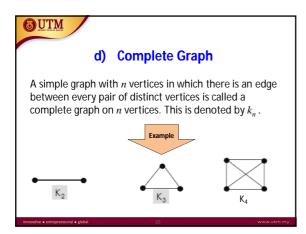


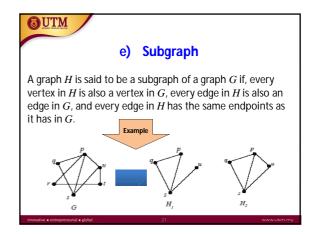


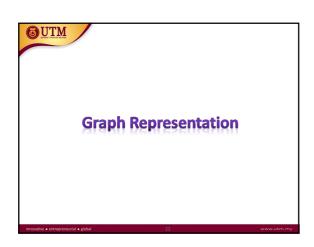






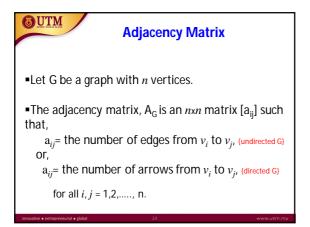


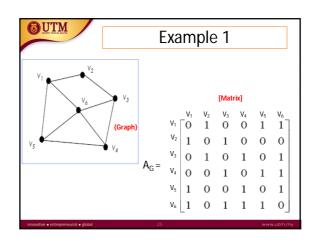


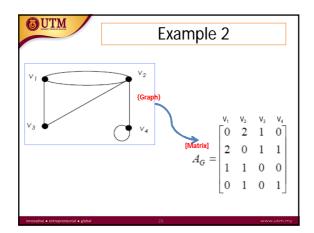


# **UTM**

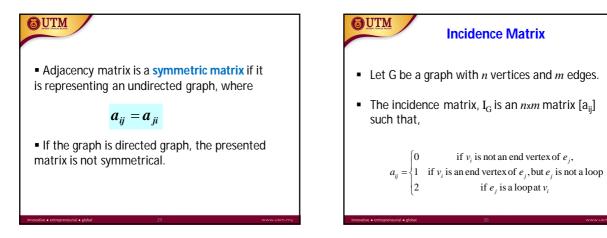
- To write programs that process and manipulate graphs, the graphs must be stored, that is, represented in computer memory.
- A graph can be represented (in computer memory) in several ways.
- 2-dimensional array: adjacency matrix and incidence matrix.

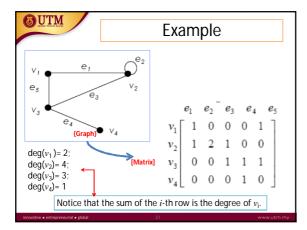


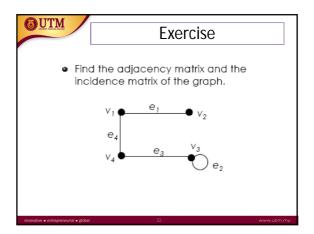




OUTM				Exa	mp	ble	93	}		]
Draw the grap	h ba	sed (	on th	ie fol	lowii	ng i	mat	trix:		
$A_G =$	1 0 1 1 0	0 0 2 0 1	1 2 0 0	1 0 0 1	0 1 0 1 0]					





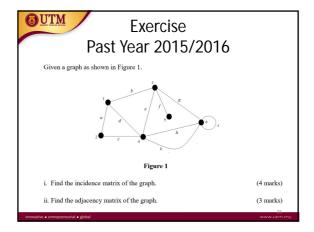


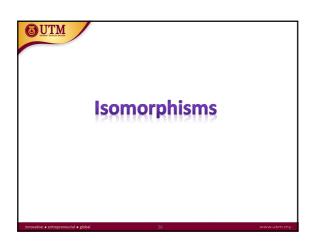
# Exercise Past Year 2015/2016

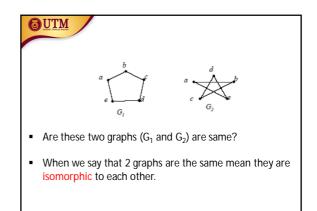
A cat show is being judged from pictures of the cats. The judges would like to see pictures of the following pairs of cats next to each other for their final decision: Fifi and Putih, Fifi and Suri, Fifi and Bob, Bob and Cheta, Bob and Didi, Bob and Suri, Cheta and Didi, Didi and Suri, Didi and Putih, Suri and Putih, Putih and Jeep, Jeep and Didi.

(3 marks)

Draw a graph modeling this situation.







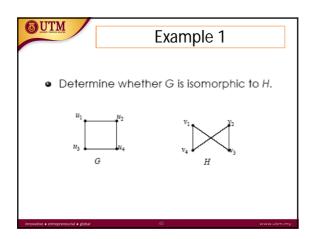
### **UTM**

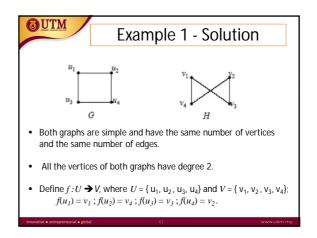
### Definition

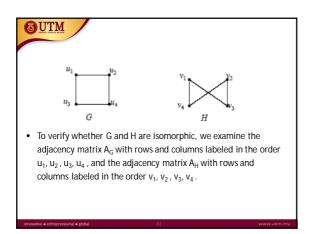
Let  $G = \{V, E\}$  and  $G' = \{V', E'\}$  be graphs. G and G' are said to be isomorphic if there exist a pair of functions  $f: V \to V'$  and  $g: E \to E'$  such that f associates each element in V with exactly one element in V' and vice versa; g associates each element in E with exactly one element in E' and vice versa, and for each  $v \in V$ , and each  $e \in E$ , if v is an endpoint of the edge e, then f(v) is an endpoint of the edge g(e).

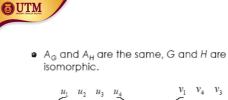
## **OUTM**

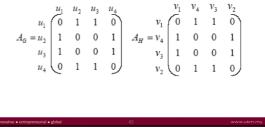
- ◆ If two graphs is isomorphic, they must have:
- the same number of vertices and edges,
- the same degrees for corresponding vertices,
- · the same number of connected components,
- the same number of loops and parallel edges,
- · both graphs are connected or both graph are not connected,
- pairs of connected vertices must have the corresponding pair of vertices connected.
- In general, it is easier to prove two graphs are not isomorphic by proving that one of the above properties fails.

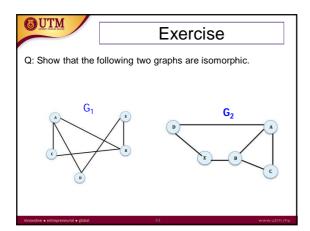


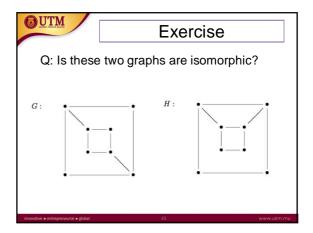


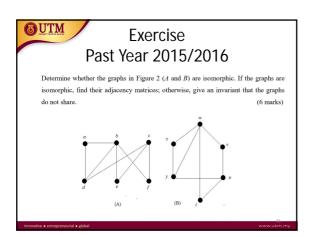




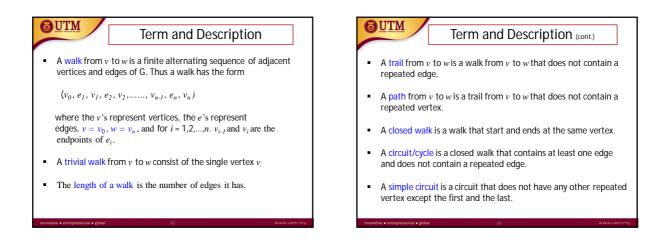


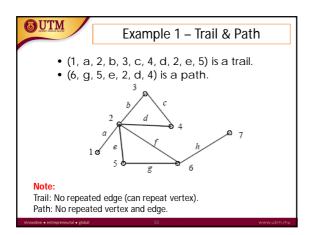


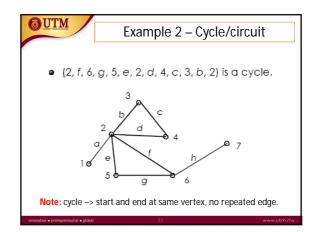


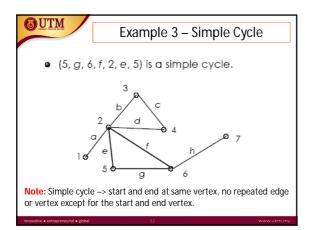


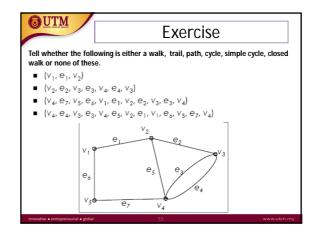


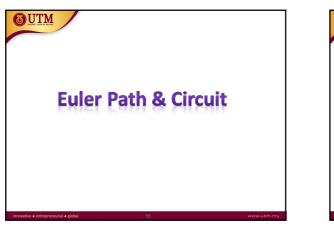




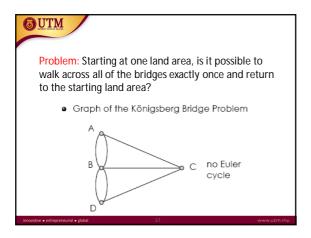


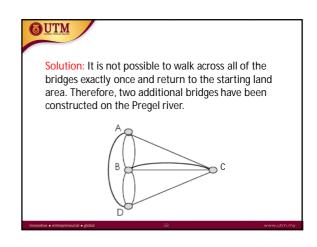








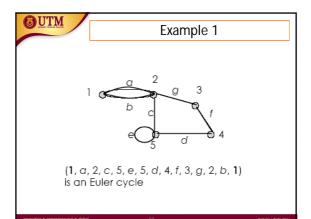


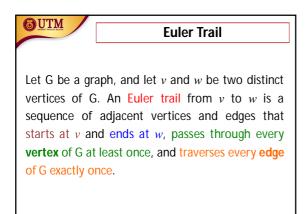


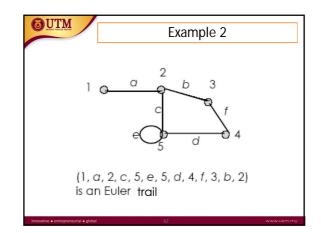
#### Euler Circuit

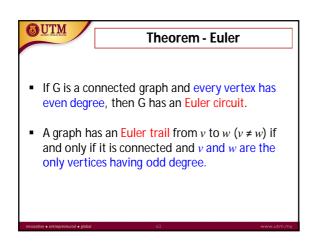
**O**UTM

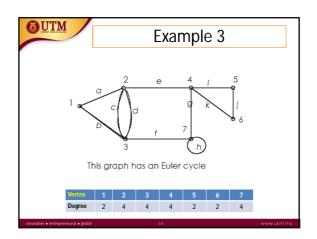
Let G be a graph. An Euler circuit for G is a circuit that contains every vertex and every edges of G. That is, an Euler circuit for G is a sequence of adjacent vertices and edges in G that has at least one edges, starts and ends at the same vertex, uses every vertex of G at least once, and uses every edge of G exactly once.

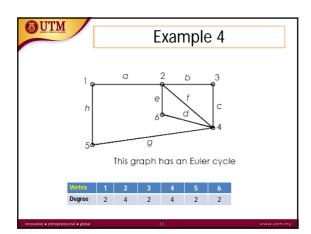


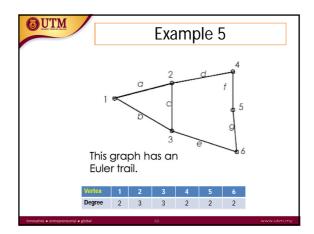


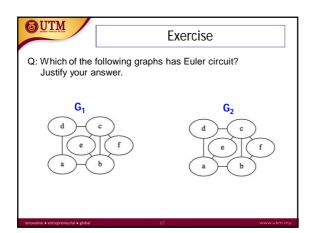


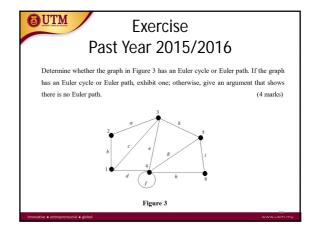


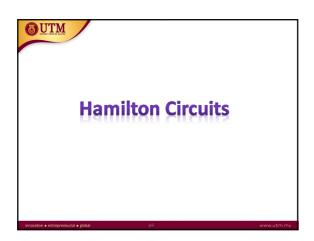


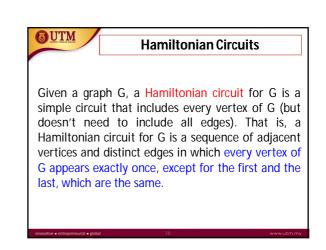


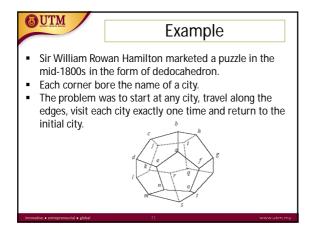


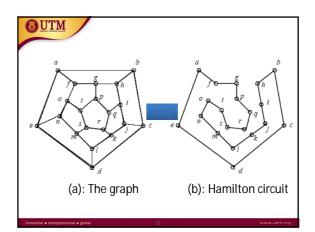


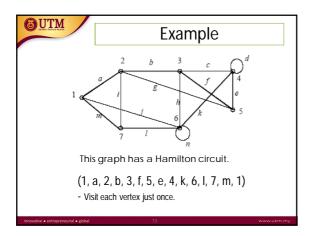


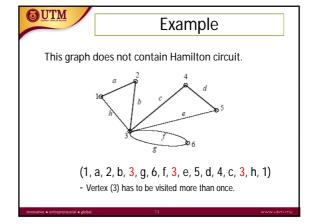


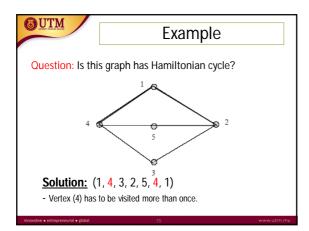


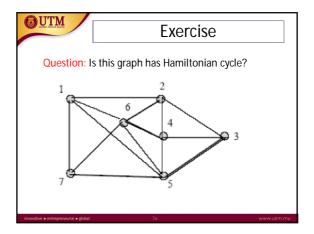


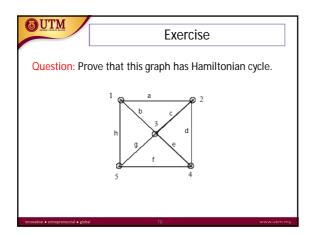


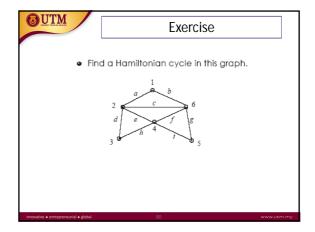


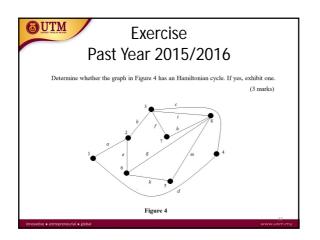


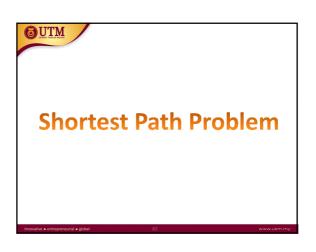


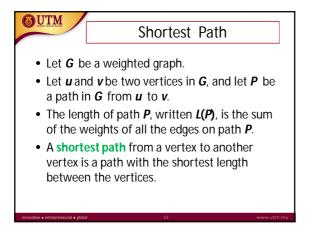


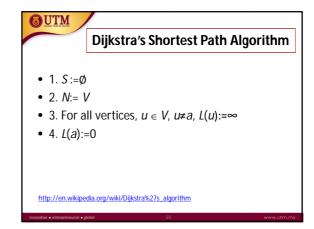




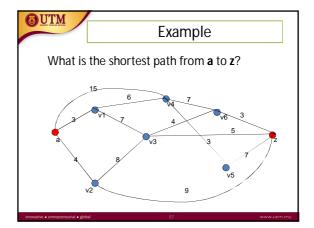


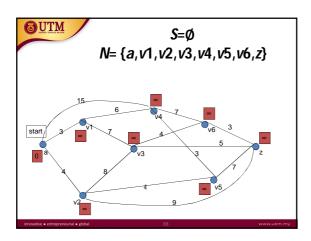


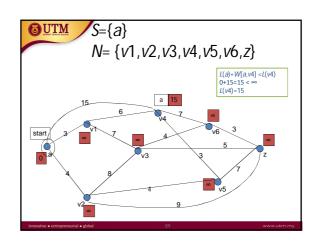


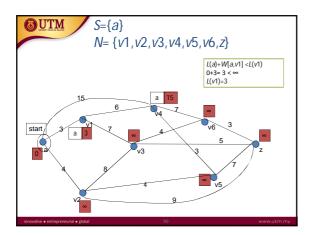


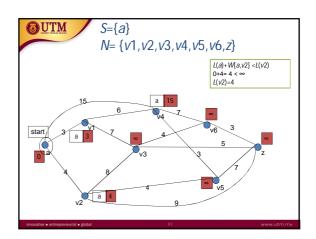
OUTM
<ul> <li>5. While <i>z</i> ∉ <i>S</i> do,</li> </ul>
5.a :Let $v \in N$ be such that
$L(v) = \min\{L(u) \mid u \in N\}$
$5.b: S = S \in \{v\}$
5.c: N:=N - {v}
5.d : For all $w \in N$ such that there is an edge
from v to w
5.d.1: If <i>L</i> ( <i>v</i> )+ <i>W</i> [ <i>v</i> , <i>w</i> ] < <i>L</i> ( <i>w</i> ) then
L(w) = L(v) + W[v, w]

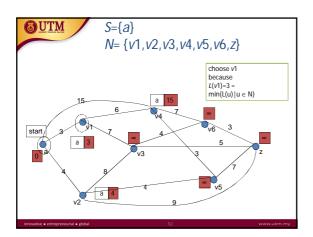


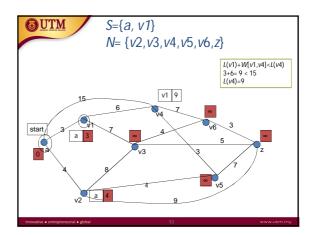


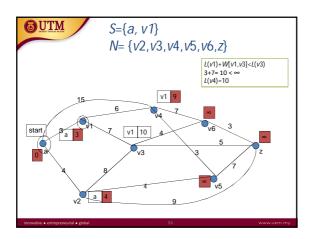


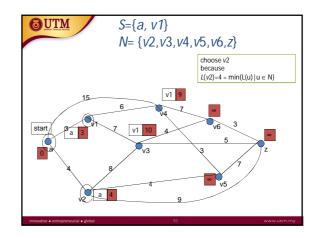


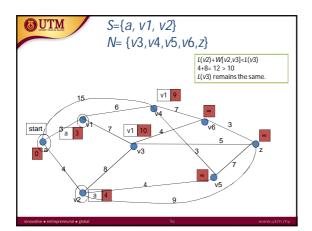


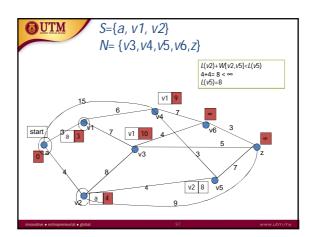


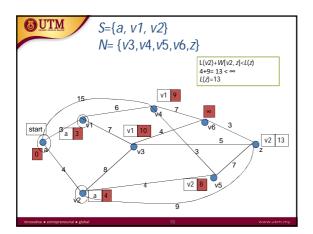


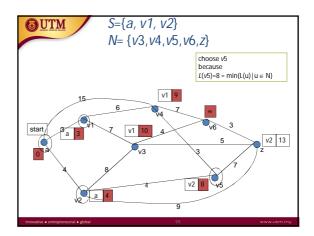


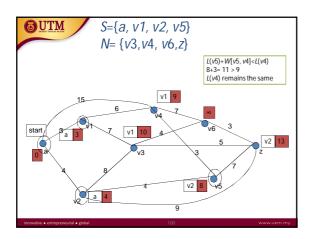


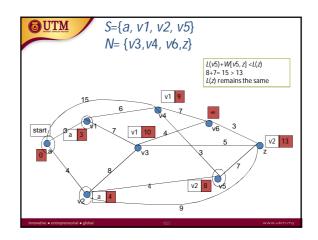


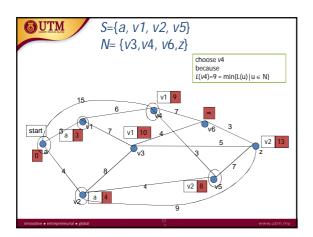


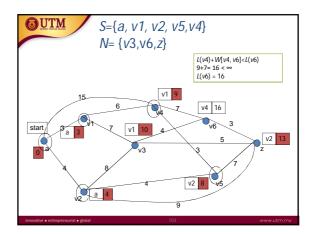


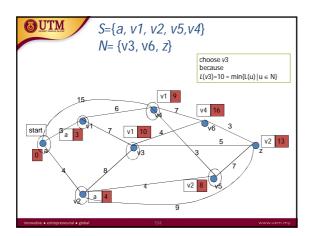


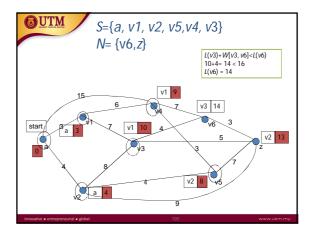


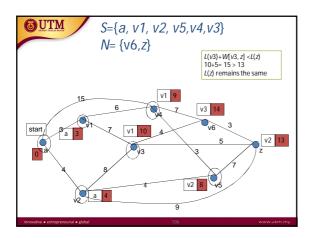


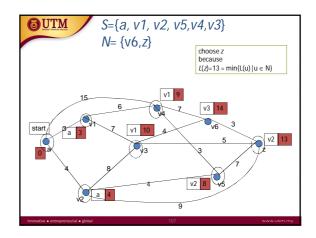


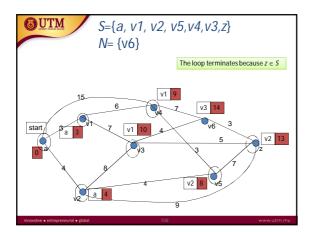


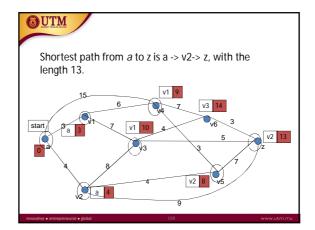












No.	S	N	L(a)	L(V:)	L(V2)	L(V3)	L(V.)	L(V3)	L(V6)	L(z
0	()	$\{a, V_1, V_2, V_3, V_4, V_5, V_6, z\}$	0	90	90	- 00	80	80	- 00	00
1	<i>{a}</i>	$\{V_1, V_2, V_3, V_4, V_5, V_6, z\}$		3	4	- 00	15	80	80	80
2	{a, V1}	$\{V_2, V_3, V_4, V_5, V_6, z\}$		3	4	10	9	8	8	90
3	$\{a, V_{l}, V_{2}\}$	$\{V_3, V_4, V_3, V_4, z\}$			4	10	9	8	80	13
4	{a, V1. V2. V3}	{V3, V4, V5, z }				10	9	8	00	13
5	{a, V1. V2. V5. V4}	{V6, <u>z.}</u>				10	9		16	13
6	$\{ \underline{a}, V_{l}, V_{2}, V_{3}, V_{4}, V_{3}, \}$	{V6, <u>z_}</u>				10			14	13
7	$\{a, V_{L}, V_{2}, V_{3}, V_{4}, V_{3}, z\}$	{ <i>V</i> <sub>0</sub> .}							14	13

