



#### **Basic Counting Principles**

 <u>Problem 3</u> - There are three boxes containing books. The first box contains 15 mathematics books by different authors, the second box contains 12 chemistry books by different authors, and the third box contains 10 computer science books by different authors. A student wants to take a book from one of the three boxes. In how many ways can the student do this?

### **OUTM**

#### **Basic Counting Principles**

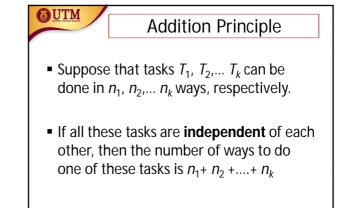
<u>Problem 4</u> - The department will award a free computer to either a CS student or a CS professor. How many different choices are there, if there are 530 students and 15 professors?



<u>Problem 5</u> - A scholarship is available, and the student to receive this scholarship must be chosen from the Mathematics, Computer Science, or the Engineering Department. How many different choices are there for this student if there are 38 qualified students from the Mathematics Department, 45 qualified students from the Computer Science Department and 27 qualified students from the Engineering Department?

# Basic Counting Principles There are a number of basic principles that we can use to solve such problems: 1) Addition Principle

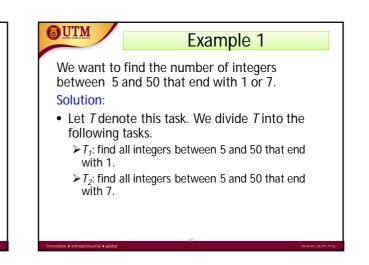
2) Multiplication Principle





**Basic Counting Principles** 

 If a task can be done in n<sub>1</sub> ways and a second task in n<sub>2</sub> ways, and if these two tasks cannot be done at the same time, then there are n<sub>1</sub> + n<sub>2</sub> ways to do either task.

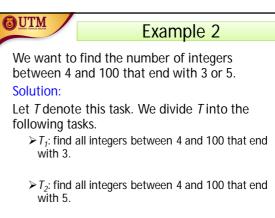


#### GUTM

- *T*<sub>1</sub>: find all integers between 5 and 50 that end with 1.
  - →11, 21, 31, 41 => 4 ways
- $T_{2^{\circ}}$  find all integers between 5 and 50 that end with 7.

→7, 17, 27, 37, 47 => 5 ways

 $.: n_1 + n_2 = 4 + 5 = 9$  ways.



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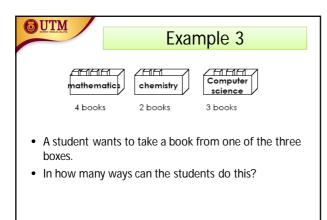
- $T_1$ : find all integers between 4 and 100 that end with 3.
  - => 13, 23, 33, 43, 53, 63, 73, 83, 93
  - => 9 integers
- $T_2$ : find all integers between 4 and 100 that end with 5.
  - => 5, 15, 25, 35, 45, 55, 65, 75, 85, 95
  - => 10 integers

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- Task  $T_1$  can be done in 9 ways.
- Task  $T_2$  can be done in 10 ways.
- The number of ways to do one of these tasks is,

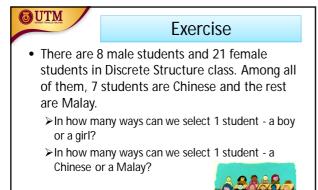
#### 9+10=19

• Task T can be completed in 19 ways.



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- *T*<sub>1</sub>: choose a mathematics book
   > 4 ways
- *T*<sub>2</sub>: choose a chemistry book
   > 2 ways
- *T<sub>3</sub>*: choose a computer science book.
   > 3 ways
- The number of ways to do one of these tasks is, >4+2+3=9





#### Multiplication Principle

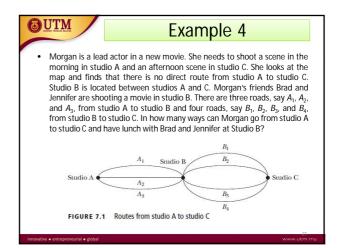
• A task *T* can be completed in *k* successive steps.

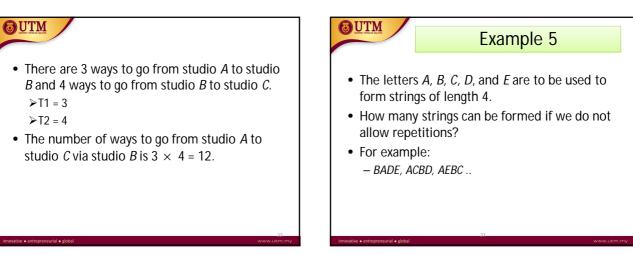
**Step 1** can be completed in  $n_1$  different ways. **Step 2** can be completed in  $n_2$  different ways. **Step k** can be completed in  $n_k$  different ways.

• Then the task *T* can be completed in  $n_1.n_2....n_k$  different ways.

#### **OUTM**

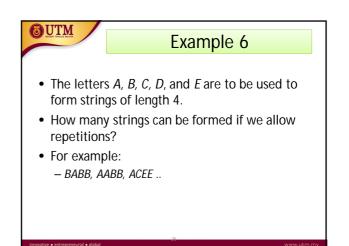
Suppose that a procedure can be broken down into two successive tasks. If there are  $n_1$ ways to do the first task and  $n_2$  ways to do the second task after the first task has been done, then there are  $n_1n_2$  ways to do the procedure.





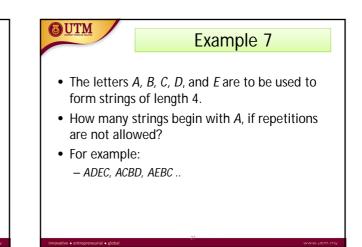
#### OUTM

- $T_1$ : choose the first letter  $\rightarrow$  5 ways
- $T_2$ : choose the second letter  $\rightarrow$  4 ways
- $T_3$ : choose the third letter  $\rightarrow$  3 ways
- $T_4$ : choose the fourth letter  $\rightarrow$  2 ways
- There are 5.4.3.2= 120 strings.



#### **OUTM**

- $T_1$ : choose the first letter  $\rightarrow$  5 ways
- $T_2$ : choose the second letter  $\rightarrow$  5 ways
- $T_3$ : choose the third letter  $\rightarrow$  5 ways
- $T_4$ : choose the fourth letter  $\rightarrow$  5 ways
- There are 5.5.5.5= 625 strings.



**OUTM** 

- $T_1$ : choose the first letter  $\rightarrow$  A (1 way)
- $T_2$ : choose the second letter  $\rightarrow$  4 ways
- $T_{3}$ : choose the third letter  $\rightarrow$  3 ways
- $T_4$ : choose the fourth letter  $\rightarrow$  2 ways
- There are 1.4.3.2= 24 strings.

#### **OUTM**

#### Exercise

- Danial, Kenny and Joseph are fighting over a turn to play a game that can only has 2 players at a time. In how many ways can we select 2 players at a time?
- Diana, Sherry, Devi and Mary are going to DSI using a motorcycle. In how many ways can we select 2 peoples to ride the motorcycle?

#### Exercise

- There are 8 male students and 21 female students in Discrete Structure class. Among all of them, 7 students are Chinese and the rest are Malay.
  - In how many ways can we select 2 students a boy and a girl?
  - In how many ways can we select 2 students a Chinese and a Malay?



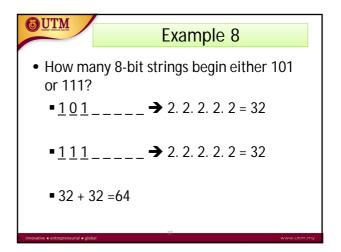
## O UTM

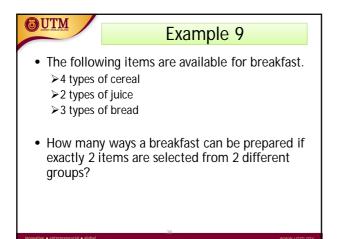
#### Exercise

• Suppose that, in order to declare a variable name in a computer language, the name must have five characters. The first character must be a letter, and the remaining characters can be letters or digits. How many different variable names are possible?

# Basic Counting Principles

- The counting problem that we have considered so far involved either the addition principle or the multiplication principle.
- Sometimes, however, we need to use both of these counting principles to solve a particular problem.







• A breakfast can be prepared in either of the following 3 ways:

➤A cereal & a juice

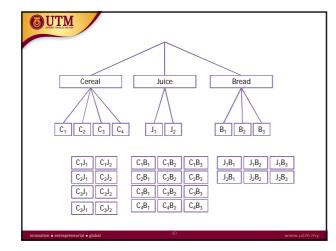
• 4. 2 = 8

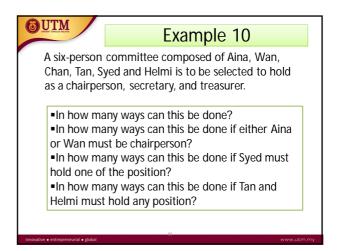
➤A cereal & a bread

• 4. 3 =12
≻A juice & a bread

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• 2. 3 = 6
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>8+12+6=26 ways





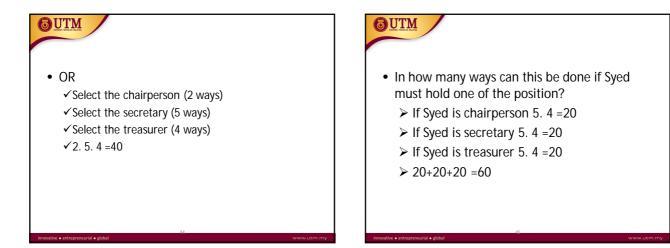
#### **OUTM**

#### Example 10 - Solution

- In how many ways can this be done?
  - Select the chairperson (6 ways)
  - Select the secretary (5 ways)
  - Select the treasurer (4 ways)
  - ▶ 6. 5. 4 =120

#### **OUTM**

In how many ways can this be done if either Aina or Wan must be chairperson?
If Aina is chairperson 5. 4 = 20
If Wan is chairperson 5. 4 = 20
20+20 = 40



#### **OUTM**

- OR
  - ➤Assign Syed for any position is 3 ways
  - Fill the highest remaining position is 5 ways
  - ➤Fill the last position is 4 ways
  - ≥3. 5. 4 =60

#### **UTM**

- In how many ways can this be done if Tan and Helmi must hold any position?
  - ➤Assign Tan 3 ways
  - ➤Assign Helmi 2 ways
  - > Fill the remaining position 4 ways
  - ≥3. 2. 4 =24

#### 

#### Exercise

- How many eight-bit strings have either the second or the fourth bit 1(or both)?
- How many license plates of 2 letters from A to Z, followed by 3 digits from 0 to 9 can be made, if repetition of letters is not allowed?

# • How many 5-digit telephone numbers can be constructed using digit 0-9 if each number starts with 67 and no digit appears more than once?