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Union

 If A and B are finite sets, the cardinality of A ∪ B,

$$|A \cup B| = |A| + |B| - |A \cap B|$$

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Intersection

 The intersection of two sets A and B, denoted by A ∩ B, is defined to be the set

$$A \cap B = \{x \mid x \in A \text{ and } x \in B\}$$

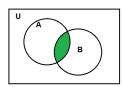
• The intersection consists of all elements belonging to both *A* and *B*.

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OUTMIntersection

Venn diagram of A ∩ B



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Example

A={1, 2, 3, 4, 5, 6}, B={2, 4, 6, 8, 10} and C={1, 2, 8, 10}

$$A \cap B = \{2, 4, 6\}$$

$$A \cap C = \{1, 2\}$$

$$C \cap B = \{2, 8, 10\}$$

 $A \cap B \cap C = \{2\}$

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Disjoint • Two sets A and B are said to

• Two sets A and B are said to be disjoint if, $A \cap B = \emptyset$ Disjoint

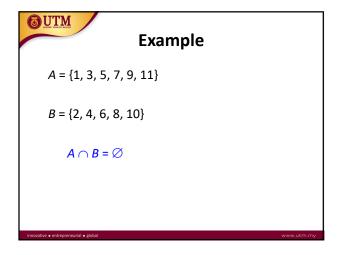
• Venn diagram, $A \cap B = \emptyset$ U

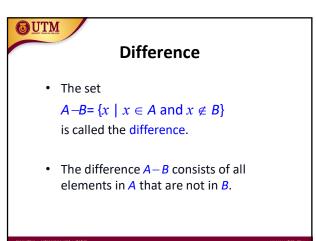
A

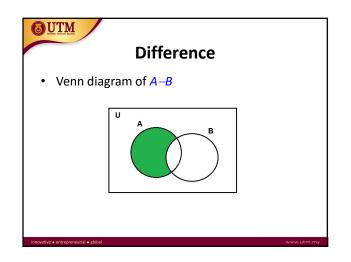
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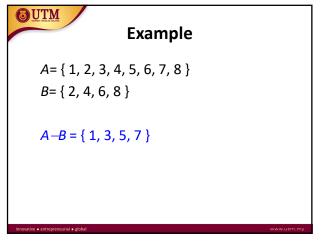
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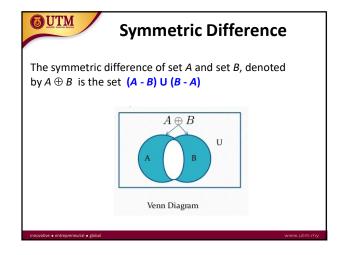
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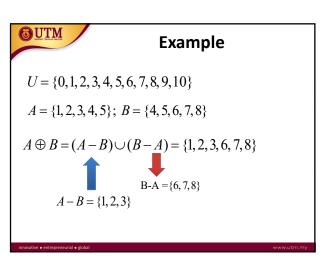












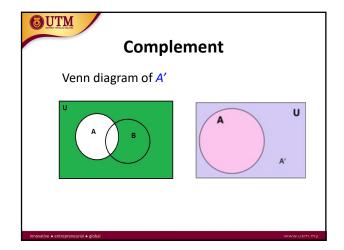
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Complement

 The complement of a set A with respect to a universal set U, denoted by A' is defined to be

$$A' = \{x \in U \mid x \notin A\}$$
$$A' = U - A$$

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Example

Let *U* be a universal set,

$$A' = U - A = \{1, 3, 5, 7\}$$

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Exercise

• Let,

$$U = \{ a, b, c, d, e, f, g, h, i, j, k, l, m \}$$

 $A = \{ a, c, f, m \}$

- $B = \{ b, c, g, h, m \}$
- Find:

 $A \cup B$, $A \cap B$, $|A \cup B|$, $A - B \operatorname{dan} A'$.

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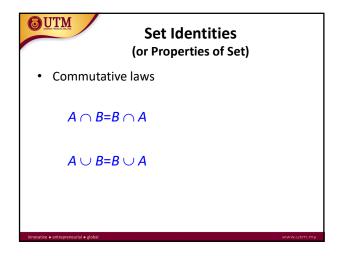
Exercise

Let the universe be the set $U=\{1, 2, 3, 4,....,10\}$.

Let $A=\{1, 4, 7, 10\}$, $B=\{1, 2, 3, 4, 5\}$ and $C=\{2, 4, 6, 8\}$.

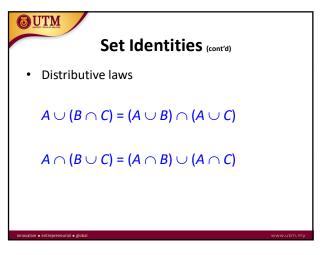
List the elements of each set:

a) U'b) $B' \cap (C-A)$ c) B-Ad) $(A \cup B) \cap (C-B)$



Set Identities (cont'd)

• Associative laws $A \cap (B \cap C) = (A \cap B) \cap C$ $A \cup (B \cup C) = (A \cup B) \cup C$



Set Identities (cont'd)

• Absorption laws

$$A \cup (A \cap B) = A$$

$$A \cap (A \cup B) = A$$

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Set Identities (cont'd)

• Idempotent laws

$$A \cap A=A$$

$$A \cup A=A$$

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Set Identities (cont'd)

• Complement laws

$$A \cap A' = \emptyset$$

$$A \cup A' = U$$

- Double complement laws: (A')' = A
- Complement of U and \emptyset :

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Set Identities (cont'd)

• De Morgan's laws

$$(A \cap B)' = A' \cup B'$$

$$(A \cup B)' = A' \cap B'$$

Set Identities (cont'd)

• Properties of universal set

$$A \cup U = U$$

$$A \cap U = A$$

• Set difference laws:

$$A - B = A \cap B'$$

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Set Identities (cont'd)

• Identity laws:

$$A \cup \emptyset = A$$

$$A \cap U = A$$

• Properties of empty set:

$$A \cup \emptyset = A$$

$$A \cap \emptyset = \emptyset$$

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Example

- Let A, B and C denote the subsets of a set S and let C' denote a complement of C in S.
- If $A \cap C = B \cap C$ and $A \cap C' = B \cap C'$, then prove that A = B

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Example

 $A = A \cap S$

 $=A\cap (C\cup C')$

 $= (A \cap C) \cup (A \cap C')$ by distributivity

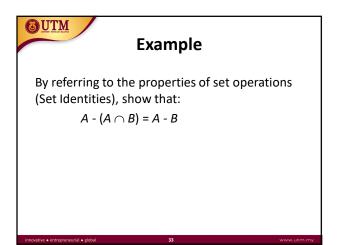
 $= (B \cap C) \cup (B \cap C')$ by the given conditions

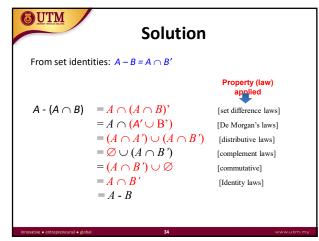
 $= B \cap (C \cup C')$ by distributivity

 $=B\cap S$

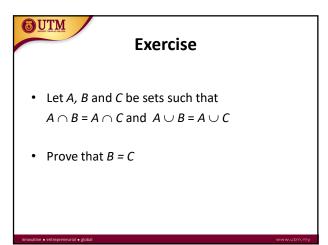
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Exercise • Let A, B and C be sets. • Show that $(A \cup (B \cap C))' = A' \cap (B' \cup C')$



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Generalized Unions and Intersections

The *union* of a collection of sets is the set that contains those elements that are members of at least one set in the collection.

Notation:

- $\bigcap_{i=1}^{n} A_i = A_1 \cup A_2 \cup \square \quad \cup A_n = \left\{ x \in U \middle| x \in A_i \text{ for at least one } i = 0, 1, 2, \dots, n \right\}$
- $\bigcap_{i=1}^{\infty}A_i=A_1\cup A_2\cup \square \ \cup A_n=\left\{x\in U\big|x\in A_i \text{ for at least one nonnegative integer } i\right\}$

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Generalized Unions and Intersections

(cont'd)

The *intersection* of a collection of sets is the set that contains those elements that are members of all the sets in the collection.

Notation:

- $\bigcap_{i=1}^{n} A_{i} = A_{1} \cap A_{2} \cap \square \cap A_{n} = \left\{ x \in U \middle| x \in A_{i} \text{ for all } i = 0, 1, 2, \dots, n \right\}$
- $\bigcup_{i=1}^{\infty} A_i = A_1 \cap A_2 \cap \square \cap A_n = \left\{ x \in U \middle| x \in A_i \text{ for all nonnegative integer } i \right\}$

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Example

For $i = 1, 2, \ldots$, let $A_i = \{i, i+1, i+2, \ldots\}$. Then,

$$\bigcap_{i=1}^{n} A_{i} = \bigcap_{i=1}^{n} \{i, i+1, i+2, \dots\} = \{1, 2, 3, \dots\},$$

and

$$\bigcap_{i=1}^{n} A_{i} = \bigcap_{i=1}^{n} \{i, i+1, i+2, \dots\} = \{n, n+1, n+2, \dots\} = A_{n}$$

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Cartesian Product

- Let A and B be sets.
- An ordered pair of elements a∈A dan b∈B written (a, b) is a listing of the elements a and b in a specific order.
- The ordered pair (a, b) specifies that a is the first element and b is the second element.

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Cartesian Product

- An ordered pair (a, b) is considered distinct from ordered pair (b, a), unless a=b.
- Example $(1, 2) \neq (2, 1)$

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Cartesian Product

 The Cartesian product of two sets A and B, written A×B is the set,

$$A \times B = \{(a,b) \mid a \in A, b \in B\}$$

For any set A,

$$A \times \emptyset = \emptyset \times A = \emptyset$$

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Example

$$A = \{a, b\}, B = \{1, 2\}.$$

$$A \times B = \{(a, 1), (a, 2), (b, 1), (b, 2)\}$$

$$B \times A = \{(1, a), (1, b), (2, a), (2, b)\}$$

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Cartesian Product

- if $A \neq B$, then $A \times B \neq B \times A$.
- if |A| = m and |B| = n, then $|A \times B| = mn$.

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Example

• $A = \{1, 3\}, B = \{2, 4, 6\}.$

$$A \times B = \{(1, 2), (1, 4), (1, 6), (3, 2), (3, 4), (3, 6)\}$$

 $B \times A = \{(2, 1), (2, 3), (4, 1), (4, 3), (6, 1), (6, 3)\}$

$$A \neq B$$
, $A \times B \neq B \times A$
 $|A| = 2$, $|B| = 3$, $|A \times B| = 2.3 = 6$.

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Cartesian Product

 The Cartesian product of sets A₁, A₂,, A_n is defined to be the set of all n-tuples

 $(a_1, a_2,...a_n)$ where $a_i \in A_i$ for i=1,...,n;

• It is denoted $A_1 \times A_2 \times \dots \times A_n$ $|A_1 \times A_2 \times \dots \times A_n| = |A_1| \cdot |A_2| \cdot \dots \cdot |A_n|$

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Example

• $A = \{a, b\}, B = \{1, 2\}, C = \{x, y\}$

 $A \times B \times C = \{(a,1,x),(a,1,y), (a,2,x), (a,2,y), (b,1,x), (b,1,y), (b,2,x), (b,2,y)\}$

• $|A \times B \times C| = 2.2.2 = 8$

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Exercise

- Let $A = \{w, x\}$, $B = \{1, 2\}$ and $C = \{KB, SD, PS\}$.
- Find | A×B |, | B×C |, | A×C |, | A×B×C |, | B×C×A |, | A×B×A×C |
- · Determine the following set,
 - a) $A \times B$, $B \times C$, $A \times C$
 - b) $A \times B \times C$
 - c) $B \times C \times A$
 - d) $A \times B \times A \times C$

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Exercise

- Let $X = \{1,2\}$, $Y = \{a\}$ and $Z = \{b,d\}$.
- List the elements of each set.
 - a) $X \times Y$
 - b) Y×X
 - c) $X \times Y \times Z$
 - d) $X \times Y \times Y$
 - e) X×X×X
 - f) $Y \times X \times Y \times Z$

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