

Group 3

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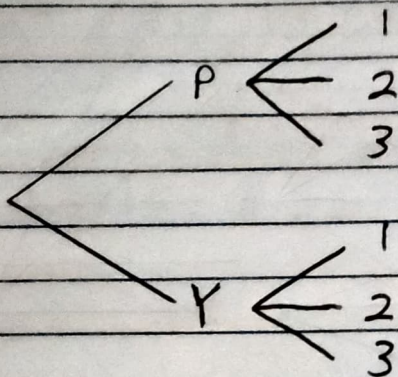
Question 1

Date

No.

1 a) $S = \{(P, 1), (P, 2), (P, 3), (P, 4), (G, 1), (G, 2), (G, 3), (G, 4), (Y, 1), (Y, 2), (Y, 3), (Y, 4)\}$

b)



c) $P_2 = \frac{1}{3} \times \frac{1}{4}$
 $= \frac{1}{12}$
 $= 0.0833$

2. a) i. $P(S) = \frac{8}{25}$
 $= 0.32$

ii. $P(X) = \frac{10}{25}$
 $= \frac{2}{5}$
 $= 0.4$

$P(S \cup X) = \frac{10}{25}$
 $= \frac{2}{5}$
 $= 0.4$

$$\begin{aligned} b) S \cup X &= 25 - 10 \\ &= 15 \end{aligned}$$

$$\begin{aligned} c) S \cap X &= (10 + 8) - 15 \\ &= 18 - 15 \\ &= 3 \end{aligned}$$

$$\begin{aligned} d) S &= 8 - 3 \\ &= 5 \end{aligned}$$

$$\begin{aligned} 3. a) P(B) &= \frac{8}{30} \\ &= \frac{4}{15} \\ &= 0.2667 \end{aligned}$$

$$\begin{aligned} b) P(M|B) &= \frac{\frac{3}{30}}{\frac{4}{15}} \\ &= \frac{3}{8} \\ &= 0.375 \end{aligned}$$

$$\begin{aligned} c) P(M \cup B) &= \frac{12}{30} + \frac{8}{30} - \frac{3}{30} \\ &= \frac{17}{30} \\ &= 0.5667 \end{aligned}$$

Question 2

Heng Xing Yu

$$1. a) P(X=2) = \frac{3}{8} = 0.3750$$

$$\begin{aligned} b) P(X \geq 2) &= P(X=2) + P(X=3) \\ &= \frac{3}{8} + \frac{1}{8} \\ &= \frac{4}{8} \\ &= \frac{1}{2} \\ &= 0.5000 \end{aligned}$$

$$\begin{aligned} c) P(X \leq 2) &= P(X=0) + P(X=1) + P(X=2) \\ &= \frac{1}{8} + \frac{3}{8} + \frac{3}{8} \\ &= \frac{7}{8} \\ &= 0.8750 \end{aligned}$$

$$\begin{aligned} d) P(X=0) + P(X=3) &= \frac{1}{8} + \frac{1}{8} \\ &= \frac{2}{8} \\ &= \frac{1}{4} \\ &= 0.2500 \end{aligned}$$

$$\begin{aligned} \text{1) a) } P(X \geq 10) &= 0.05 + 0.12 + 0.06 \\ &= 0.2300 \end{aligned}$$

$$\begin{aligned} \text{b. } P(X > 10) &= 0.12 + 0.06 \\ &= 0.1800 \end{aligned}$$

$$\begin{aligned} \text{c. } P(X < 4) &= 0.11 + 0.07 \\ &= 0.1800 \end{aligned}$$

$$\begin{aligned} \text{d. } P(4 \leq X \leq 9) &= 0.13 + 0.28 + 0.18 \\ &= 0.5900 \end{aligned}$$

$$\begin{aligned} \text{e. } P(3 < X < 10) &= 0.13 + 0.28 + 0.18 \\ &= 0.5900 \end{aligned}$$

$$\text{f. } P(7 < X < 9) = 0.0000$$

$$\begin{aligned} \text{3a) } P(X \geq 1) &= 1 - P(X = 0) \\ &= 1 - 0.05 \\ &= 0.9500 \end{aligned}$$

$$\begin{aligned} \text{b) } P(X \geq 3) &= 0.25 + 0.15 + 0.1 + 0.05 \\ &= 0.5500 \end{aligned}$$

$$\begin{aligned} \text{c) } P(X \leq 5) &= 1 - P(X = 6) \\ &= 1 - 0.05 \\ &= 0.9500 \end{aligned}$$

$$\begin{aligned} \text{d) } P(2 \leq X \leq 4) &= 0.3 + 0.25 + 0.15 \\ &= 0.7000 \end{aligned}$$

$$\begin{aligned} \text{e) } P(X = 0) + P(X = 2) + P(X = 4) + P(X = 6) &= 0.05 + 0.3 + 0.15 + 0.05 \\ &= 0.5500 \end{aligned}$$

Assignment 3

Q3 Binomial

1. a. i. $\frac{1}{50}$

$n=50, p=0.02$

ii. $P(\text{rejected}) = P(X > 1) = 1 - P(X \leq 1)$
 $= 1 - [P(X=0) + P(X=1)]$

$= 1 - \left[\binom{50}{0} \times 0.02^0 \times (1-0.02)^{50-0} + \binom{50}{1} \times (0.02)^1 \times (1-0.02)^{50-1} \right]$
 $= 1 - [0.364 + 0.371]$
 $= 0.261 //$

$\lambda = 20$

b. $X \sim P_0(20) \rightarrow P(X \geq 3)$

$= 1 - P(X \leq 2)$

$= 1 - 0.0000 \rightarrow \text{from table}$

$= 1 //$

$$2. a. P(\text{folding bike}) = 0.60 \quad n=12$$

$$P(\text{maintain bike}) = 0.40$$

$$P(X=4) = {}^{12}C_4 \times 0.60^4 \times (1-0.60)^{12-4}$$

$$= 0.0420 //$$

$$b. P(4 \leq X \leq 7)$$

$$P(X=4) + P(X=5) + P(X=6) + P(X=7)$$

$$\left({}^{12}C_4 \times 0.60^4 \times (1-0.60)^{12-4} \right) + \left({}^{12}C_5 \times 0.60^5 \times (1-0.60)^{12-5} \right) +$$

$$\left({}^{12}C_6 \times 0.60^6 \times (1-0.60)^{12-6} \right) + \left({}^{12}C_7 \times 0.60^7 \times (1-0.60)^{12-7} \right)$$

$$= 0.5466 //$$

$$c. P(X=2)$$

$$P = 0.40$$

$$= {}^{12}C_2 \times (0.4)^2 \times (1-0.4)^{12-2}$$

$$= 0.0639 //$$

3. a. ^{binomial} $n = 15$ $p = 0.25$

$$\begin{aligned}
 P(3 \leq X \leq 6) &= P(X=3) + P(X=4) + P(X=5) + P(X=6) \\
 &= \binom{15}{3} \times 0.25^3 \times (1-0.25)^{15-3} + \binom{15}{4} \times 0.25^4 \times (1-0.25)^{15-4} \\
 &\quad + \binom{15}{5} \times 0.25^5 \times (1-0.25)^{15-5} + \binom{15}{6} \times 0.25^6 \times (1-0.25)^{15-6} \\
 &= 0.7073 //
 \end{aligned}$$

b. $P(X < 4) = P(X=3) + P(X=2) + P(X=1) + P(X=0)$

$$\begin{aligned}
 &= \binom{15}{3} \times 0.25^3 \times (1-0.25)^{15-3} + \binom{15}{2} \times 0.25^2 \times (1-0.25)^{15-2} \\
 &\quad + \binom{15}{1} \times 0.25^1 \times (1-0.25)^{15-1} + \binom{15}{0} \times 0.25^0 \times (1-0.25)^{15-0} \\
 &= 0.4613 //
 \end{aligned}$$

c. $P(X > 5) = 1 - P(X \leq 5)$

$$\begin{aligned}
 &= 1 - [P(X=4) + P(X=3) + P(X=2) + P(X=1) + P(X=0) \\
 &\quad + P(X=5)] \\
 &= 1 - \left[\binom{15}{4} \times 0.25^4 \times (1-0.25)^{15-4} + \binom{15}{3} \times 0.25^3 \times (1-0.25)^{15-3} \right. \\
 &\quad + \binom{15}{2} \times 0.25^2 \times (1-0.25)^{15-2} + \binom{15}{1} \times 0.25^1 \times (1-0.25)^{15-1} \\
 &\quad \left. + \binom{15}{0} \times 0.25^0 \times (1-0.25)^{15-0} + \binom{15}{5} \times 0.25^5 \times (1-0.25)^{15-5} \right] \\
 &= 1 - 0.8516 = 0.1484 //
 \end{aligned}$$

Question 4

Hong King Yu

$$1) a) P(x=3) = (0.80)^{3-1} (0.20) \\ = 0.1280$$

$$b) P(x=7) = {}^{7-1}C_{31} (0.2)^3 (0.8)^4 \\ = 0.0492$$

$$c) \mu = \frac{1}{p} \\ = \frac{1}{0.20} \\ = 5$$

$$\sigma^2 = \frac{(1-p)}{p^2} \\ = \frac{1-0.20}{0.20^2} \\ = 20$$

2) a) It is Geometry Experiment. It is because not sure how many of the number of other participants and it looks infinite for the other participant. We need to ask them until the first participant who brings the charger appears.

b) x is a random variable with probability of success to find a participant who brings the laptop charger for each trial.

$$c) P(x=1) = (1-0.40)^{1-1} (0.40)^1 \\ = 0.40$$

$$d) P(x=1) = 0.40 \\ P(x=2) = (1-0.40)^{2-1} (0.40) \\ = 0.24$$

$$P(x=3) = (1-0.40)^{3-1} (0.40) \\ = 0.144$$

$$P(x \leq 3) = 0.40 + 0.24 + 0.144 = 0.784$$

Name: Gan Jia Hui

Matric no: A21FC0177

Section: 09

$$1. a) P(x=178) = P\left(z = \frac{178-163}{8}\right) \quad P(x=178) = 0.0301 \times 100$$

$$= P(z=1.88) \quad = 3.01\% *$$

$$= 0.0301$$

$$b) 5000 \times 0.0301 = 151 \text{ ppl} *$$

$$c) \quad \begin{array}{l} \text{Graph: Normal distribution curve with area to the right of } z=0.95 \text{ shaded. } P=0.1700 \\ z=0.95 \end{array}$$

$$0.95 = \frac{x-163}{8}$$

$$x = 170.6 \text{ cm} *$$

$$2. a) P(x=30) = {}^{180}C_{30} (0.21)^{30} (0.79)^{150} = 0.0271 *$$

$$b) P(30 < x < 35) = P(30) + P(31) + P(32) + P(33) + P(34) + P(35)$$

$$= {}^{180}C_{30} (0.21)^{30} (0.79)^{150} +$$

$${}^{180}C_{31} (0.21)^{31} (0.79)^{149} +$$

$${}^{180}C_{32} (0.21)^{32} (0.79)^{148} +$$

$${}^{180}C_{33} (0.21)^{33} (0.79)^{147} +$$

$${}^{180}C_{34} (0.21)^{34} (0.79)^{146} +$$

$${}^{180}C_{35} (0.21)^{35} (0.79)^{145} +$$

$$= 0.0271 + 0.0349 + 0.0432 + 0.0514 + 0.0591 + 0.0656$$

$$= 0.2813 *$$

$$c) \text{ mean, } \mu = np \quad \text{Std, } \sigma = \sqrt{npq}$$

$$= (180)(0.21) \quad = \sqrt{(180)(0.21)(0.79)} \quad N(37.8, 5.46)$$

$$= 37.8 \quad = 5.46$$

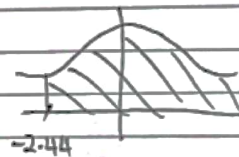
$$P(x \geq 25) = P(x \geq 25 - 0.5)$$

$$= P\left(z \geq \frac{24.5 - 37.8}{5.46}\right)$$

$$= P(z \geq -2.44)$$

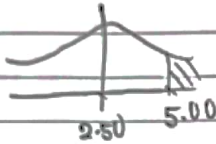
$$= 1 - 0.0073$$

$$= 0.9927 *$$



$$\begin{aligned}
 \text{d) } P(X \leq 28) &= P(Z \leq \frac{28 - 37.8}{5.46}) \\
 &= P(Z \leq -1.70) \\
 &= 0.0446
 \end{aligned}$$

3.9)



$$\begin{aligned}
 P(X > 5) &= P(Z > \frac{5 - 2.50}{0.83}) \\
 &= P(Z > 3.01)
 \end{aligned}$$

$$\begin{aligned}
 \text{b) } P(X > 5) &= P(Z > \frac{5 - 2.50}{0.83}) \\
 &= P(Z > 3.01) \\
 &= 0.0013
 \end{aligned}$$

$$\begin{aligned}
 \text{c) } P(X < 1.47) &= P(Z < \frac{1.47 - 3}{1.50}) \\
 &= P(Z < -1.02) \\
 &= 0.1539 \\
 &= 15.39\%
 \end{aligned}$$

