

Answers

1. $4P4 = 4$ rankings
2. $5P3 = 60$
3. $\frac{14!}{2!3!4!} = 302702400$
4. ${}_{12}P7 = 3991680$
5. ${}_{26}P10 = 1.9275 \times 10^{13}$ ways
6. $3 + 2 + 4 = 9$
7.
 - a. ${}_{12}C5 = 1287$
 - b. ${}_{5}C1 \times {}_{3}C1 \times {}_{3}C1 \times {}_{2}C1 = 90$
 - c. ${}_{5}C2 \times {}_{3}C2 \times {}_{3}C1 = 90$
 - d. $5 \times 3 \times 3 \times 2 + (5 \times 3 \times {}_{3}C2) = 135$
8.
 - a. $(5-1)! = 24$
 - b. $2! \times (4-1)! = 12$
 - c. $(3-1)! = 2$
 - d. ${}_{5}P3 = 60$
9.
 - a. ${}_{17}C12 = 6188$
 - b. $({}_{3}C3 \times {}_{4}C2 \times {}_{4}C2) + ({}_{3}C3 \times {}_{4}C3 \times {}_{4}C1) = 52$
10.
 - a. ${}_{10}C6 \times {}_{12}C6 = 194040$
 - b. ${}_{12}C12 + ({}_{12}C11 + {}_{10}C1) + ({}_{12}C10 \times {}_{10}C2) + ({}_{12}C9 \times {}_{10}C3) + ({}_{12}C8 \times {}_{12}C4) + ({}_{12}C7 \times {}_{10}C5) = 333025$
11. $N = 5(4-1)+1 = 16$
12. $N = 101(2-1)+1 = 102$
13. $N = 5(6-1)+1 = 26$
14. Let computers be 1,2,3,4,5,6. Let a_r be number of computers connected to a certain computer r is connected. We cannot have a case where $a_r = 0$ and a_t for some other computer t is 5. Therefore, the connections for a_r may only be $\{0,1,2,\dots,4\}$ or $\{1,2,3,4,5\}$. In this case, number of computer $> a_r$, so there exists at least 2 computers with the same number of connections.
15.
 - a. $N = 2(3-1)+1 = 5$
 - b. 13 balls.